

A Step Towards the Cognitive Radar: Target Detection under Nonstationary Clutter

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Outline

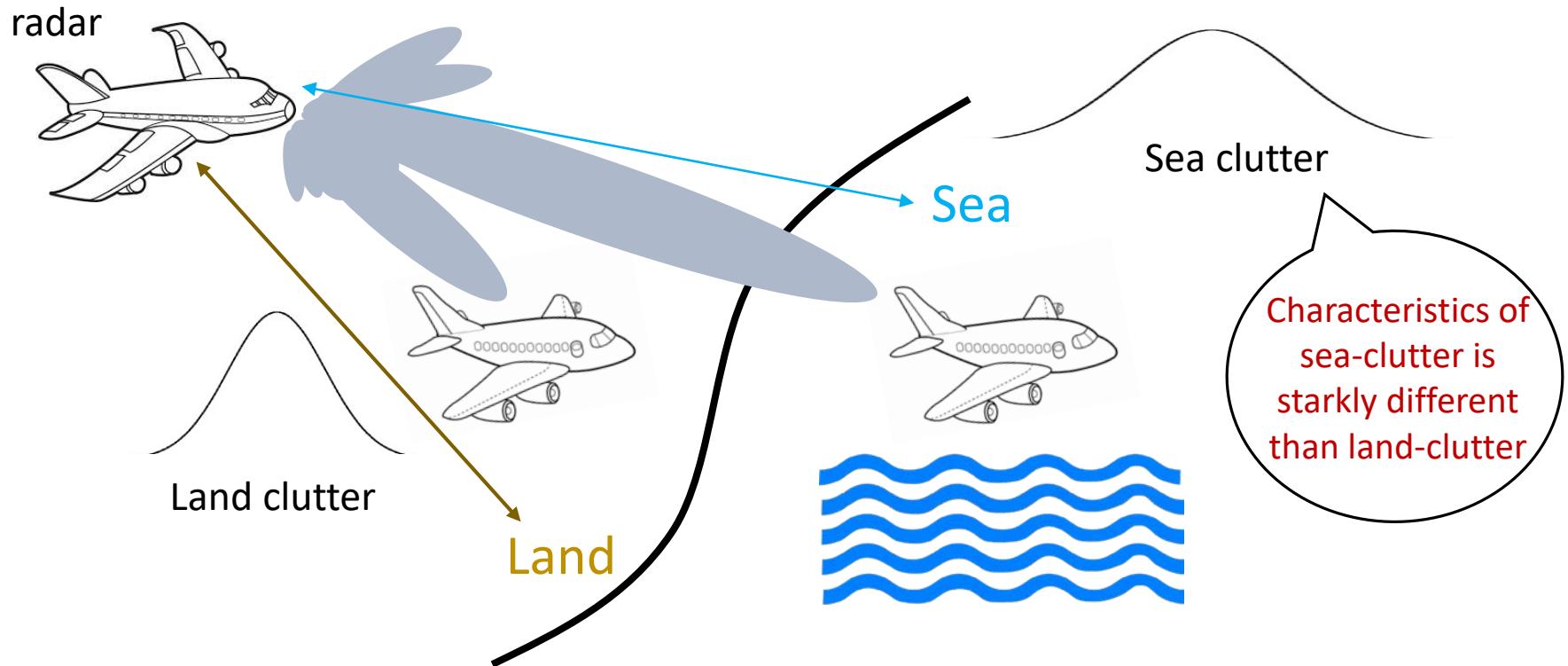
- Introduction
 - Challenges
 - Motivations
 - Our approach
 - Relevance to DDDAS
- Target Detection Method
 - Change point detection
 - CUSUM
 - Extended CUSUM
- Numerical Results
- Conclusions and Future Work

Introduction

Problem Description

- Goal:
 - Improve target detection capability in the presence of nonstationary clutter.
- Challenges:
 - Characteristics of the clutter can vary enormously depending on radar-operational scenarios (e.g., weather change, dynamic target, and changes in the environment).
 - However, most existing radar algorithms
 - assume stationary, parametric distributions for the clutter and noise processes,
 - consider the availability of a dictionary of possible probability density functions (pdfs),
 - do not address the problem of estimating the time instant when the characteristics of the clutter changes.
 - Therefore, the radar performance can severely deteriorate when the inherent nonstationary characteristics are not accounted for.

Problem Description (cont.)



An illustrative example of target detection in nonstationary environment

Motivation

- Cognitive radar framework conceptualizes an advanced radar system that
 - **senses** its scenario effectively,
 - **learns** from its experience,
 - **adapts** to the changes.
- Thus, in a nonstationary environment, a cognitive radar provides a unifying approach by
 - autonomously learning and estimating the change-point in the statistical characteristics of the scenario,
 - incorporating the newly learned environment statistics into the target detection algorithm.

Our Approach

- Employ a **data-driven active drift detection** algorithm

sensing

- to detect changes of statistical characteristics of the environment.

- Apply **incremental learning** (i.e., learning under concept drift) algorithms

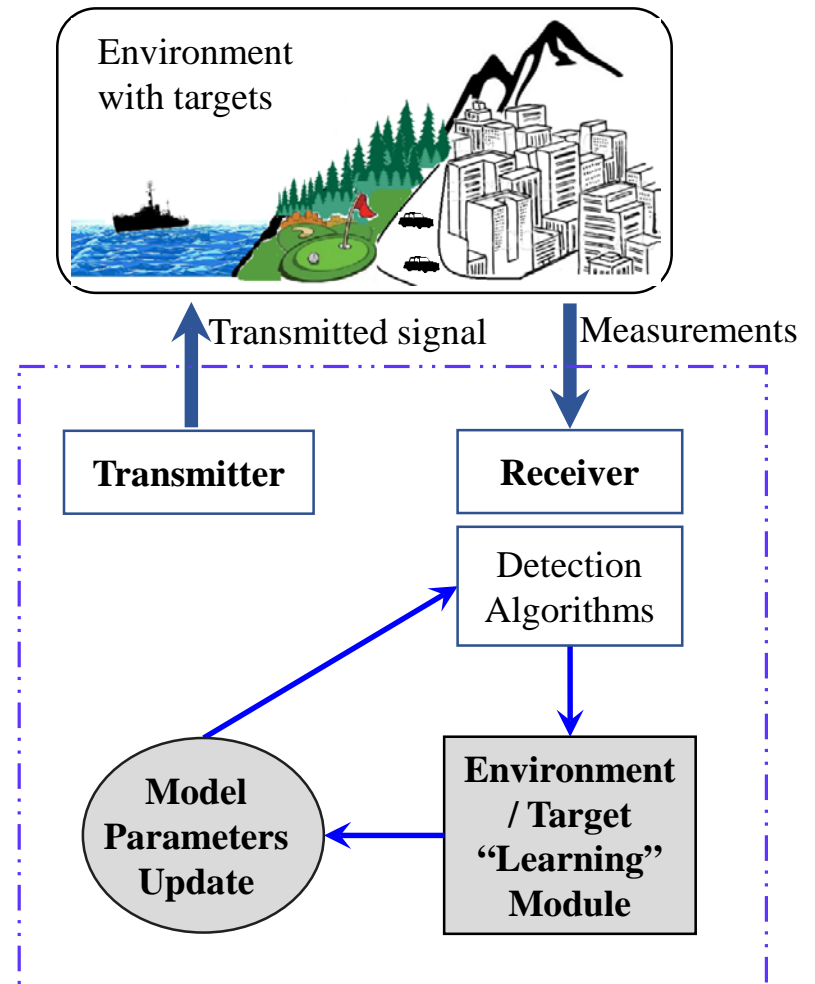
learning

- to learn the new statistical characteristics of the environment.

- Integrate the newly learned environment characteristics in the detection algorithm

adapting

- to adapt to the changes in the environment.



Relevance to DDDAS

- Our proposed technique with adaptive learning and cognitive augmentation is of high relevance
 - to remotely piloted radar systems
 - for substantially better intelligence, surveillance, and reconnaissance (ISR) capability
- It is also germane to the key science and technology frontiers of DDDAS:
 - Applications modeling →
 - Developing *data-driven* learning algorithms to detect any significant change in the underlying distribution of the model
 - Jointly combining newly measured data with the previously-stored calibration data to learn the environment model
 - Advances in Mathematical and Statistical Algorithms →
 - Incorporating learned model parameters into radar algorithms to provide robust and improved detection performance
 - Application Measurement Systems and Methods → *[on-going work, not part of this presentation]*
 - Synthesizing the next transmit waveforms based on the updated model parameters
 - Using the designed waveforms as *control-agents* to dynamically steer the next received measurements
 - Software Infrastructures and other systems software → *[future work, not part of this presentation]*
 - Addressing the near real-time implementation issues of the proposed signal processing algorithms.

Target Detection Method

Data-Driven Active Drift Detection

A typical change point detection problem:

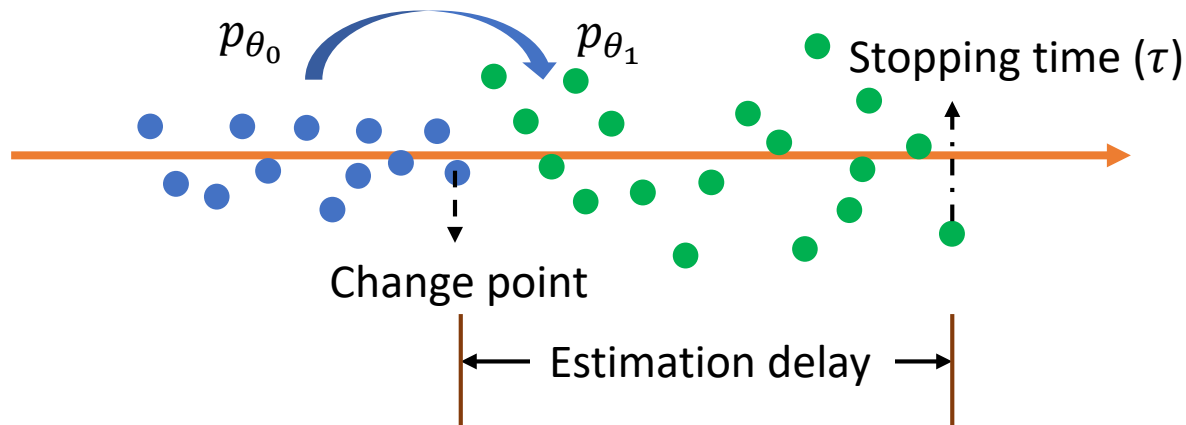
At current time N , decide from two hypotheses:

$$\mathcal{D}_0: \mathbf{y}_1, \mathbf{y}_2, \dots, \mathbf{y}_N \sim p_{\theta_0}$$

$$\mathcal{D}_1: \mathbf{y}_1, \mathbf{y}_2, \dots, \mathbf{y}_{k_0} \sim p_{\theta_0}, \mathbf{y}_{k_0+1}, \dots, \mathbf{y}_N \sim p_{\theta_1}$$

where

- \mathbf{y}_n : observed data at time n ;
- k_0 : change point;
- $p_{\theta_0}, p_{\theta_1}$: two different distributions before and after the change point.



Data-Driven Active Drift Detection (cont.)

Change point detection formulation for radar detection problem:

$$\tau = \operatorname{argmin}_{\tau} \sup_{n \geq 1} \operatorname{ess\,sup} E_n[(\tau - n)^+ | \mathcal{Y}_0^c, \dots, \mathcal{Y}_{n-1}^c] \quad (1)$$

such that $E_{\infty}[\tau] \geq \alpha$

where

- $C_c, c \in \{0,1\}$: two classes representing the absence and presence of the target;
- $\mathcal{Y}_0 = \{\mathbf{y}_{0,t}, r_{0,t}\}, t = 1, \dots, T_0$: calibration data set for two classes,
 - $\mathbf{y}_{0,t}$: t_{th} radar measurement
 - $r_{0,t} = 0$ if $\mathbf{y}_{0,t} \in C_0$ and $r_{0,t} = 1$ if $\mathbf{y}_{0,t} \in C_1$
 - T_0 : number of measurements in the calibration data;
- \mathcal{Y}_n^c : radar data observed at measurement time n from class c ;
- τ : stopping time;
- $(x)^+ = \max(0, x)$;
- $E_n[\cdot]$: expectation with respect to p_n^c ,
 - p_n^c : probability distribution when the change occurs at n ;
- $E_{\infty}[\tau]$: mean time between false alarms, assuming that change never happens;
- $\operatorname{ess\,sup}$: essential supremum of a set of random variables \mathcal{X} ; it is a random variable Z such that (i) $P(Z \geq X) = 1 \forall X \in \mathcal{X}$; and (ii) $P(Y \geq X) = 1, \forall X \in \mathcal{X} \rightarrow P(Y \geq Z) = 1, \forall X \in \mathcal{X}$.

Data-Driven Active Drift Detection (cont.)

CUmulative SUM (CUSUM) algorithm:

- provides the optimum stopping time τ for the problem in (1)

$$\tau = \inf \left\{ n \geq 1 : \left(g(\mathcal{Y}_0^c, \dots, \mathcal{Y}_n^c) = R_n - \min_{1 \leq k \leq n} R_k \right) \geq b \right\}$$

where

- $R_k = \sum_{i=1}^k \ln \frac{p_{\theta_1^c}(\mathcal{Y}_i^c)}{p_{\theta_0^c}(\mathcal{Y}_i^c)}$
- n : batch index
- b : a predefined threshold

Parameter training procedure:

- Find an estimate of θ_0^c using
 - calibration data \mathcal{Y}_0^c , $c \in \{0, 1\}$
 - knowledge of the parametric distribution underlying the data
- Compute the confidence intervals for θ_0^c
- Assign the confidence interval extremas to θ_1^c
- Assign $b = \max_{1 \leq t \leq T_0} g(\mathcal{Y}_0^c)$, where $\mathcal{Y}_0^c = \mathbf{y}_{0,t} | r_{0,t} = c$, $t = 1, \dots, T_0$

Data-Driven Active Drift Detection (cont.)

Extended CUSUM algorithm:

– when no prior knowledge is available about the distribution of \mathcal{Y}_n^c , $c \in \{0, 1\}$

- Convert measurements into new samples (take \mathcal{Y}_0^c as an example):

Convert

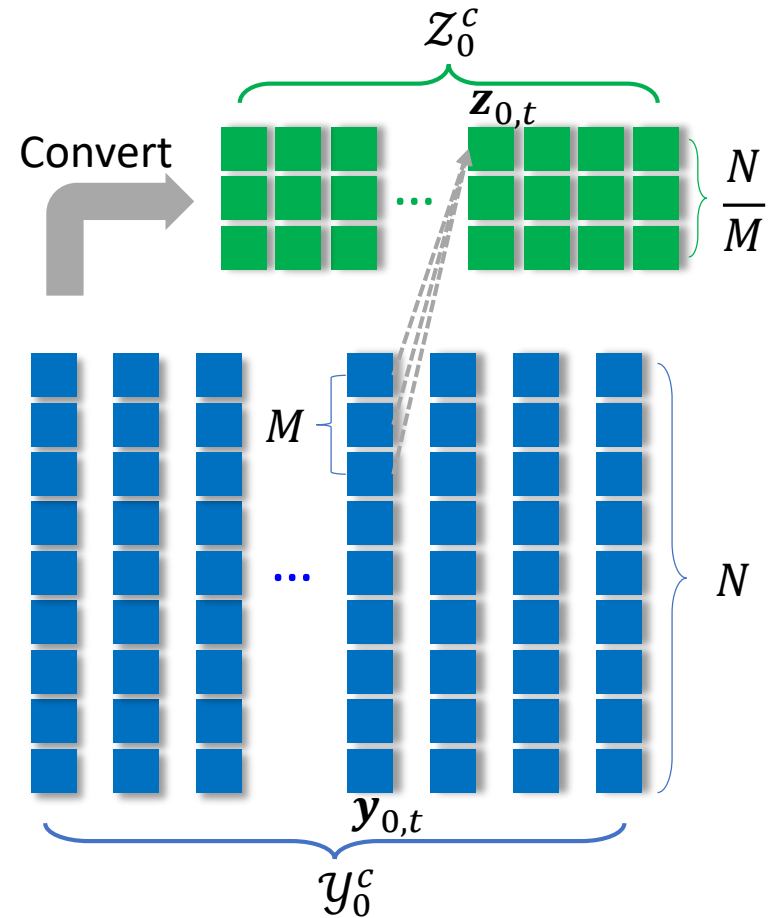
$$\mathcal{Y}_0^c = \{\mathbf{y}_{0,t} | r_t = c\}$$

$$z_{0,t,i} = \frac{1}{M} \sum_{v=(i-1)M+1}^{iM} y_{0,t,v}$$

$$\mathbf{z}_{0,t} = [z_{0,t,1}, \dots, z_{0,t,N/M}]^T$$

$$\mathcal{Z}_0^c = \{\mathbf{z}_{0,t} | r_t = c\}$$

where $y_{0,t,v}$ and $z_{0,t,i}$ are v_{th} and i_{th} entries of vectors $\mathbf{y}_{0,t}$ and $\mathbf{z}_{0,t}$, respectively.



Data-Driven Active Drift Detection (cont.)

Extended CUSUM algorithm (cont.):

- Use new samples to employ CUSUM algorithm:

$$\tau = \inf \left\{ n \geq 1 : \left(g(\mathcal{Z}_0^c, \dots, \mathcal{Z}_n^c) = R_n - \min_{1 \leq k \leq n} R_k \right) \geq b \right\}$$

where

- $R_k = \sum_{i=1}^k \ln \frac{p_{\theta_1^c}(\mathcal{Z}_i^c)}{p_{\theta_0^c}(\mathcal{Z}_i^c)}$
- n is the batch index
- b is a predefined threshold

Parameter training procedure:

- Find an estimate of θ_0^c using the calibration data \mathcal{Z}_0^c , $c \in \{0, 1\}$
- Compute the confidence intervals for θ_0^c
- Assign the confidence interval extremas to θ_1^c
- Assign $b = \max_{1 \leq t \leq T_0} g(\mathcal{Z}_0^c)$, where $\mathcal{Z}_0^c = \mathbf{z}_{0,t} | r_{0,t} = c$, $t = 1, \dots, T_0$

Numerical Results

Simulation Setup

Assumptions:

- Radar collects measurements
 - from multiple range cells (indexed by j)
 - over a sequence of coherent processing intervals (CPIs) (indexed by k)
- Radar receives and processes N temporal samples in each CPI
- Target is assumed to be present in the $j = 1$ range cell
- Target remains in a cell during the entire processing of $k = 1, 2, \dots, K$ CPIs
- Target response is considered to be known and constant (denoted as a)

Detection problem (of j_{th} range cell at k_{th} CPI):

$$\begin{cases} \mathcal{H}_0: \mathbf{y}_k^{(j)} = \mathbf{n}_k^{(j)} \\ \mathcal{H}_1: \mathbf{y}_k^{(j)} = a\mathbf{1} + \mathbf{n}_k^{(j)} \end{cases}, \quad \text{for } k = 1, 2, \dots, K, \quad j = 0, 1, 2, \dots,$$

where each vector is of dimension $N \times 1$.

Nonstationary modeling:

- For $k = 1, 2, \dots, k_0$, we have $\mathbf{n}_k^{(j)} \sim p_{n, \theta_0}$, i.e., $\mathbf{y}_k^{(j)} \sim p_{\theta_0^c}$
- For $k = k_0 + 1, \dots, K$, we have $\mathbf{n}_k^{(j)} \sim p_{n, \theta_1}$, i.e., $\mathbf{y}_k^{(j)} \sim p_{\theta_1^c}$

Simulation Setup (cont.)

Parameter training procedure:

Suppose we have T_0^c training data for class c , i.e., $\mathcal{Y}_0^c = \{\mathbf{y}_{0,t}^c\}$ for $t = 1, \dots, T_0^c$.

- If the **noise before change point is known** as $\mathbf{n}_k^{(j)} \sim \mathcal{N}(0, \sigma^2 \mathbf{I})$, then

1. $\theta_0^1 = [a, \sigma^2]$, $\theta_0^0 = [0, \sigma^2]$

2. Compute sample mean $\hat{\mu}^c$ and sample variance \hat{s}^{2c}

$$\hat{\mu}^c = \frac{1}{T_0^c N} \sum_{t=1}^{T_0^c} \mathbf{1}^T \mathbf{y}_{0,t}^c \quad \hat{s}^{2c} = \frac{1}{T_0^c N - 1} \sum_{t=1}^{T_0^c} (\mathbf{y}_{0,t}^c - \hat{\mu}^c \mathbf{1})^T (\mathbf{y}_{0,t}^c - \hat{\mu}^c \mathbf{1})$$

3. Take the lower/upper limits on the 95% confidence intervals of mean and variance

$$a_{ll}^c = \hat{\mu}^c - 1.96 \frac{\sigma}{\sqrt{T_0^c N}}$$

$$a_{ul}^c = \hat{\mu}^c + 1.96 \frac{\sigma}{\sqrt{T_0^c N}}$$

$$\sigma_{ll}^{2c} = \frac{(T_0^c N - 1) \hat{s}^{2c}}{\chi_{T_0^c N - 1}^2(\alpha/2)}$$

$$\sigma_{ul}^{2c} = \frac{(T_0^c N - 1) \hat{s}^{2c}}{\chi_{T_0^c N - 1}^2(1 - \alpha/2)}$$

where $\alpha = 0.05$

4. Evaluate $g_n = R_n - \min_{1 \leq k \leq n} R_k$, with $R_k = \sum_{t=1}^k \ln \frac{p_{\theta_1^c}(\mathbf{y}_{0,t}^c)}{p_{\theta_0^c}(\mathbf{y}_{0,t}^c)}$ having parameters

from θ_0^c to either $\theta_1^c = [a_{ll}^c, \sigma_{ll}^{2c}]$, $\theta_1^c = [a_{ul}^c, \sigma_{ul}^{2c}]$, $\theta_1^c = [a_{ul}^c, \sigma_{ll}^{2c}]$, or $\theta_1^c = [a_{ll}^c, \sigma_{ul}^{2c}]$

5. Let $b = \max_{1 \leq n \leq T_0^c} g_n$

Simulation Setup (cont.)

Parameter training procedure (cont.):

- If the noise $\mathbf{n}_k^{(j)}$ distribution is unknown, then the conversion for the extended CUSUM algorithm is used:
 - $\theta_0^c = [\hat{\mu}_z^c, \hat{s}_z^{2c}]$, where $\hat{\mu}_z^c$ and \hat{s}_z^{2c} are sample mean and variance of $\mathcal{Z}_0^c = \{\mathbf{z}_{0,t}^c\}$ (training data after the conversion) under \mathcal{H}_c
 - θ_1^c and b can be trained similar to the above.

Change Point Detection:

Once θ_0^c , θ_1^c , and b are obtained, then CUSUM (or extended CUSUM) algorithm is used to detect the change point.

Adaptive Target Detection:

Once a change in the clutter distribution is detected, the proposed radar accordingly modifies the log-likelihood ratio

$$\underbrace{\ln \left[\frac{p_{\theta_0^c}(\mathbf{y}_k^{(j)} | \mathcal{H}_1)}{p_{\theta_0^c}(\mathbf{y}_k^{(j)} | \mathcal{H}_0)} \right]}_{\text{before change point}} \quad \rightarrow \quad \underbrace{\ln \left[\frac{p_{\theta_1^c}(\mathbf{y}_k^{(j)} | \mathcal{H}_1)}{p_{\theta_1^c}(\mathbf{y}_k^{(j)} | \mathcal{H}_0)} \right]}_{\text{after change point}}$$

Simulation Setup (cont.)

We consider four clutter distributions:

- Gaussian distribution
- Student-t distribution
- K distribution
- Weibull distribution

Based on the proposed framework, 12 cases are included in the simulation results for target detection under nonstationary clutter as follows:

TABLE I: Distributions of Clutter in Target Detection

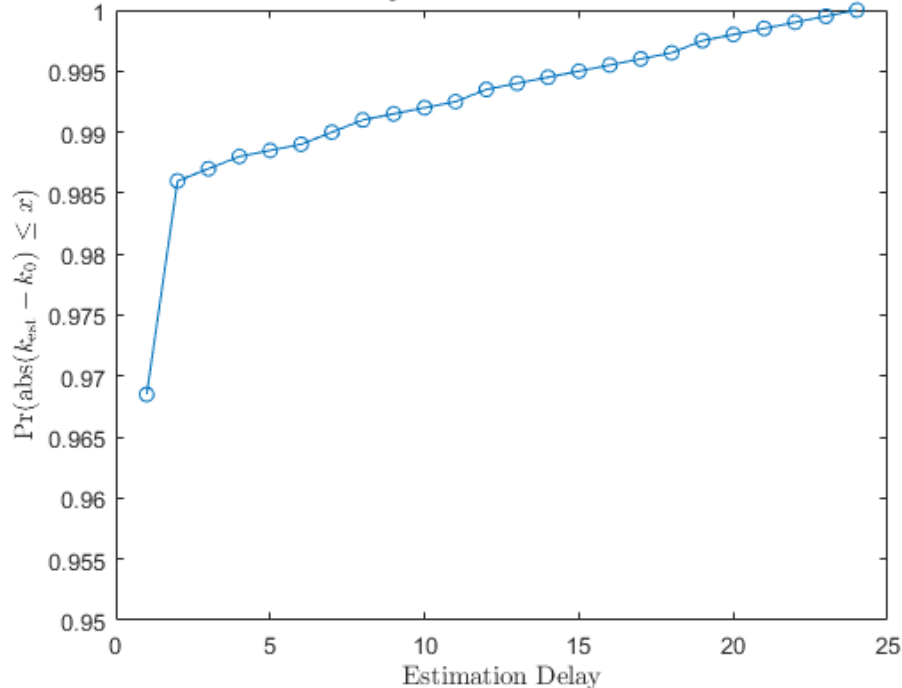
Before Change Point	After Change Point				
Gaussian		Student-t	K	Weibull	} CUSUM
Student-t	Gaussian		K	Weibull	
K	Gaussian	Student-t		Weibull	} Extended CUSUM
Weibull	Gaussian	Student-t	K		

We present the results in terms of the (i) [change point estimation delay](#) and (ii) [adaptive detection performance](#).

Numerical Results

Gaussian \rightarrow Student-t

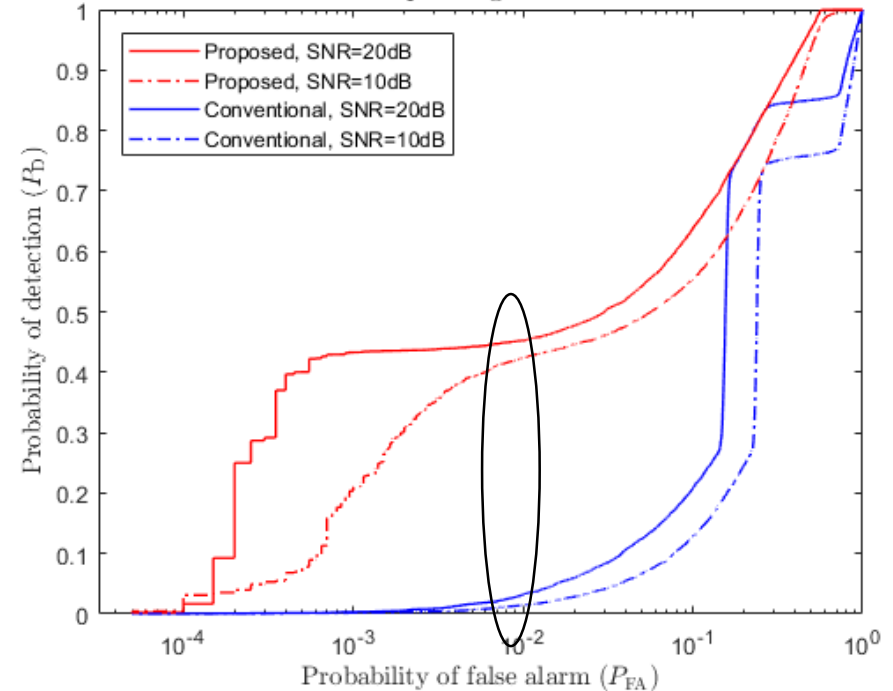
Estimation Delay Cumulative Distribution Function



Change point detection (CUSUM)

- **Observation:** Change in clutter distribution is detected within **one processing interval** for **more than 96.5%** of the time

Receiver operating characteristics

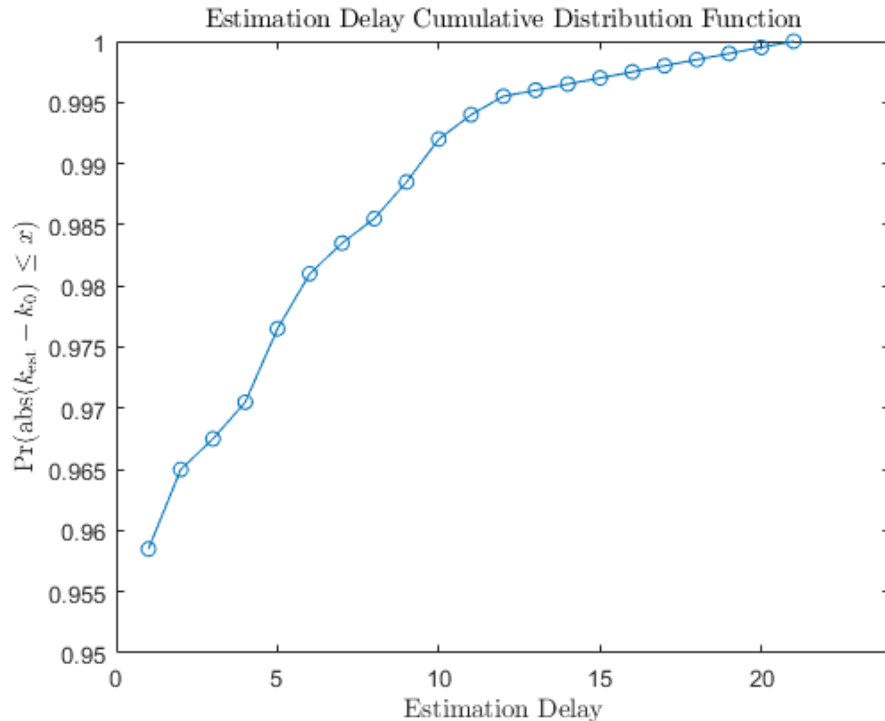


ROC curves (10dB and 20dB)

- **Observation:** Detection performance **improves substantially** (P_D increased by ≈ 0.4) due to the incorporation of the modified clutter characteristics

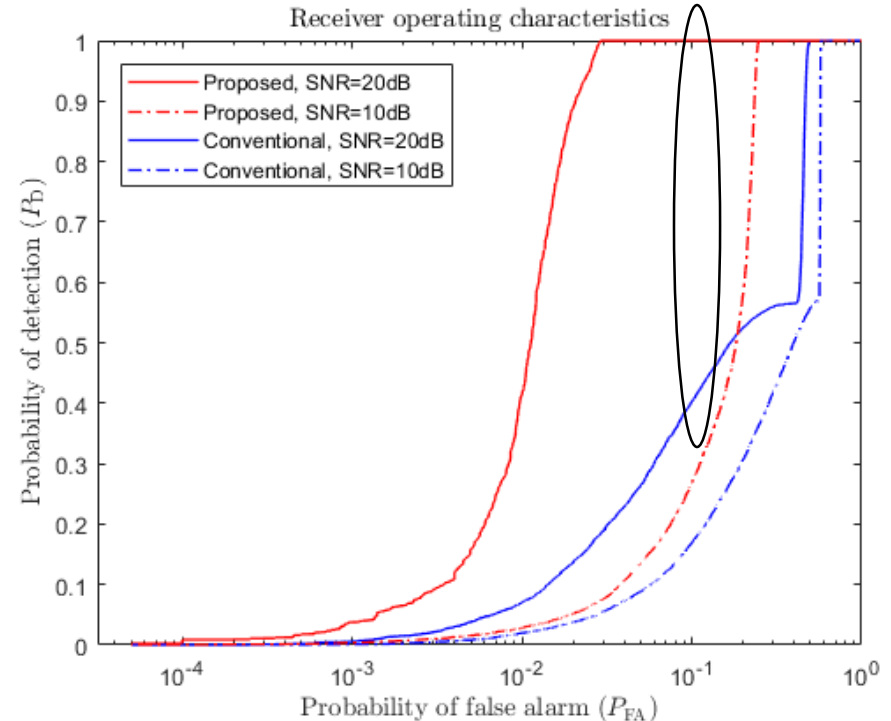
Numerical Results (cont.)

Gaussian \rightarrow K



Change point detection (CUSUM)

- **Observation:** Change in clutter distribution is detected within **one processing interval** for **more than 95.5%** of the time

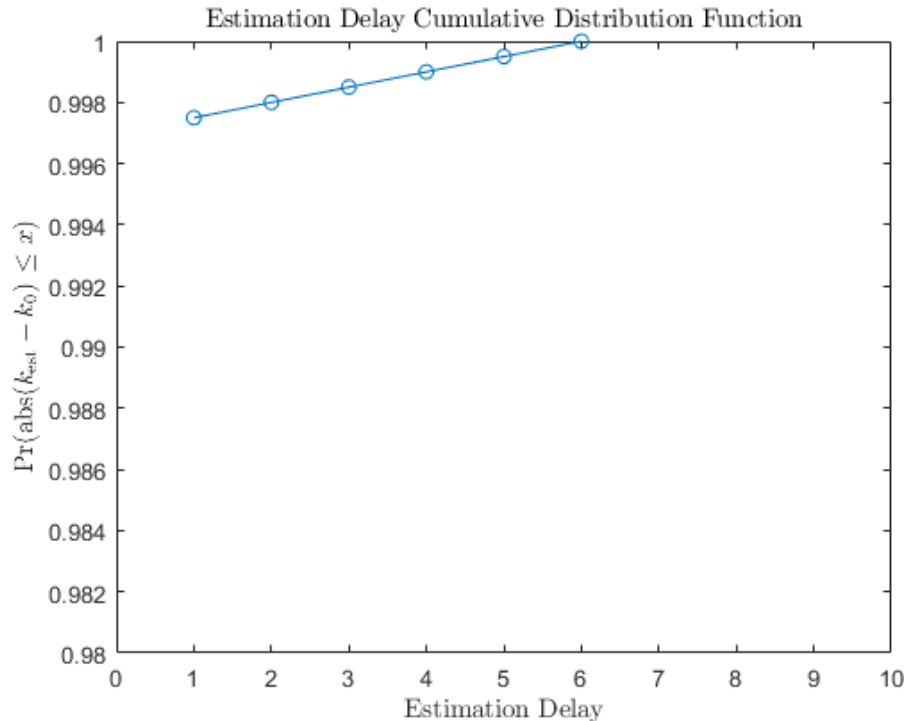


ROC curves (10dB and 20dB)

- **Observation:** Detection performance **improves substantially** (P_D increased by > 0.5) due to the incorporation of the modified clutter characteristics

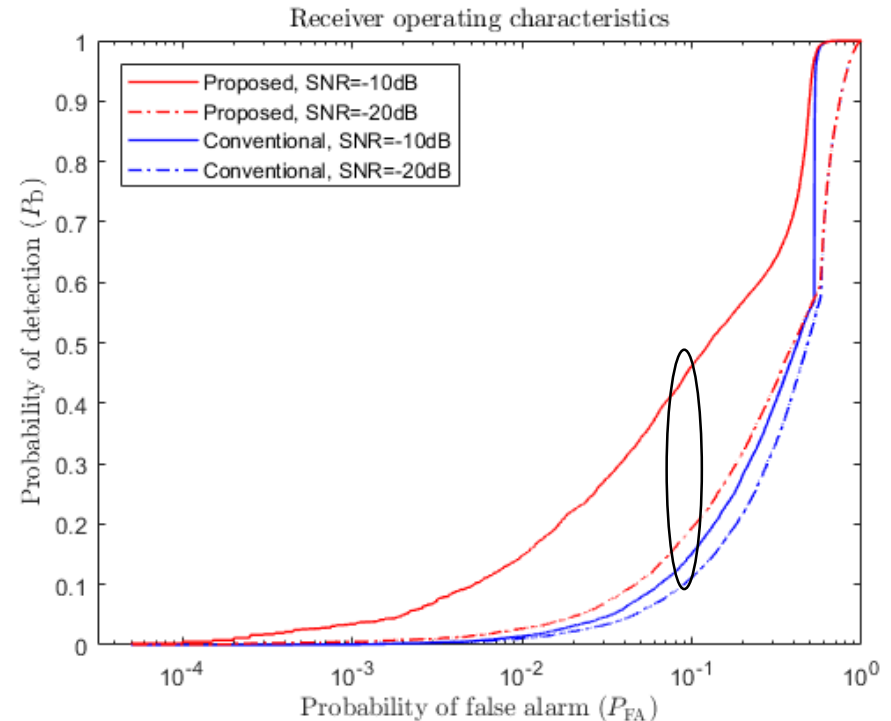
Numerical Results (cont.)

Weibull \rightarrow K



Change point detection (extended CUSUM)

- **Observation:** Change in clutter distribution is detected within **one processing interval** for **more than 99.6%** of the time



ROC curves (-10dB and -20dB)

- **Observation:** Detection performance **improves substantially** (P_D increased by ≈ 0.4) due to the incorporation of the modified clutter characteristics

Numerical Results (cont.)

Change Point Detection Performance Summary:

Clutter before change point	Clutter after change point	Probability of change detection in one step delay	Estimation delay when probability of change detection $\geq 99\%$
Gaussian (G)	T	96.85%	7
	K	95.85%	10
	W	97.10%	6
Student-t (T)	G	91.80%	2
	K	99.40%	1
	W	98.90%	2
K	G	98.90%	3
	T	98.60%	2
	W	93.05%	2
Weibull (W)	G	97.20%	14
	T	97.00%	2
	K	99.75%	1

Numerical Results (cont.)

Improved Detection Performance Summary:

Clutter before change point	Clutter after change point	Improved P_D when $P_{FA} = 0.01$	
		SNR= 10dB	SNR= 20dB
Gaussian (G)	T	40.9%	42.1%
	K	0.8%	34.4%
	W	1.6%	48.7%
		SNR= -10dB	SNR= -20dB
Student-t (T)	G	4.0%	24.8%
	K	56.0%	11.7%
	W	64.4%	2.5%
K	G	*	*
	T	*	*
	W	86.3%	27.4%
Weibull (W)	G	*	*
	T	*	*
	K	13.4%	1.6%

* No comparable data exist since the case likelihood ratio=0/0 arise too often in conventional radar.

Conclusions and Future Work

Conclusions and Future Work

Conclusions:

- We developed a **data-driven algorithm** to detect a target in the presence of nonstationary environment (clutter).
- Applied an **active drift learning technique** to detect and estimate any change-point (if present) in the clutter distribution.
- Employed the **incremental learning** and **drift detection** algorithms to incrementally learn the environment and update the system parameters on the fly.
- Demonstrated with numerical examples that the proposed algorithm
 - **quickly detects a change** in the underlying clutter distribution,
 - **significantly improves** the target **detection performance**.

Future Work:

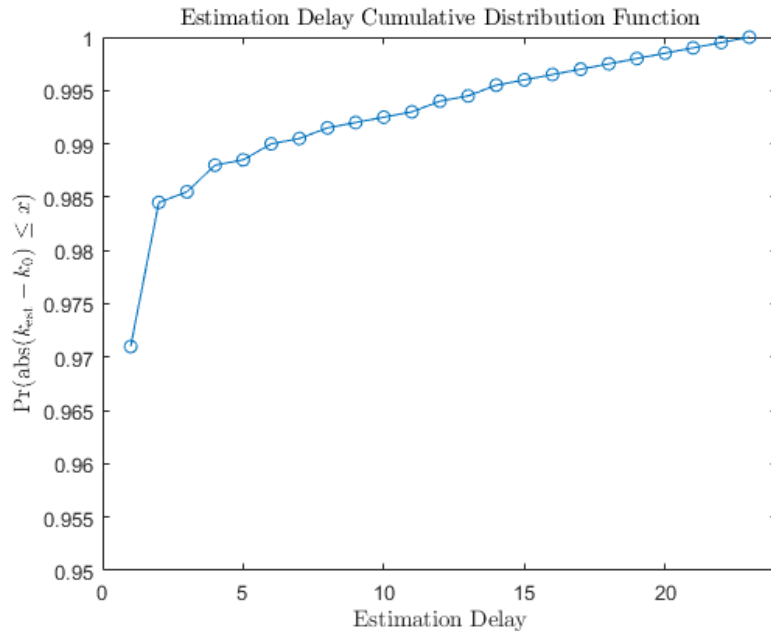
- Extend the model to include a Bayesian formulation of the change point parameter.
- Explore the active drift learning under noisy labels and passive drift learning methodologies.
- Validate the performance of our proposed technique with real data.
- Incorporate waveform design and other adaptive techniques to further improve the detection and tracking performance under nonstationary environment.

Thank you!

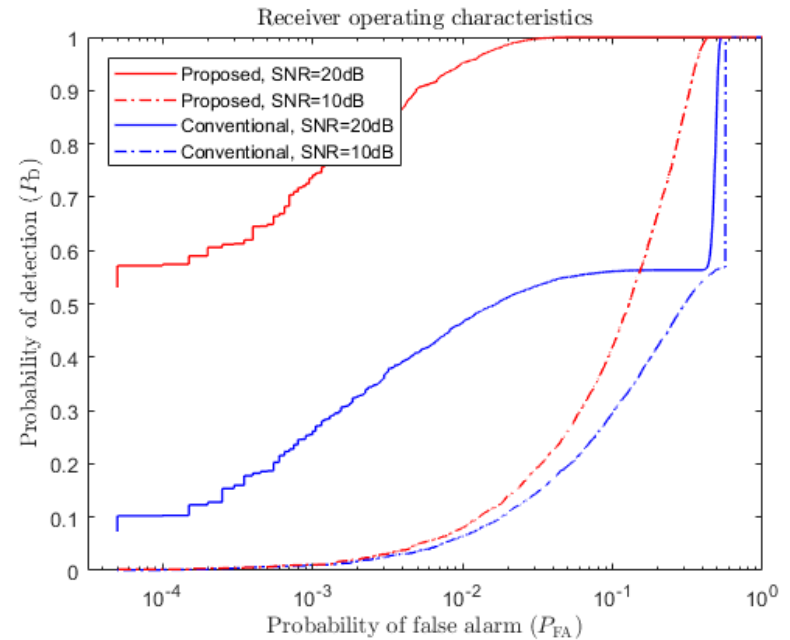
Appendix

More Numerical Results

Gaussian->Weibull



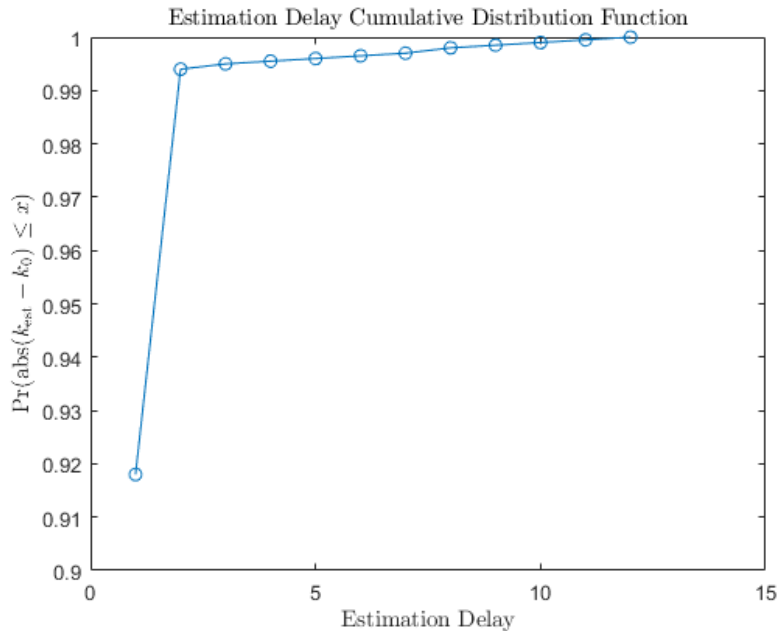
Change point detection (CUSUM)



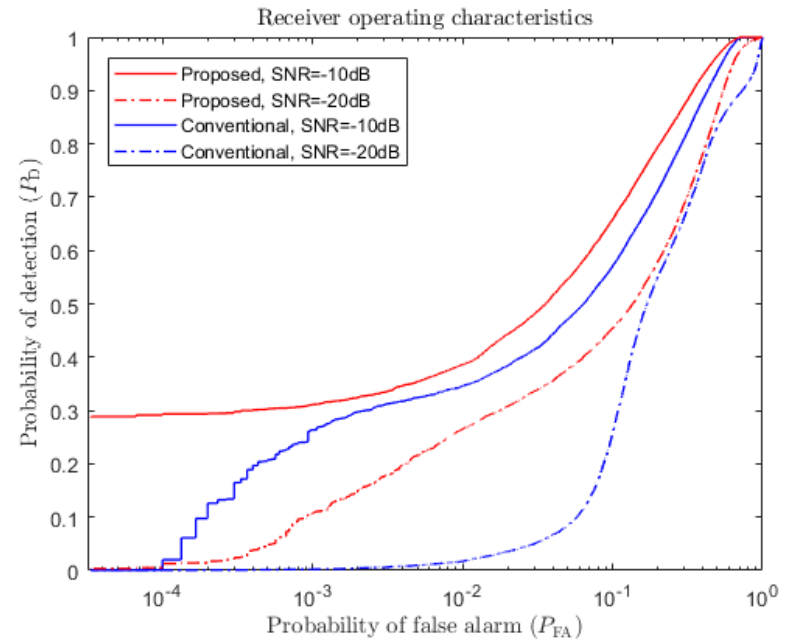
ROC curve (10dB and 20dB)

More Numerical Results

Student-t->Gaussian



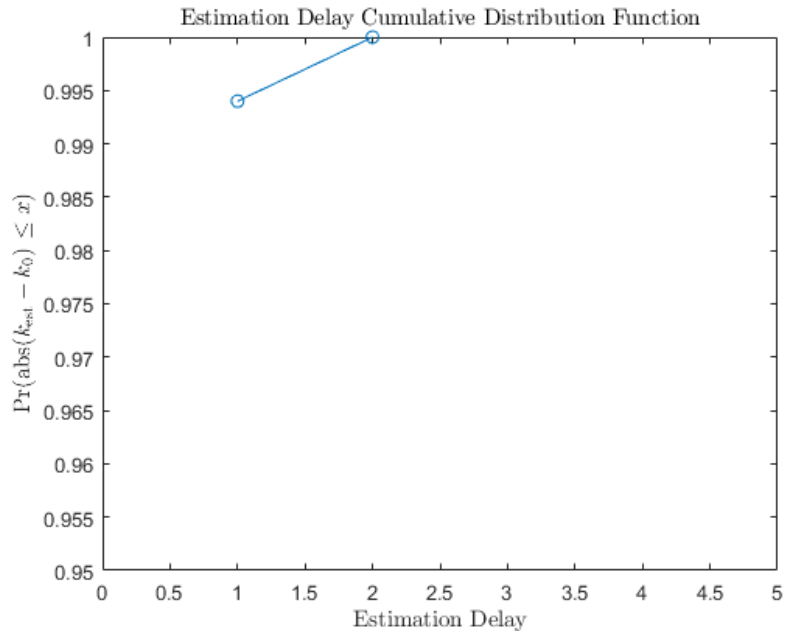
Change point detection (extended CUSUM)



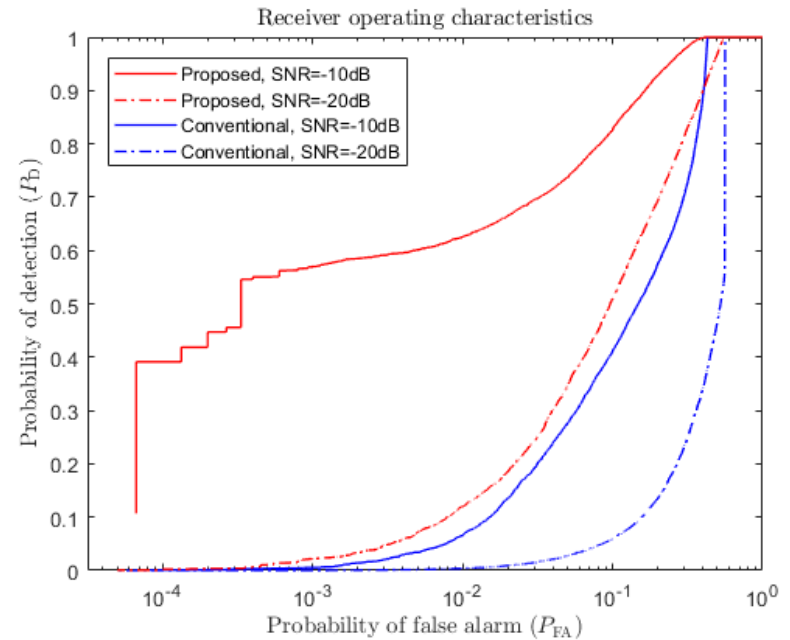
ROC curve (-10dB and -20dB)

More Numerical Results

Student-t- \rightarrow K



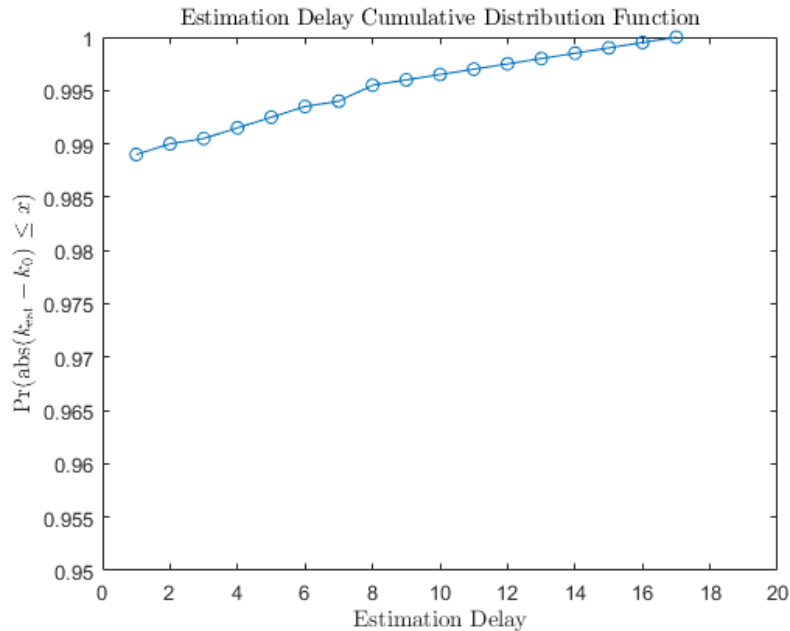
Change point detection (extended CUSUM)



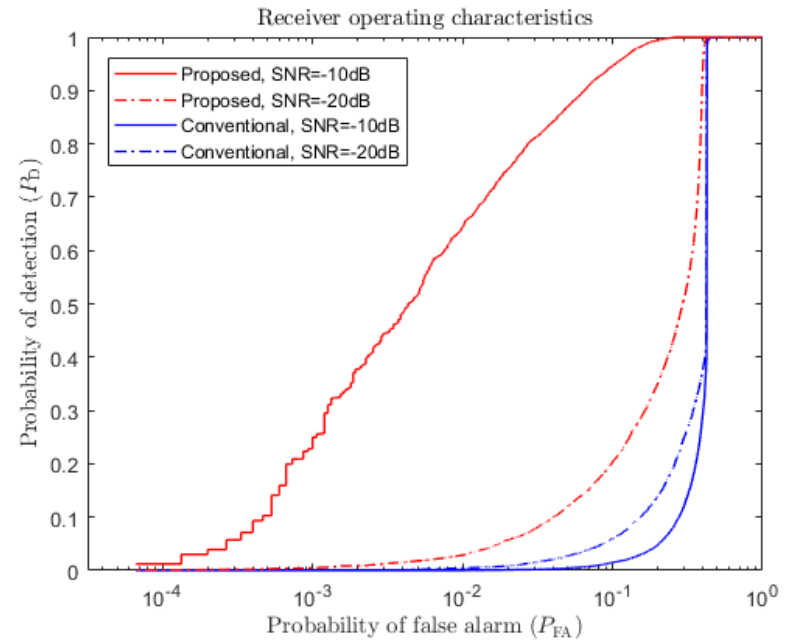
ROC curve (-10dB and -20dB)

More Numerical Results

Student-t- \rightarrow Weibull



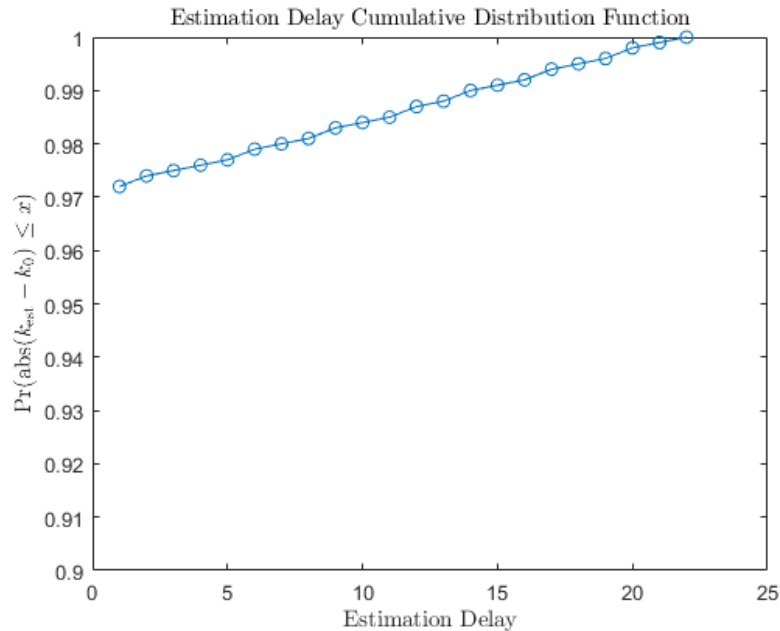
Change point detection (extended CUSUM)



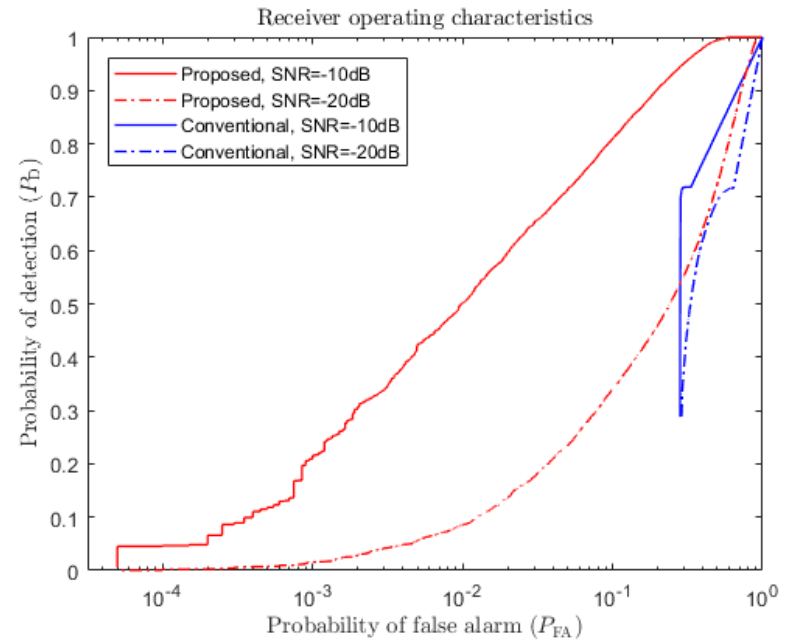
ROC curve (-10dB and -20dB)

More Numerical Results

Weibull->Gaussian



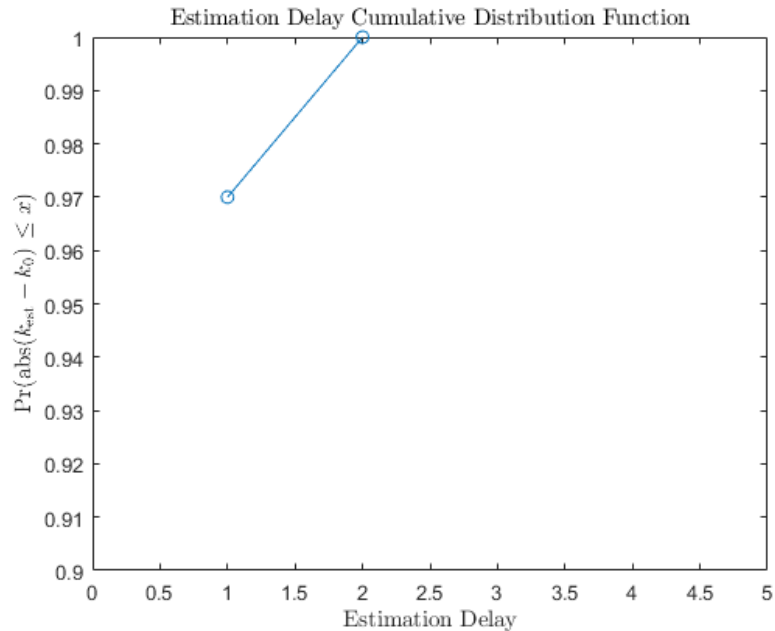
Change point detection (extended CUSUM)



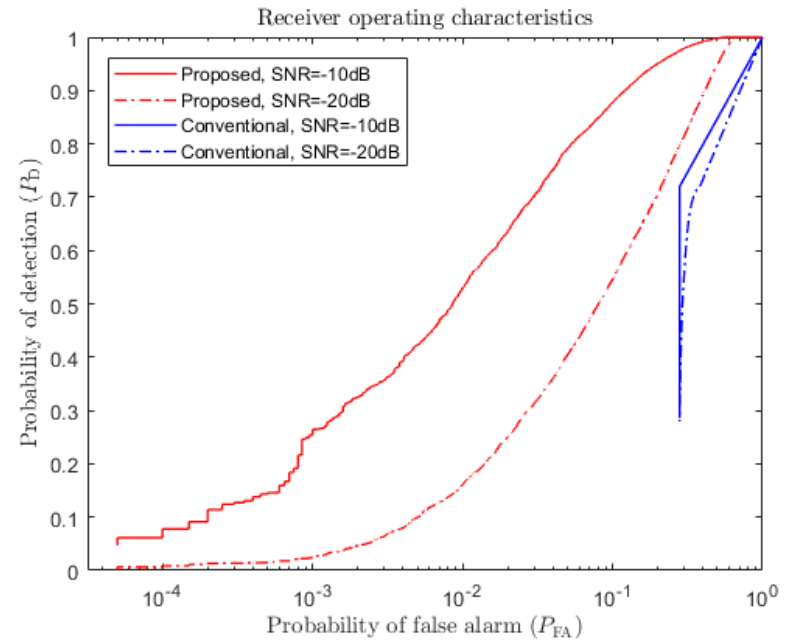
ROC curve (-10dB and -20dB)

More Numerical Results

Weibull->Student-t



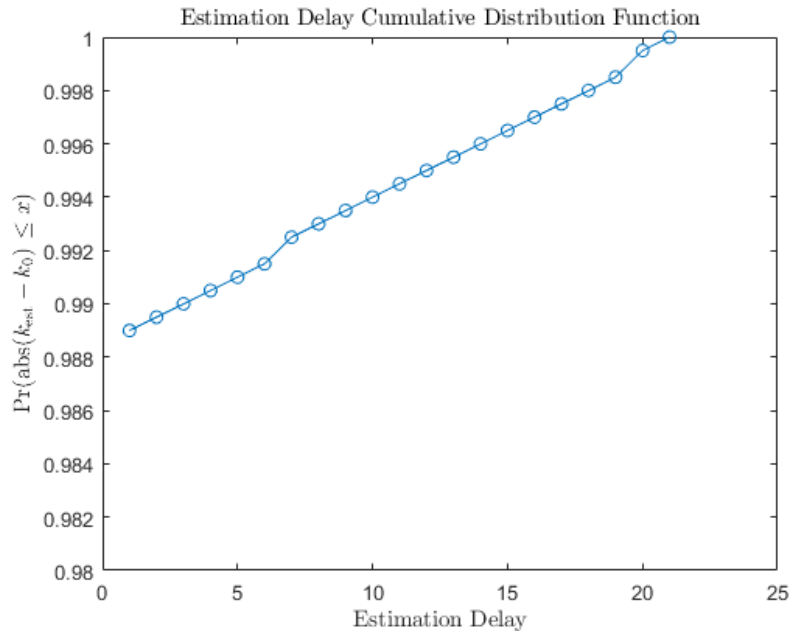
Change point detection (extended CUSUM)



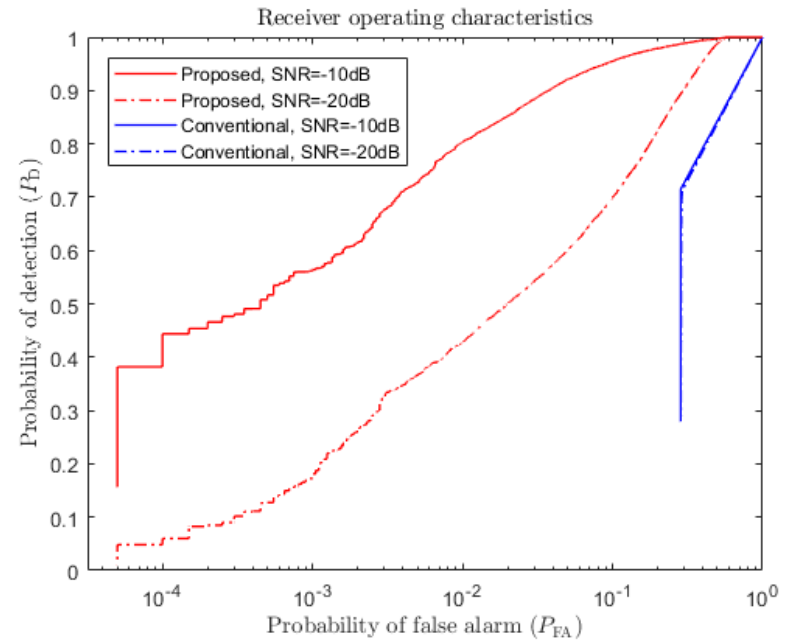
ROC curve (-10dB and -20dB)

More Numerical Results

K->Gaussian



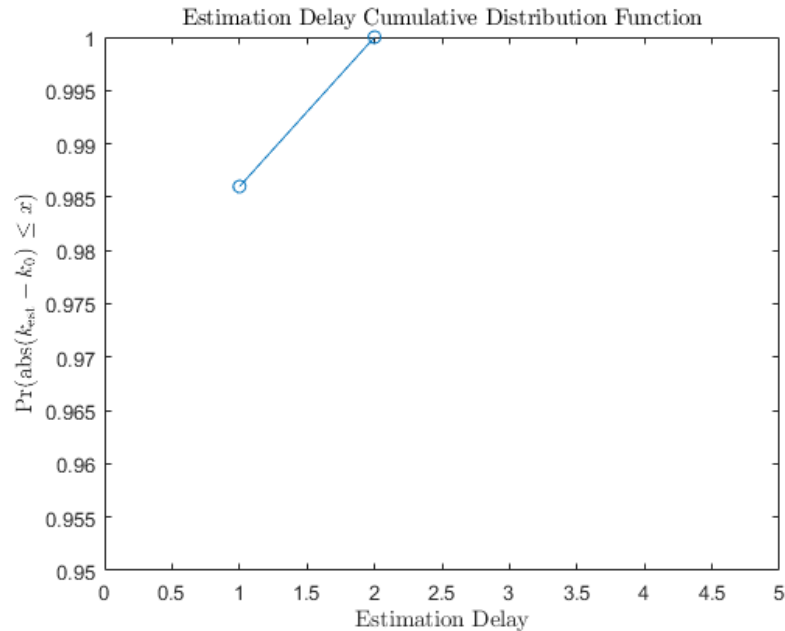
Change point detection (extended CUSUM)



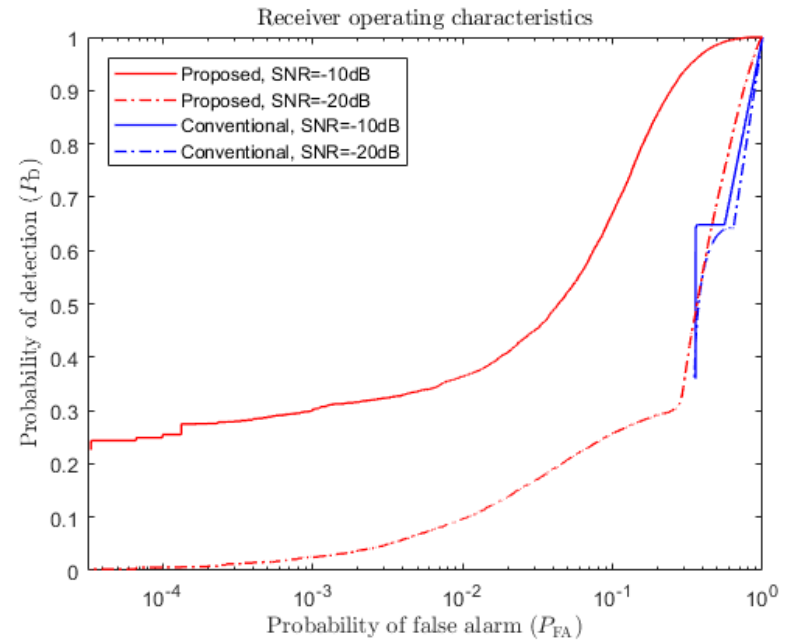
ROC curve (-10dB and -20dB)

More Numerical Results

K->Student-t



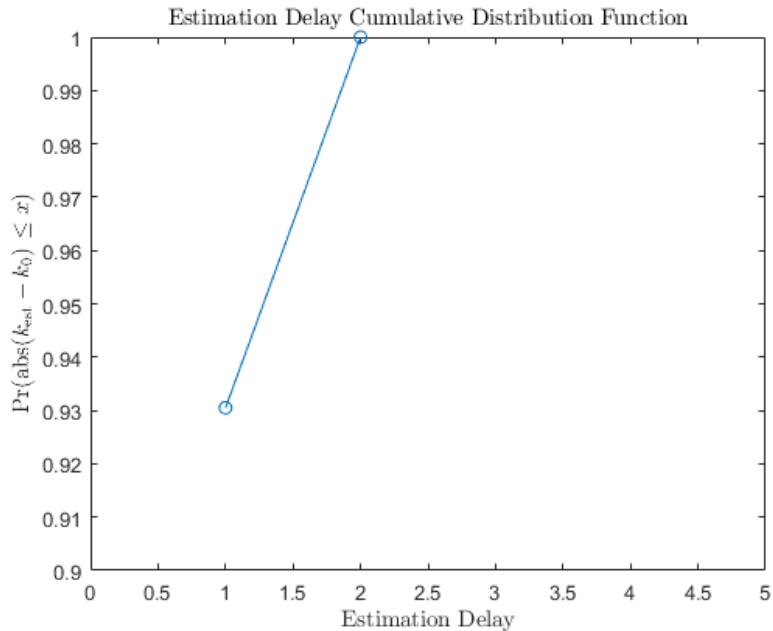
Change point detection (extended CUSUM)



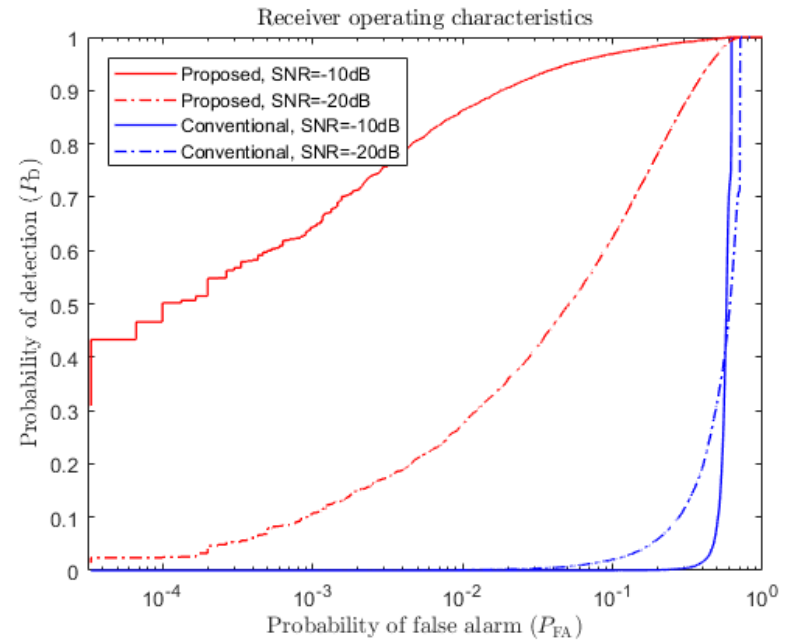
ROC curve (-10dB and -20dB)

More Numerical Results

K->Weibull



Change point detection (extended CUSUM)



ROC curve (-10dB and -20dB)

Numerical Results (cont.)

Improved Detection Performance Summary:

Clutter before change point	Clutter after change point	Improved P_D when $P_{FA} = 0.01$		Improved P_D when $P_{FA} = 0.001$	
		SNR=10dB	SNR=20dB	SNR=10dB	SNR=20dB
Gaussian (G)	T	40.9%	42.1%	20.8%	43.0%
	K	0.8%	34.4%	0.3%	3.2%
	W	1.6%	48.7%	0%	48%
		SNR=-10dB	SNR=-20dB	SNR=-10dB	SNR=-20dB
Student-t (T)	G	4.0%	24.8%	4.8%	10.6%
	K	56.0%	11.7%	56.5%	2.2%
	W	64.4%	2.5%	25.0%	0.5%
K	G	*	*	*	*
	T	*	*	*	*
	W	86.3%	27.4%	64.5%	10.1%
Weibull (W)	G	*	*	*	*
	T	*	*	*	*
	K	13.4%	1.6%	3.4%	0.4%

* No comparable data exist since the case likelihood ratio=0/0 arise too often in conventional radar.