Shared Memory and Distributed Multiprocessing

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Issue with Parallelism

- Parallel software is the problem
- Need to get significant performance improvement
  - Otherwise, just use a faster uniprocessor, since it's easier!
- Difficulties
  - Partitioning
  - Coordination
  - Communications overhead

Amdahl's Law

- Sequential part can limit speedup
- Example: 100 processors, 90× speedup?
  - $T_{new} = T_{parallelizable}/100 + T_{sequential}$
  - $$\text{Speedup} = \frac{1}{(1 - F_{\text{paralleliz able}}) + F_{\text{paralleliz able}}/100} = 90$$
  - Solving: $F_{parallelizable} = 0.999$
- Need sequential part to be 0.1% of original time

Scaling Example

- Workload: sum of 10 scalars, and 10 × 10 matrix sum
  - Speed up from 10 to 100 processors
- Single processor: Time = (10 + 100) × t_{add}
- 10 processors
  - Time = 10 × t_{add} + 100/10 × t_{add} = 20 × t_{add}
  - Speedup = 110/20 = 5.5 (55% of potential)
- 100 processors
  - Time = 10 × t_{add} + 100/100 × t_{add} = 11 × t_{add}
  - Speedup = 110/11 = 10 (10% of potential)
- Assumes load can be balanced across processors

Scaling Example (cont)

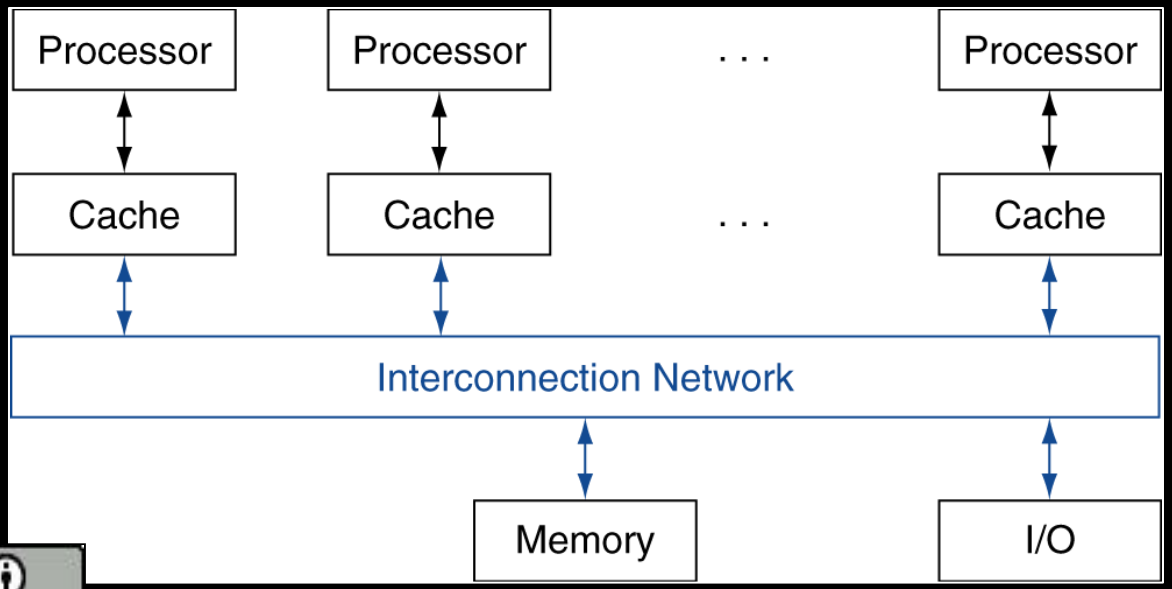
- What if matrix size is 100 × 100?
- Single processor: Time = (10 + 10000) × t_{add}
- 10 processors
  - Time = 10 × t_{add} + 10000/10 × t_{add} = 1010 × t_{add}
  - Speedup = 10010/1010 = 9.9 (99% of potential)
- 100 processors
  - Time = 10 × t_{add} + 10000/100 × t_{add} = 110 × t_{add}
  - Speedup = 10010/110 = 91 (91% of potential)
- Assuming load balanced

Strong vs Weak Scaling

- Strong scaling: problem size fixed
  - As in example
- Weak scaling: problem size proportional to number of processors
  - 10 processors, 10 × 10 matrix
    - Time = 20 × t_{add}
  - 100 processors, 32 × 32 matrix
    - Time = 10 × t_{add} + 1000/100 × t_{add} = 20 × t_{add}
  - Constant performance in this example

Shared Memory

- SMP: shared memory multiprocessor
  - Hardware provides single physical address space for all processors
  - Synchronize shared variables using locks
  - Memory access time
    - UMA (uniform) vs. NUMA (nonuniform)



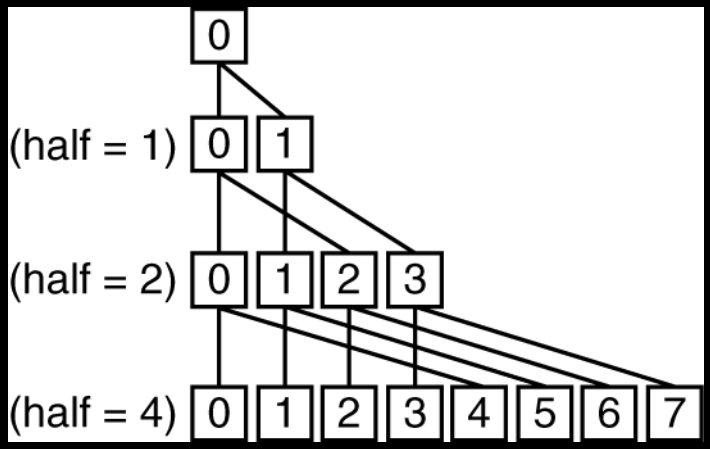
Example: Sum Reduction

- Sum 100,000 numbers on 100 processor UMA
  - Each processor has ID: 0 ≤ Pn ≤ 99
  - Partition 1000 numbers per processor
  - Initial summation on each processor

```
sum[Pn] = 0;
  for (i = 1000*Pn;
      i < 1000*(Pn+1); i = i + 1)
    sum[Pn] = sum[Pn] + A[i];
```

- Now need to add these partial sums
  - Reduction: divide and conquer
  - Half the processors add pairs, then quarter, …
  - Need to synchronize between reduction steps

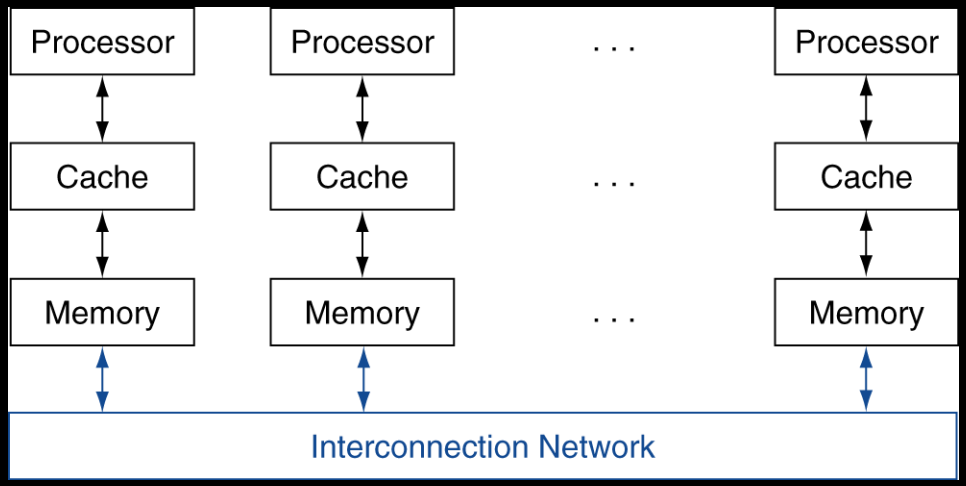
Example: Sum Reduction




```
half = 100;
repeat
  synch();
  if (half%2 != 0 && Pn == 0)
    sum[0] = sum[0] + sum[half-1];
    /* Conditional sum needed when half is odd;
       Processor0 gets missing element */
  half = half/2; /* dividing line on who sums */
  if (Pn < half) sum[Pn] = sum[Pn] + sum[Pn+half];
until (half == 1);
```

Message Passing

- Each processor has private physical address space
- Hardware sends/receives messages between processors



Loosely Coupled Clusters

- Network of independent computers
  - Each has private memory and OS
  - Connected using I/O system
    - E.g., Ethernet/switch, Internet
- Suitable for applications with independent tasks
  - Web servers, databases, simulations, …
- High availability, scalable, affordable
- Problems
  - Administration cost (prefer virtual machines)
  - Low interconnect bandwidth
    - c.f. processor/memory bandwidth on an SMP

Sum Reduction (Again)

- Sum 100,000 on 100 processors
- First distribute 1000 numbers to each
  - The do partial sums

```
sum = 0;
for (i = 0; i<1000; i = i + 1)
  sum = sum + AN[i];
```

- Reduction
  - Half the processors send, other half receive and add
  - The quarter send, quarter receive and add, …

Sum Reduction (Again)

- Given send() and receive() operations

```
limit = 100; half = 100;/* 100 processors */
repeat
  half = (half+1)/2; /* send vs. receive
                        dividing line */
  if (Pn >= half && Pn < limit)
    send(Pn - half, sum);
  if (Pn < (limit/2))
    sum = sum + receive();
  limit = half; /* upper limit of senders */
until (half == 1); /* exit with final sum */
```

  - Send/receive also provide synchronization
  - Assumes send/receive take similar time to addition

Cache Coherence Problem

- Suppose two CPU cores share a physical address space
  - Write-through caches

Time step	Event	CPU A's cache	CPU B's cache	Memory
0				0
1	CPU A reads X	0		0
2	CPU B reads X	0	0	0
3	CPU A writes 1 to X	1	0	1

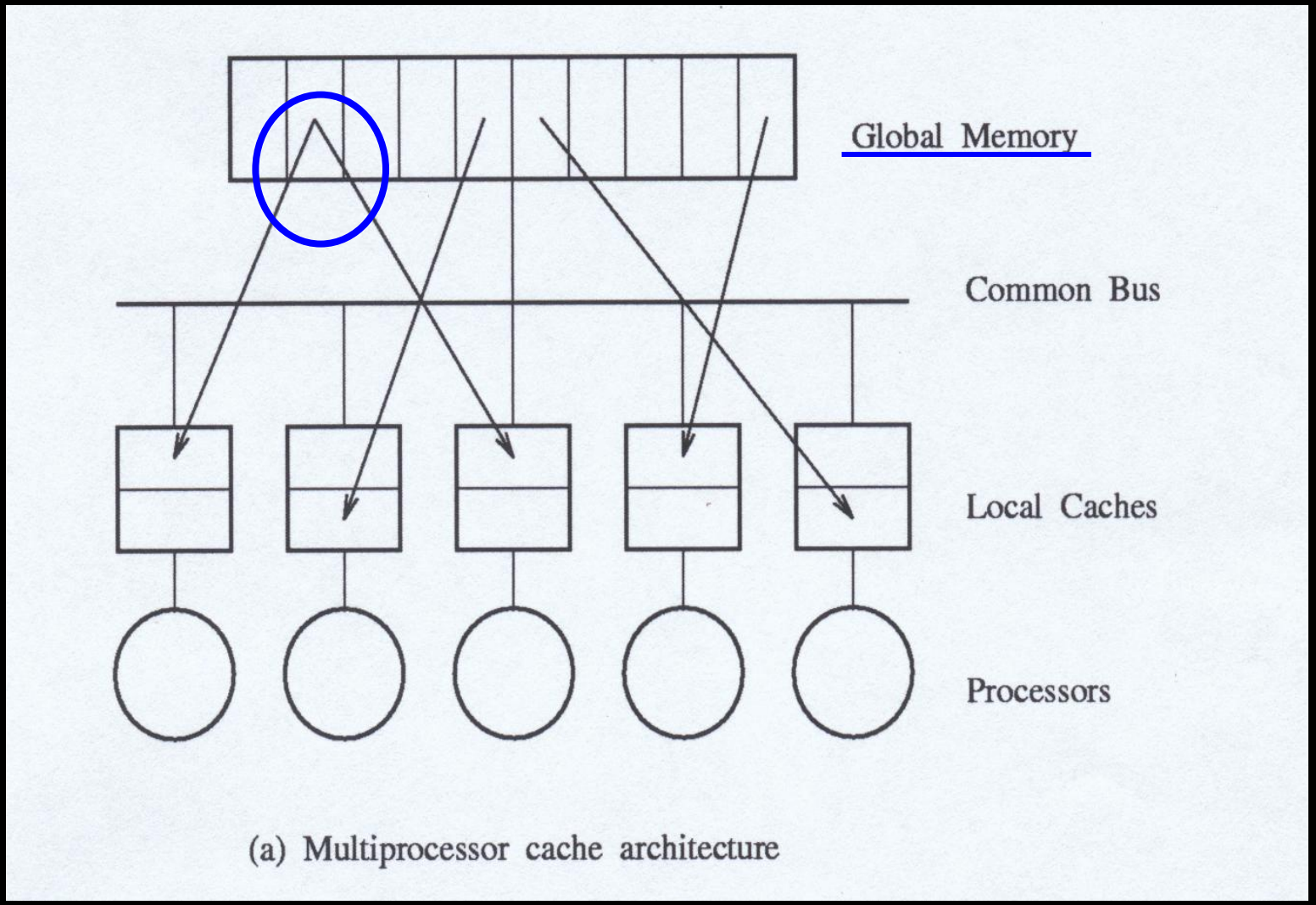
Coherence Defined

- Informally: Reads return most recently written value
- Formally:
  - P writes X; P reads X (no intervening writes)
    $\Rightarrow$ read returns written value
  - P_1 writes X; P_2 reads X (sufficiently later)
    $\Rightarrow$ read returns written value
    - c.f. CPU B reading X after step 3 in example
  - P_1 writes X, P_2 writes X
    $\Rightarrow$ all processors see writes in the same order
    - End up with the same final value for X

Memory Consistency

- When are writes seen by other processors
  - "Seen" means a read returns the written value
  - Can't be instantaneously
- Assumptions
  - A write completes only when all processors have seen it
  - A processor does not reorder writes with other accesses
- Consequence
  - P writes X then writes Y
    $\Rightarrow$ all processors that see new Y also see new X
  - Processors can reorder reads, but not writes

Multiprocessor Caches



(a) Multiprocessor cache architecture

Multiprocessor Caches

- Caches provide [for shared items]
  - Migration
  - Replication
- Migration Reduces
  - Latency
  - Bandwidth demands
- Replication reduces
  - Latency
  - Contention for a read of shared item