

Matrix and Tensor Factorization for Profiling Player Behavior

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Preface

Matrix and tensor factorization models are scalable and flexible tools for learning efficient representations for a variety of descriptive, predictive and prescriptive analytics tasks. They can be easily deployed without requiring high-performance computing environments and extensive parameter tuning for analyzing large scale and high dimensional behavioral data to come up with interpretable and actionable results. Their range of applications includes recommender systems, behavior prediction, natural language processing, digital forensics, process and budget optimization and behavioral profiling.

In this compact book, we will introduce certain theoretical as well as practical aspects behind a set of matrix and tensor factorization models for behavioral profiling. We will particularly concentrate on the various straightforward-to-implement algorithms used to come up with useful factorizations, ideas to enforce interpretability for human analysts and example behavioral profiling case studies with a behavioral dataset from a digital game. The methods we cover in detail for profiling behavior include unconstrained matrix factorization, Singular Value Decomposition, k -Means clustering, Archetypal Analysis, Simplex Volume Maximization and k -Maxoids Analysis for analyzing bipartite (rectangular) matrices and two- and three-way DEDICOM for respectively decomposing structurally constrained asymmetric similarity matrices and tensors.

Although our main intention is about analyzing player behavior in digital games, the methods we introduced can easily be applied to analyze behavioral telemetry data from similar digital products (such as mobile and web applications) as well. Therefore, this book is

suitable for developers, analysts, data scientists and engineers, who are interested in tracking, collecting and analyzing behavioral telemetry data to better understand their user-base and automatically learn informative features for a variety of analytics applications.

This work will be based on my recent research on Game Analytics and mainly the second chapter of my PhD thesis [1] with additional content from the first, third, seventh and eighth chapters about the applications. The set of peer-reviewed publications that will mainly accompany this work are from [2–19]. Furthermore, I have published over 40 peer-reviewed papers in the broad area of data science covering purely theoretical as well as application-oriented work in behavioral analytics, psychometrics, text mining and quantum computing. The complete list of my publications can be found on my website <https://sites.google.com/view/rafetsifa>.

Notations

I mostly kept a fixed notation for the equations in this work. Lowercase bold letters symbolize vectors (e.g. \mathbf{v}), uppercase bold letters are for matrices (e.g. \mathbf{V}) and Chancery font capital letters will stand for tensors (collections of matrices) (e.g. \mathcal{S}). Capital letters with calligraphic font will represent mathematical sets (e.g. \mathcal{S}) and $|\cdot|$ will represent the set cardinality. Unless stated otherwise, I will be using the column vector notation to specify vectors and the superscript T (e.g. \mathbf{A}^T) will be used to represent the transpose of matrices and vectors. I will be mostly using subscripts to index rows, columns and individual elements in vectors, matrices and tensors. For instance, a_i will be the i th element of the vector \mathbf{a} , the scalar b_{ij} will be indicating the element in the i th row and the j th column of a matrix \mathbf{B} and c_{ijk} will be pointing to the i th row and the j th column of the k th slice of a tensor \mathcal{C} . Additionally \mathbf{d}_i and \mathbf{d}_j will be respectively symbolizing the i th column and the j th row of matrix \mathbf{D} . Similarly, \mathbf{E}_k will be referring to the k th slice of a tensor \mathcal{E} .

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I am also deeply thankful to my current and former colleagues in the Media Engineering department at Fraunhofer IAIS. I want to thank Ulrich Nütten, César Ojeda, Kostadin Cvejovski, Dr. Mirwaes Wahabzada, Eduardo Brito, Ben Wulff, Dr. Anna Ladi, Maren Pielka, Dr. Jannis Schücker and Rajkumar Ramamurthy for the amazing research atmosphere. Warm thanks go to Prof. Dr. Alessandro Canossa, Dr. Sam Devlin, Prof. Dr. Lennart Nacke, Prof. Dr. Tom Stafford, Marc Müller, Prof. Dr. Günter Wallner, Dr. Johanna Pirker, Prof. Dr. Diego Klabjan, Prof. Dr. Pieter Spronck, Yaser Norouzzadeh, Dr. África Perriáñez, Paul Bertens, Prof. Dr. Daniel Johnson, Prof. Dr. Fabio Zambetta, Dr. Marco Tamassia, Dr. William Raffe, Prof. Dr. Michael Hitchens, Sridev Srikanth and Raheel Yawar for our valuable discussions and collaborations.

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Bonn, Germany
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1 Introduction to Player Profiling and Matrix Factorization

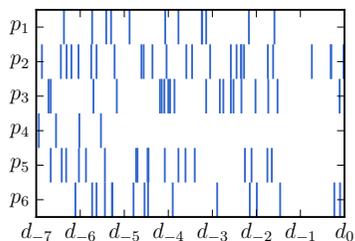
The fundamental objective of the process of profiling user behavior in the context of game analytics is about helping the game development team to better understand player behavior. In this work, we will focus on different matrix and tensor factorization models for factorizing behavioral data matrices to extract efficient representations that reveal interesting insights about the analyzed player population and can be further used in higher-level analytics applications. In order to motivate ourselves to the use of such models in industry settings, in this chapter we will define the notion of behavioral profiling in the context of game analytics, take a brief look at the types of collected behavioral data and the workflow of typical profiling frameworks and finally present an overview of this book.

1.1 Analytics from Telemetry Data

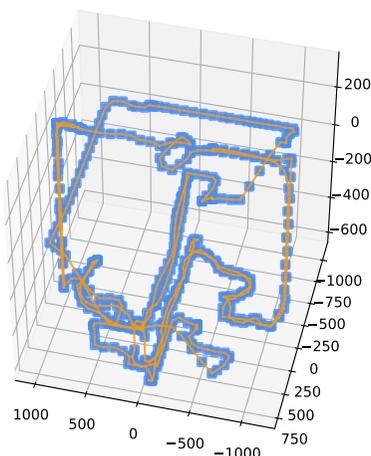
Today's gaming environments are becoming increasingly complex and owing to (arguably) inexpensive storage solutions it is now possible to track every in-game action of any player in real- or quasi-real time. Although the granularity and the type of the collected data is game- and tracking system dependent, there are some types that are universal for most of the settings. These include meta data (e.g. player id, country, registration date, device type etc.), activities on time (e.g. arrivals,

ID	Country	Install
FISCHER	DE	01/28/2008
300pingpain	US	03/30/2009
kodia034	CN	01/16/2009
MasterBlaster	TR	04/15/2009
br_B0LS0N4R0_br	BR	12/01/2009
CoupDeGrace	BE	02/14/2009
NeverSaw0815	RU	09/11/2009
uragan002	ES	05/05/2008
9Medic	GB	12/08/2009

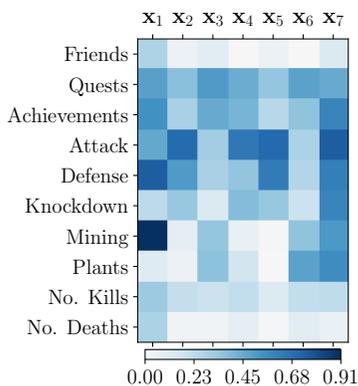
(a) meta information



(b) temporal activities



(c) location



(d) performance snapshots

Figure 1.1: Illustration of different sources of information collected about players of today's games. Common example input types include (a) meta information, (b) activities on time, (c) location in the real and virtual worlds (d) snapshots of predefined performance indicators. Data of these formats can be directly or indirectly fed into matrix and tensor factorization methods to automatically extract features that can be used in a variety of analytics applications. In order to show the behavior of the studied models, in this work, we will be analyzing snapshotted player performance data (similar to (d)). Additionally, we will layout some practical ideas about harnessing different data sources for behavioral profiling at the end of the book.

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