

Dmitry
Vostokov

Visual category Theory

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$\text{Part}_6 \in C^{\text{Parts}}$

Visual Category Theory Brick by Brick, Part 6: Using LEGO® to Teach Abstract Mathematics

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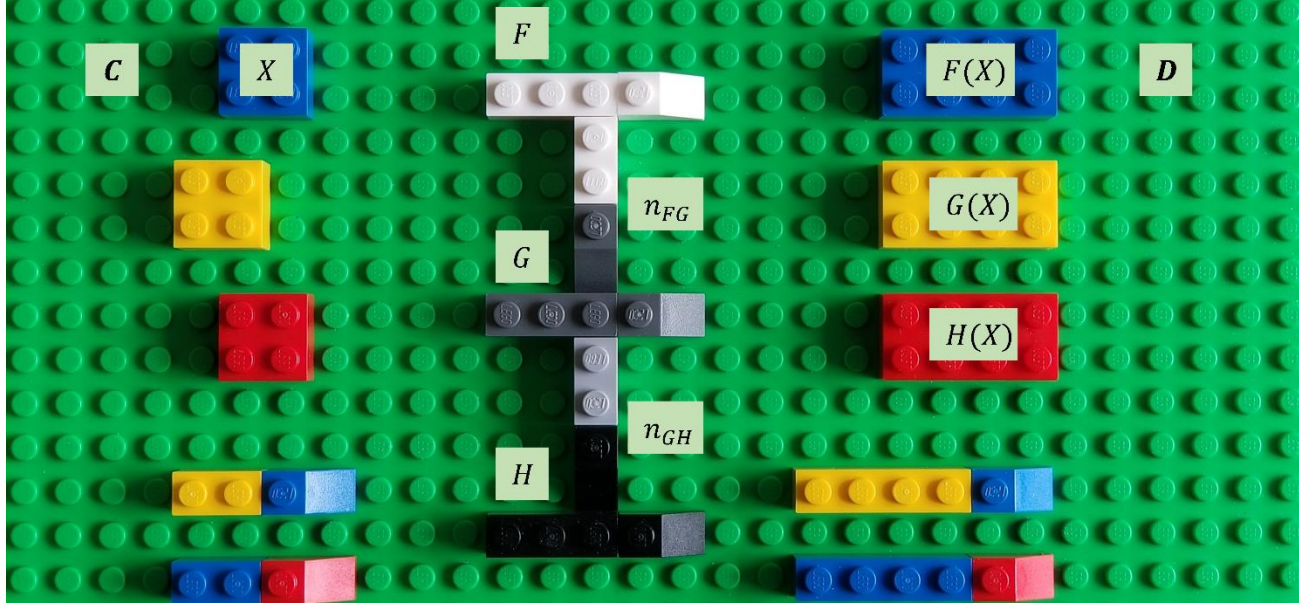
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In *Part₁* we introduced natural transformations between functors. Natural transformations can be “vertically” composed.

$F, G, H : \mathcal{C} \rightarrow \mathcal{D}$, $X \in \mathcal{C}$, $F(X), G(X), H(X) \in \mathcal{D}$

$n_{FG} : F \rightarrow G$, $n_{FG}(X) : F(X) \rightarrow G(X)$, $n_{GH} : G \rightarrow H$, $n_{GH}(X) : G(X) \rightarrow H(X)$

$n_{FH} = n_{GH} \circ n_{FG} : F \rightarrow H$, $n_{FH}(X) = n_{GH}(X) \circ n_{FG}(X) : F(X) \rightarrow H(X)$



In addition to 12 books mentioned in *Part₁*, *Part₃*, *Part₄*, and *Part₅* we also used:

- Iconicity and Abduction by Gianluca Caterina and Rocco Gangle
- Directed Algebraic Topology: Models of Non-Reversible Worlds by Marco Grandis

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