

For most 2-by-1 and 3-by-1 multiplication problems, we use the **addition method**, but sometimes it may be faster to use subtraction. By practicing these skills, you will be able to move on to multiplying most 2-digit numbers together. ■

### Important Terms

**addition method:** A method for multiplying numbers by breaking the problem into sums of numbers. For example,  $4 \times 17 = (4 \times 10) + (4 \times 7) = 40 + 28 = 68$ , or  $41 \times 17 = (40 \times 17) + (1 \times 17) = 680 + 17 = 697$ .

**distributive law:** The rule of arithmetic that combines addition with multiplication, specifically  $a \times (b + c) = (a \times b) + (a \times c)$ .

**factoring method:** A method for multiplying numbers by factoring one of the numbers into smaller parts. For example,  $35 \times 14 = 35 \times 2 \times 7 = 70 \times 7 = 490$ .

### Suggested Reading

Benjamin and Shermer, *Secrets of Mental Math: The Mathemagician's Guide to Lightning Calculation and Amazing Math Tricks*, chapter 2.

Julius, *More Rapid Math Tricks and Tips: 30 Days to Number Mastery*.

———, *Rapid Math Tricks and Tips: 30 Days to Number Power*.

Kelly, *Short-Cut Math*.

### Problems

Because 2-by-1 and 3-by-1 multiplication problems are so important, an ample number of practice problems are provided. Calculate the following 2-by-1 multiplication problems in your head using the addition method.

1.  $40 \times 8$

2.  $42 \times 8$

3.  $20 \times 4$

4.  $28 \times 4$

5.  $56 \times 6$

6.  $47 \times 5$

7.  $45 \times 8$

8.  $26 \times 4$

9.  $68 \times 7$

10.  $79 \times 9$

11.  $54 \times 3$

12.  $73 \times 2$

13.  $75 \times 8$

14.  $67 \times 6$

15.  $83 \times 7$

16.  $74 \times 6$

17.  $66 \times 3$

18.  $83 \times 9$

19.  $29 \times 9$

20.  $46 \times 7$

Calculate the following 2-by-1 multiplication problems in your head using the addition method and the subtraction method.

**21.**  $89 \times 9$

**22.**  $79 \times 7$

**23.**  $98 \times 3$

**24.**  $97 \times 6$

**25.**  $48 \times 7$

The following problems arise while squaring 2-digit numbers or multiplying numbers that are close together. They are essentially 2-by-1 problems with a 0 attached.

**26.**  $20 \times 16$

**27.**  $20 \times 24$

**28.**  $20 \times 25$

**29.**  $20 \times 26$

**30.**  $20 \times 28$

**31.**  $20 \times 30$

**32.**  $30 \times 28$

**33.**  $30 \times 32$

**34.**  $40 \times 32$

**35.**  $30 \times 42$

**36.**  $40 \times 48$

**37.**  $50 \times 44$

**38.**  $60 \times 52$

**39.**  $60 \times 68$

**40.**  $60 \times 69$

**41.**  $70 \times 72$

**42.**  $70 \times 78$

**43.**  $80 \times 84$

**44.**  $80 \times 87$

**45.**  $90 \times 82$

**46.**  $90 \times 96$

Here are some more problems that arise in the first step of a 2-by-2 multiplication problem.

**47.**  $30 \times 23$

**48.**  $60 \times 13$

**49.**  $50 \times 68$

**50.**  $90 \times 26$

**51.**  $90 \times 47$

**52.**  $40 \times 12$

**53.**  $80 \times 41$

**54.**  $90 \times 66$

**55.**  $40 \times 73$

Calculate the following 3-by-1 problems in your head.

**56.**  $600 \times 7$

**57.**  $402 \times 2$

**58.**  $360 \times 6$

**59.**  $360 \times 7$

**60.**  $390 \times 7$

**61.**  $711 \times 6$

**62.**  $581 \times 2$

**63.**  $161 \times 2$

**64.**  $616 \times 7$

**65.**  $679 \times 5$

**66.**  $747 \times 2$

**67.**  $539 \times 8$

**68.**  $143 \times 4$

**69.**  $261 \times 8$

**70.**  $624 \times 6$

**71.**  $864 \times 2$

**72.**  $772 \times 6$

**73.**  $345 \times 6$

**74.**  $456 \times 6$

**75.**  $476 \times 4$

**76.**  $572 \times 9$

**77.**  $667 \times 3$

When squaring 3-digit numbers, the first step is to essentially do a 3-by-1 multiplication problem like the ones below.

**78.**  $404 \times 400$

**79.**  $226 \times 200$

**80.**  $422 \times 400$

**81.**  $110 \times 200$

**82.**  $518 \times 500$

**83.**  $340 \times 300$

**84.**  $650 \times 600$

**85.**  $270 \times 200$

**86.**  $706 \times 800$

**87.**  $162 \times 200$

**88.**  $454 \times 500$

**89.**  $664 \times 700$

Use the factoring method to multiply these 2-digit numbers together by turning the original problem into a 2-by-1 problem, followed by a 2-by-1 or 3-by-1 problem.

**90.**  $43 \times 14$

**91.**  $64 \times 15$

**92.**  $75 \times 16$

**93.**  $54 \times 24$

**94.**  $89 \times 72$

In poker, there are 2,598,960 ways to be dealt 5 cards (from 52 different cards, where order is not important). Calculate the following multiplication problems that arise through counting poker hands.

- 95.** The number of hands that are straights (40 of which are straight flushes) is

$$10 \times 4^5 = 4 \times 4 \times 4 \times 4 \times 4 \times 10 = ???$$

- 96.** The number of hands that are flushes is

$$(4 \times 13 \times 12 \times 11 \times 10 \times 9)/120 = 13 \times 11 \times 4 \times 9 = ???$$

- 97.** The number of hands that are four-of-a-kind is  $13 \times 48 = ???$

- 98.** The number of hands that are full houses is  $13 \times 12 \times 4 \times 6 = ???$

*Solutions for this lecture begin on page 97.*