Forecasting The Equity Risk Premium: The Role Of Technical Indicators,

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Forecasting the Equity Risk Premium: The Role of Technical Indicators

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Forecasting the Equity Risk Premium: 
The Role of Technical Indicators

Abstract

Academic research relies extensively on macroeconomic variables to forecast the U.S. equity risk premium, with relatively little attention paid to the technical indicators widely employed by practitioners. Our paper fills this gap by comparing the forecasting ability of technical indicators with that of macroeconomic variables. Technical indicators display statistically and economically significant in-sample and out-of-sample forecasting power, matching or exceeding that of macroeconomic variables. Furthermore, technical indicators and macroeconomic variables provide complementary information over the business cycle: technical indicators better detect the typical decline in the equity risk premium near business-cycle peaks, while macroeconomic variables more readily pick up the typical rise in the equity risk premium near cyclical troughs. Consistent with this behavior, we show that combining information from both technical indicators and macroeconomic variables significantly improves equity risk premium forecasts versus using either type of information alone. Overall, the substantial countercyclical fluctuations in the equity risk premium appear well captured by the combined information in technical indicators and macroeconomic variables.

*JEL* classification: C53, C58, E32, G11, G12, G17

*Key words:* equity risk premium predictability; macroeconomic variables; moving-average rules; momentum; volume; sentiment; out-of-sample forecasts; asset allocation; business cycle
1. Introduction
Numerous studies report evidence of U.S. equity risk premium predictability based on assorted macroeconomic variables, including the dividend-price ratio (Rozell 1984, Campbell and Shiller 1988, Fama and French 1988, Cochrane 2008, Pástor and Stambaugh 2009), inflation rate (Nelson 1976, Fama and Schwert 1977, Campbell and Voulteenaho 2004), nominal interest rates and interest rate spreads (Keim and Stambaugh 1986, Campbell 1987, Breen, Glosten, and Jagannathan 1989, Fama and French 1989), consumption-wealth ratio (Lettau and Ludvigson 2001), and volatility (Guo 2006). Ang and Bekaert (2007), Hjalmarsson (2010), and Henkel, Martin, and Nadari (2011) find that macroeconomic variables also predict the equity risk premium across countries.¹ The ability of macroeconomic variables to predict the equity risk premium has profoundly shifted the emphasis of asset pricing theory from expected cash flows to discount rates (Cochrane 2011).

Relative to macroeconomic variables (i.e., “economic fundamentals”), technical indicators have received significantly less attention in the literature, despite their widespread use among practitioners (Schwager 1989, 1992, 2012, Billingsley and Chance 1996, Menkhoff and Taylor 2007, Park and Irwin 2007, Covel 2009, Lo and Hasanhodzic 2009, 2010). Technical indicators rely on past price and volume patterns to identify price trends believed to persist into the future. Existing studies analyze the profitability of trading strategies based on a variety of technical indicators, including filter rules (Fama and Blume 1966), moving averages (Brock, Lakonishok, and LeBaron 1992), momentum (Conrad and Kaul 1998, Ahn, Conrad, and Dittmar 2003), and automated pattern recognition (Lo, Mamaysky, and Wang 2000). These studies, however, do not specifically analyze how well technical indicators directly predict the equity risk premium, which is the focus of the vast literature on equity risk premium predictability based on macroeconomic variables.

In this paper, we investigate the capacity of technical indicators to directly forecast the equity risk premium and compare their performance to that of macroeconomic variables. In comparing the technical and macroeconomic predictors, we generate all forecasts in a standard predictive regression framework, where the equity risk premium is regressed on a constant and the lag of a macroeconomic variable or technical indicator. To parsimoniously incorporate information from many predictors, we also estimate predictive regressions based on a small number of principal components extracted from the entire set of macroeconomic

¹The studies cited are representative and do not constitute an exhaustive list. For example, Johannes, Korteweg, and Polson (2013) recently examine return predictability under model uncertainty and learning using Bayesian methods.
variables and/or technical indicators. Our investigation complements existing studies of equity risk premium predictability, which ignore technical indicators, as well as existing studies of technical indicators, which focus on the profitability of technical strategies.

We employ both in-sample and out-of-sample tests, as each testing approach has its relative merits. Because they use all available data, in-sample tests have more power for detecting return predictability. In-sample estimation also provides more efficient parameter estimates and thus more precise estimates of the expected equity risk premium. On the other hand, out-of-sample tests implicitly examine the stability of the data-generating process and guard against in-sample overfitting. Employing both in-sample and out-of-sample tests helps to establish the robustness of our results.

We use data spanning 1950:12 to 2011:12 for 14 well-known macroeconomic variables from the literature and 14 common technical indicators, including those based on moving averages, momentum, and volume. In-sample results demonstrate that individual technical indicators typically predict the equity risk premium as well as, or better than, individual macroeconomic variables.\footnote{In independent and subsequent (to this paper) research, Goh, Jiang, Tu, and Zhou (2012) find that technical indicators have greater predictive power than macroeconomic variables for U.S. bond returns.} Regressions based on principal components extracted from the 14 macroeconomic variables (PC-ECON model) or 14 technical indicators (PC-TECH model) reveal that both macroeconomic variables as a group and technical indicators as a group significantly predict the equity risk premium. Moreover, the in-sample $R^2$ statistic for a predictive regression based on principal components extracted from the entire set of macroeconomic variables and technical indicators taken together (PC-ALL model) equals the sum of the $R^2$ statistics for the PC-ECON and PC-TECH models. The additive nature of the predictability indicates that macroeconomic variables and technical indicators capture different types of information that is relevant for predicting the equity risk premium and thus represent complementary approaches to equity risk premium forecasting.

Consistent with differential information, the PC-ECON and PC-TECH model estimates of the expected equity risk premium display complementary countercyclical patterns. Technical indicators better detect the typical decline in the actual equity risk premium near business-cycle peaks, while macroeconomic variables more readily pick up the typical rise in the actual equity risk premium later in recessions near cyclical troughs. The PC-ALL model estimate of the expected equity risk premium exhibits an even clearer countercyclical pattern. This accentuated countercyclical pattern enables the expected equity risk premium generated by the PC-ALL model to better track the sizable fluctuations in the actual equity risk premium around
business-cycle peaks and troughs.

Out-of-sample results confirm the in-sample results. Forecast encompassing tests suggest that utilizing information from both macroeconomic variables and technical indicators can improve equity risk premium forecasts. Indeed, the PC-ALL model performs the best and significantly outperforms the historical average forecast, which Goyal and Welch (2003, 2008) show to be a very stringent benchmark. Furthermore, the PC-ALL forecast has substantial economic value for a mean-variance investor with a relative risk coefficient of five who optimally allocates across equities and risk-free Treasury bills. In particular, the investor realizes substantial utility gains by using the PC-ALL forecast versus ignoring any forecastability or using the information in macroeconomic variables alone.

Theoretically, why do macroeconomic variables and technical indicators predict the equity risk premium? In dynamic asset pricing models, the future state of the economy is the fundamental driver of time-varying expected stock returns. Macroeconomic variables track changing macroeconomic conditions and should thus have predictive power for the equity risk premium. This predictive ability reflects time-varying compensation to investors for bearing aggregate risk and is consistent with rational asset pricing; see, for example, Cochrane (2011) and the references therein. Explanations of the predictive power of technical indicators are not as well known, however, and require more discussion. There are basically four types of theoretical models that explain why technical indicators can have predictive ability, all of which point to an informationally inefficient market.

The first type of theoretical model recognizes differences in the time for investors to receive information. Under this friction, Treynor and Ferguson (1985) show that technical analysis is useful for assessing whether or not information has been fully incorporated into equity prices, while Brown and Jennings (1989) demonstrate that past prices enable investors to make better inferences about price signals. In addition, Grundy and McNichols (1989) and Blume, Easley, and O’Hara (1994) show that trading volume can provide useful information beyond prices.

The second type of model posits different responses to information by heterogeneous investors. Cespa and Vives (2012) recently show that asset prices can deviate from their fundamental values if there is a positive level of asset residual payoff uncertainty and/or persistence in liquidity trading. In this setting, rational long-term investors follow trends. In the real world, different responses to information are more likely during recessions, due to consumption smoothing asset sales by households that experience job losses and liquidation sales of margined assets by some investors. These factors help to explain why we find that
technical indicators display enhanced predictive ability during recessions.

The next type of model allows for underreaction and overreaction to information. Due to behavioral biases, Hong and Stein (1999) explain that, at the start of a trend, investors underreact to news; as the market rises, investors subsequently overreact, leading to even higher prices. Similarly, positive feedback traders—who buy (sell) after asset prices rise (fall)—can create price trends that technical indicators detect. Hedge fund guru George Soros (2003) argues that positive feedback can actually alter firm fundamentals, thereby justifying to a certain extent the price trends. Edmans, Goldstein, and Jiang (2012) recently show that such feedback trading can occur in a rational model of investors with private information.

Finally, models of investor sentiment shed light on the efficacy of technical analysis. Since Keynes (1936), researchers have analyzed how investor sentiment can drive asset prices away from fundamental value. DeLong, Shleifer, Summers, and Waldmann (1990) show that, in the presence of limits to arbitrage, noise traders with irrational sentiment can cause prices to deviate from fundamentals, even when informed traders recognize the mispricing. Baker and Wurgler (2006, 2007) find that measures of investor sentiment help to explain the cross-section of U.S. equity returns, while Baker, Wurgler, and Yuan (2012) provide similar international evidence. From an asset pricing perspective, Stambaugh, Yu, and Yuan (2012) find that sentiment measures help to explain common pricing anomalies. In this paper, the monthly sentiment-changes index from Baker and Wurgler (2007) is significantly and positively contemporaneously correlated with the realized equity risk premium, and we show that technical indicators significantly predict the sentiment-changes index, while macroeconomic variables do not. The differential information useful for predicting the equity risk premium in technical indicators thus appears related to their ability to anticipate changes in investor sentiment.

In sum, theoretical models based on information frictions help to explain the predictive value of the technical indicators. Empirically, Moskowitz, Ooi, and Pedersen (2012) recently find that pervasive price trends exist across commonly traded equity index, currency, commodity, and bond futures. Insofar as the stock market is not a pure random walk and exhibits periodic trends, technical indicators should prove informative, as they are primarily designed to detect trends.
2. In-Sample Analysis

2.1. Bivariate Predictive Regressions

The conventional framework for analyzing equity risk premium predictability based on macroeconomic variables is the following predictive regression model:

\[ r_{t+1} = \alpha_i + \beta_i x_i, t + \varepsilon_{t+1}, \]

where the equity risk premium, \( r_{t+1} \), is the return on a broad stock market index in excess of the risk-free rate from period \( t \) to \( t + 1 \); \( x_i, t \) is a predictor available at \( t \); and \( \varepsilon_{t+1} \) is a zero-mean disturbance term. Under the null hypothesis of no predictability, \( \beta_i = 0 \), and (1) reduces to the constant expected equity risk premium model. Because theory suggests the sign of \( \beta_i \), Inoue and Kilian (2004) recommend a one-sided alternative hypothesis to increase the power of in-sample tests of predictability; we define \( x_i, t \) such that \( \beta_i \) is expected to be positive under the alternative. We test \( H_0: \beta_i = 0 \) against \( H_A: \beta_i > 0 \) using a heteroskedasticity-consistent \( t \)-statistic corresponding to \( \hat{\beta}_i \), the ordinary least squares (OLS) estimate of \( \beta_i \) in (1).

The well-known Stambaugh (1999) bias potentially inflates the \( t \)-statistic for \( \hat{\beta}_i \) in (1) and distorts test size when \( x_i, t \) is highly persistent, as is the case for a number of popular predictors. We address this concern by computing \( p \)-values using a wild bootstrap procedure that accounts for the persistence in regressors and correlations between equity risk premium and predictor innovations, as well as general forms of heteroskedasticity. The Online Appendix accompanying this paper details the wild bootstrap procedure.\(^3\)

We estimate predictive regressions using updated monthly data from Goyal and Welch (2008).\(^4\) The equity risk premium is the difference between the continuously compounded return on the S&P 500 (including dividends) and the log return on a risk-free bill. The following 14 macroeconomic variables are representative of the literature (Goyal and Welch 2008) and constitute the set of \( x_i, t \) variables used to predict the equity risk premium in (1):


2. **Dividend yield (log)**, DY: log of a twelve-month moving sum of dividends minus the log of lagged dividends.

\(^3\)Amihud and Hurvich (2004), Lewellen (2004), Campbell and Yogo (2006), and Amihud, Hurvich, and Wang (2009) develop predictive regression tests that explicitly account for the Stambaugh bias. These tests, however, are not necessarily robust to general forms of heteroskedasticity. Inferences based on these procedures are qualitatively similar to those based on the wild bootstrap.

\(^4\)The data are available from Amit Goyal’s web page at http://www.hec.unil.ch/agoyal/.
stock prices.


5. *Equity risk premium volatility*, RVOL: based on the moving standard deviation estimator,

\[
\hat{\sigma}_t = \frac{1}{12} \sum_{i=1}^{12} |r_{t+1-i}|, \quad (2)
\]

and subsequently converted to

\[
\hat{\text{Vol}}_t = \sqrt{\frac{\pi}{2}} \sqrt{12\hat{\sigma}_t}. \quad (3)
\]


7. *Net equity expansion*, NTIS: ratio of a twelve-month moving sum of net equity issues by NYSE-listed stocks to the total end-of-year market capitalization of NYSE stocks.


14. *Inflation*, INFL: calculated from the Consumer Price Index (CPI) for all urban consumers; we use \(x_{i,t-1}\) in (1) for inflation to account for the delay in CPI releases.

Table 1 reports summary statistics for the equity risk premium and 14 macroeconomic variables for 1950:12 to 2011:12. The start of the sample reflects data availability for the technical indicators (discussed below). The average monthly equity risk premium is 0.47%, which, together with a monthly standard deviation of 4.26%, produces a monthly Sharpe ratio of 0.11. Most of the macroeconomic variables are

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5This is the volatility measure used by Mele (2007). Goyal and Welch (2008) measure monthly volatility as the sum of squared daily excess stock returns during the month. This measure, however, produces a severe outlier in October of 1987. \(\hat{\text{Vol}}_t\) avoids this problem and yields more plausible estimation results.
strongly autocorrelated, particularly the valuation ratios, nominal interest rates, and interest rate spreads.

To compare technical indicators to the macroeconomic variables, we employ 14 technical indicators based on three popular technical strategies. The first is a moving-average (MA) rule that generates a buy or sell signal \( S_{i,t} = 1 \) or \( S_{i,t} = 0 \), respectively) at the end of \( t \) by comparing two moving averages:

\[
S_{i,t} = \begin{cases} 
1 & \text{if } \text{MA}_{s,t} \geq \text{MA}_{l,t} \\
0 & \text{if } \text{MA}_{s,t} < \text{MA}_{l,t} 
\end{cases}
\]  

(4)

where

\[
\text{MA}_{j,t} = \frac{1}{j} \sum_{i=0}^{j-1} P_{t-i} \text{ for } j = s, l;
\]

(5)

\( P_t \) is the level of a stock price index; and \( s \) (\( l \)) is the length of the short (long) MA \((s < l)\). We denote the MA indicator with MA lengths \( s \) and \( l \) by \( \text{MA}(s, l) \). Intuitively, the MA rule detects changes in stock price trends, because the short MA will be more sensitive to recent price movement than the long MA. For example, when prices have recently been falling, the short MA will tend to be lower than the long MA. If prices begin trending upward, then the short MA tends to increase faster than the long MA, eventually exceeding the long MA and generating a buy signal. We analyze monthly MA rules with \( s = 1, 2, 3 \) and \( l = 9, 12 \).

The second technical strategy is based on momentum. A simple momentum rule generates the following signal:

\[
S_{i,t} = \begin{cases} 
1 & \text{if } P_t \geq P_{t-m} \\
0 & \text{if } P_t < P_{t-m} 
\end{cases}
\]  

(6)

Intuitively, a current stock price that is higher than its level \( m \) periods ago indicates “positive” momentum and relatively high expected excess returns, thereby generating a buy signal. We denote the momentum indicator that compares \( P_t \) to \( P_{t-m} \) by \( \text{MOM}(m) \), and we compute monthly signals for \( m = 9, 12 \).

Technical analysts frequently employ volume data in conjunction with past prices to identify market trends. In light of this, the final technical strategy we consider incorporates “on-balance” volume (e.g., Granville 1963). We first define

\[
\text{OBV}_t = \sum_{k=1}^{t} \text{VOL}_k D_k,
\]

(7)

where \( \text{VOL}_k \) is a measure of the trading volume during period \( k \) and \( D_k \) is a binary variable that takes a
value of one if \( P_k - P_{k-1} \geq 0 \) and \(-1\) otherwise. We then form a trading signal from \( OBV_t \) as

\[
S_{i,t} = \begin{cases} 
1 & \text{if } MA_{s,t}^{OBV} \geq MA_{l,t}^{OBV} \\
0 & \text{if } MA_{s,t}^{OBV} < MA_{l,t}^{OBV}
\end{cases},
\]

where

\[
MA_{j,t}^{OBV} = (1/j) \sum_{i=0}^{j-1} OBV_{t-i} \quad \text{for } j = s, l.
\]

Intuitively, relatively high recent volume together with recent price increases, say, indicate a strong positive market trend and generate a buy signal. We compute monthly signals for \( s = 1, 2, 3 \) and \( l = 9, 12 \) and denote the corresponding indicator by \( \text{VOL}(s,l) \).

The MA, momentum, and volume-based indicators are representative of the trend-following technical indicators analyzed in the academic literature (e.g., Sullivan, Timmermann, and White 1999). We use the S&P 500 index and monthly volume data from Google Finance in (4), (6), and (8).\(^6\) After accounting for the lags in constructing the technical indicators, we have observations for all of the indicators starting in 1950:12.\(^7\) The technical indicators generate buy signals \( (S_{i,t} = 1) \) between 66% and 72% of the time.

To directly compare these technical indicators to equity risk premium forecasts based on macroeconomic variables, we transform the technical indicators to point forecasts of the equity risk premium by replacing \( x_{i,t} \) in (1) with \( S_{i,t} \) from (4), (6), or (8):

\[
r_{t+1} = \alpha_i + \beta_i S_{i,t} + \varepsilon_{i,t+1}.
\]

Because \( S_{i,t} = 1 \) \( (S_{i,t} = 0) \) represents a bullish (bearish) signal, we again test \( H_0: \beta_i = 0 \) against \( H_A: \beta_i > 0 \).

Panel A of Table 2 reports estimates of \( \beta_i \) for the bivariate predictive regressions given by (1) and (10), as well as heteroskedasticity-consistent \( t \)-statistics and \( R^2 \) statistics. After accounting for the lag in the predictive regression, the estimation sample is 1951:01 to 2011:12 (732 observations). Six of the 14 macroeconomic variables exhibit significant predictive ability at conventional levels in the second column of Panel A: DY, RVOL, TBL, LTY, LTR, and TMS. Among these six significant predictors, the dividend

\(^6\)The volume data are available at http://www.google.com/finance.

\(^7\)Technical indicators are often computed using monthly, weekly, or daily data. We compute technical indicators using monthly data to put the forecasts based on macroeconomic variables and technical indicators on a more equal footing. In ongoing research, we are investigating the use of weekly and daily data to generate monthly trading signals to study the more practical problem of maximizing portfolio performance using technical indicators.
yield, Treasury bill rate, and term spread are among the most studied in the literature. At first glance, the $R^2$ statistics in the third column of Panel A appear small. However, because monthly stock returns inherently contain a substantial unpredictable component, a monthly $R^2$ near 0.5% can represent an economically significant degree of equity risk premium predictability (Kandel and Stambaugh 1996, Xu 2004, Campbell and Thompson 2008). Five of the $R^2$ statistics in the third column of Panel A exceed this 0.5% benchmark.

Turning to the results for the technical indicators, 13 of the 14 indicators evidence significant predictive ability at conventional levels in the seventh column of Table 2, Panel A. The coefficient estimates indicate that a buy signal predicts that the next month’s equity risk premium is higher by 48 to 94 basis points than when there is a sell signal. In addition, 10 of the 14 $R^2$ statistics in the eighth column of Panel A are above the 0.5% threshold, and the $R^2$ for MA(2,12) is 1.03%, which is the largest $R^2$ in Panel A. Overall, the in-sample bivariate regression results in Table 2, Panel A suggest that individual technical indicators generally predict the equity risk premium as well as, or better than, individual macroeconomic variables.

We are interested in gauging the relative strength of equity risk premium predictability during NBER-dated business-cycle expansions and recessions. Computing $R^2$ statistics separately for cyclical expansions and recessions is the most natural way to proceed. Because of the nature of the $R^2$ statistic, however, there is no clean decomposition of the full-sample $R^2$ statistic into sub-sample $R^2$ statistics based on the full-sample parameter estimates. To compare the degree of return predictability across expansions and recessions, we compute the following intuitive versions of the conventional $R^2$ statistic:

$$R^2_c = 1 - \frac{\sum_{t=1}^{T} I^c_t \hat{\varepsilon}^2_{i,t}}{\sum_{t=1}^{T} I^c_t (r_t - \bar{r})^2} \text{ for } c = \text{EXP, REC};$$

where $I^\text{EXP}_t$ ($I^\text{REC}_t$) is an indicator variable that takes a value of unity when month $t$ is an expansion (recession) and zero otherwise; $\hat{\varepsilon}_{i,t}$ is the fitted residual based on the full-sample estimates of the predictive regression model in (1) or (10); $\bar{r}$ is the full-sample mean of $r_t$; and $T$ is the number of usable observations for the full sample. Observe that, unlike the full-sample $R^2$ statistic, the $R^2_\text{EXP}$ and $R^2_\text{REC}$ statistics can be negative. The fourth and fifth columns of Table 2, Panel A indicate that equity risk premium predictability is substantially higher for recessions vis-à-vis expansions for a number of the macroeconomic variables, including DP, DY, RVOL, TBL, LTR, TMS, and DFR. According to the last two columns of Panel A, predictability is highly concentrated during recessions for all of the technical indicators.
2.2. Predictive Regressions Based on Principal Components

Next, we incorporate information from multiple macroeconomic variables by estimating a predictive regression based on principal components.\(^8\) Let \(x_t = (x_{1,t}, \ldots, x_{N,t})'\) denote the \(N\)-vector (\(N = 14\)) of the entire set of macroeconomic variables and let \(\hat{F}^{ECON}_t = (\hat{F}^{ECON}_{1,t}, \ldots, \hat{F}^{ECON}_{K,t})'\) denote the vector containing the first \(K\) principal components extracted from \(x_t\) (where \(K \ll N\)). The principal component predictive regression (PC-ECON model) is given by

\[
r_{t+1} = \alpha + \sum_{k=1}^{K} \beta k \hat{F}^{ECON}_{k,t} + \epsilon_{t+1}. \tag{12}\]

Principal components parsimoniously incorporate information from a large number of potential predictors in a predictive regression. The first few principal components identify the key comovements among the entire set of predictors, which filters out much of the noise in individual predictors, thereby guarding against in-sample overfitting.

We again estimate (12) via OLS, compute heteroskedasticity-consistent \(t\)-statistics, and base inferences on wild bootstrapped \(p\)-values. The first five columns of Table 2, Panel B report estimation results for (12) with \(K = 3\), the value selected by the adjusted \(R^2\).\(^9\) The coefficient estimate on the third principal component is significant at the 1% level. The \(R^2\) for the PC-ECON model is 1.18%, which is greater than the 0.5% benchmark. The \(R^2_{EXP}\) and \(R^2_{REC}\) statistics indicate that equity risk premium predictability is over twice as large for recessions compared to expansions.

To illustrate the economic content of the principal components, Panels A through C of Figure 1 present the estimated principal components \((\{\hat{F}^{ECON}_{k,t}\})_{k=1}^{3}\), while the corresponding panels in Figure 2 display the estimated loadings for the individual macroeconomic variables on the principal components.\(^10\) Panel A of Figure 2 shows that the valuation ratios (DP, EY, EP, and BM) load heavily on \(\hat{F}^{ECON}_{1,t}\); that is, the first princi-

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\(^8\)Ludvigson and Ng (2007, 2009) estimate predictive regressions for excess stock and bond returns, respectively, based on principal components extracted from macroeconomic variables.

\(^9\)The AIC also selects \(K = 3\). To keep the model reasonably parsimonious, we consider a maximum \(K\) value of three, given the 14 macroeconomic variables. Note that we account for the “estimated regressors” in (12) via the wild bootstrap procedure (as explained in the Online Appendix). Bai and Ng (2006) analyze the asymptotic properties of parameter estimates for predictive regressions with estimated principal components.

\(^10\)The \(x_{i,t}\) variables, estimated principal components, and estimated loadings are related via \(x_{i,t} - \bar{x}_i = \sum_{k=1}^{K} \hat{\lambda}_{i,k} \hat{F}^{ECON}_{k,t} + \hat{\epsilon}_{i,t}\) (\(i = 1, \ldots, N\)), where \(\bar{x}_i\) is the sample mean of \(x_{i,t}\) (so that, following convention, the principal components have zero mean), \(\hat{\lambda}_{i,k}\) is the estimated loading of the \(i\)th variable on the \(k\)th factor, and \(\hat{\epsilon}_{i,t}\) is the estimated idiosyncratic component of \(x_{i,t}\). Note that the scales and signs of the principal components and loadings are indeterminate. Principal component estimation uses a normalization to identify the scales and signs of the principal components and loadings. This normalization has no effect on the \(t\)-statistics, \(R^2\) statistics, or expected equity risk premium estimates in (12), (13), or (14).
pal component extracted from the macroeconomic variables primarily captures common fluctuations in the valuation ratios. This is also evident in Figure 1, Panel A, where the persistence of $\hat{F}_{1,t}^{\text{ECON}}$ (autocorrelation of 0.99) matches that of the individual valuation ratios in Table 1. From Figure 2, Panel B, we see that RVOL and DFY load most heavily on $\hat{F}_{2,t}^{\text{ECON}}$; accordingly, $\hat{F}_{2,t}^{\text{ECON}}$ spikes during the Global Financial Crisis in Figure 1, Panel B, when stock market volatility and credit spreads increased dramatically. Panel C of Figure 2 indicates that a number of the macroeconomic variables load relatively strongly on $\hat{F}_{3,t}^{\text{ECON}}$, including DP, DY, DE, TBL, LT, TMS, DFR, and INFL. $\hat{F}_{3,t}^{\text{ECON}}$ thus reflects a wider variety of macroeconomic variables and potentially captures more useful predictive information, which apparently helps $\hat{F}_{3,t}^{\text{ECON}}$ to better forecast the equity risk premium than $\hat{F}_{1,t}^{\text{ECON}}$ and $\hat{F}_{2,t}^{\text{ECON}}$. Although the three principal components extracted from the 14 macroeconomic variables are contemporaneously uncorrelated by construction, they all exhibit countercyclical tendencies in Panels A through C of Figure 1. The countercyclical pattern is especially evident for $\hat{F}_{2,t}^{\text{ECON}}$ and $\hat{F}_{3,t}^{\text{ECON}}$, which have distinct local minima (maxima) near business-cycle peaks (troughs).

To incorporate information from all of the technical indicators, we estimate (12) with $\hat{F}_{t}^{\text{TECH}}$ replacing $\hat{F}_{t}^{\text{ECON}}$ (PC-TECH model):

$$r_{t+1} = \alpha + \sum_{k=1}^{K} \beta_k \hat{F}_{k,t}^{\text{TECH}} + \epsilon_{t+1},$$

(13)

where $\hat{F}_{t}^{\text{TECH}} = (\hat{F}_{1,t}^{\text{TECH}}, \ldots, \hat{F}_{K,t}^{\text{TECH}})'$ is the vector containing the first $K$ principal components extracted from $S_t = (S_{1,t}, \ldots, S_{N,t})'$, the $N$-vector of 14 technical indicators. The last five columns of Table 2, Panel B report estimation results for (13) with $K = 1$ (the value selected by the adjusted $R^2$). The coefficient estimate on the first principal component is significant at the 5% level, and the $R^2$ for the PC-TECH model is 0.84% (which is again above the 0.5% benchmark). The 14 technical indicators, taken as a group, thus significantly predict the equity risk premium. Similarly to Panel A, the last two columns of Panel B indicate that return predictability based on technical indicators is substantially higher for recessions vis-à-vis expansions.

The last panels in Figures 1 and 2 show the $\hat{F}_{1,t}^{\text{TECH}}$ estimates and estimated loadings for the technical indicators on the first principal component, respectively. The technical indicators load nearly uniformly on $\hat{F}_{1,t}^{\text{TECH}}$ in Figure 2, Panel D, so that the first principal component is essentially a simple average of the 14 indicators. Intuitively, this implies that if the first principal component takes a large (small) value, then most of the individual technical indicators are giving a buy (sell) signal; hence, the first principle component acts like a “consensus” indicator. Panel D of Figure 1 indicates that $\hat{F}_{1,t}^{\text{TECH}}$ is also linked to business-cycle
panels A through C of Figure 2 also load heavily on \( \hat{\beta}_1 \) at the 5%, 10%, and 1% levels, respectively. Panel D of Figures 3 and 4 demonstrates that \( \hat{R} \) sum of the Table 2 reveals that the coefficients are relatively insensitive to this factor, so that \( \hat{\beta} \) technical indicators load nearly uniformly on the first principal component, while the macroeconomic variables or technical indicators. Panel C of Figure 2 also load heavily on \( \hat{F} \) for the PC-ALL model is 2.02%, which equals the sum of the \( R^2 \) statistics for the PC-ECON and PC-TECH models. This indicates that the macroeconomic variables and technical predictors essentially contain complementary information. Continuing the pattern, the fourth and fifth columns of Panel C show that equity risk premium predictability is much stronger in the PC-ALL model for recessions compared to expansions.\(^\text{13} \)

The \( \{\hat{F}^{\text{ALL}}\}_{k=1}^{4} \) estimates and corresponding loading estimates, shown in Figures 3 and 4, respectively, reflect the complementarity of the macroeconomic variables and technical indicators; that is, the principal components extracted from the entire set of predictors are often very similar to those extracted separately from the set of macroeconomic variables or technical indicators. Panel A of Figure 4 shows that the 14 technical indicators load nearly uniformly on the first principal component, while the macroeconomic variables are relatively insensitive to this factor, so that \( \hat{F}^{\text{ALL}} \) is closely related to \( \hat{F}^{\text{TECH}} \). Panel A of Figure 3 confirms this relationship, as \( \hat{F}^{\text{ALL}} \) behaves very similarly to \( \hat{F}^{\text{TECH}} \) in Figure 1, Panel D. Panels B through D of Figures 3 and 4 demonstrate that \( \hat{F}^{\text{ALL}}_{1,t}, \hat{F}^{\text{ALL}}_{3,t}, \) and \( \hat{F}^{\text{ALL}}_{4,t} \) closely correspond to \( \hat{F}^{\text{ECON}}_{1,t}, \hat{F}^{\text{ECON}}_{2,t}, \) and \( \hat{F}^{\text{ECON}}_{3,t} \), respectively. The same macroeconomic variables that load heavily on \( \hat{F}^{\text{ECON}}_{1,t}, \hat{F}^{\text{ECON}}_{2,t}, \) and \( \hat{F}^{\text{ECON}}_{3,t} \) in Panels A through C of Figure 2 also load heavily on \( \hat{F}^{\text{TECH}}_{2,t}, \hat{F}^{\text{TECH}}_{3,t}, \) and \( \hat{F}^{\text{TECH}}_{4,t} \) in Panels B through D of Figure 2.

\(^{11} K = 4 \) is selected by the adjusted \( R^2 \). We consider a maximum \( K \) value of four, since we now extract principal components from 28 potential predictors. The value of four is also the sum of the respective \( K \) values selected for the PC-ECON and PC-TECH models.

\(^{12} \)We checked this result for various subsamples and found that the \( R^2 \) for the PC-ALL model is not always equal to the sum of the \( R^2 \) statistics for the PC-ECON and PC-TECH models, but they are always quite close.

\(^{13} \)We tested for structural breaks in all of the predictive regression models using the Elliott and Müller (2006) \( qLL \) statistic, which is asymptotically efficient for a broad range of persistent breaking processes and has good size and power properties in the presence of heteroskedasticity. Overall, there is little evidence of structural instability in the predictive regressions. The complete results are reported in the Online Appendix.
4, while the technical indicators respond relatively weakly to the latter three factors.\textsuperscript{14} Furthermore, $\hat{F}_{2,t}^{\text{ALL}}$, $\hat{F}_{3,t}^{\text{ALL}}$, and $\hat{F}_{4,t}^{\text{ALL}}$ in Panels B through D of Figure 3 behave similarly to the factors in Panels A through C of Figure 1. The coefficient estimates on $\hat{F}_{2,t}^{\text{ALL}}$ and $\hat{F}_{4,t}^{\text{ALL}}$ in Table 2, Panel C are similar to those on $\hat{F}_{1,t}^{\text{ECON}}$ and $\hat{F}_{3,t}^{\text{ECON}}$, respectively, in Panel B.

The PC-ALL model estimation results thus imply that the macroeconomic variables and technical indicators provide almost completely complementary approaches to equity risk premium prediction. The first principal component in the PC-ALL model is primarily driven by common fluctuations in the technical indicators and only weakly related to the macroeconomic variables; the second through fourth principal components predominantly reflect comovements in subsets of the macroeconomic variables. The significant coefficient estimates on $\hat{F}_{1,t}^{\text{ALL}}$, $\hat{F}_{3,t}^{\text{ALL}}$, and $\hat{F}_{4,t}^{\text{ALL}}$ in the PC-ALL model demonstrate that macroeconomic variables and technical indicators both provide useful information for predicting the equity risk premium.

Figure 5 further illustrates the complementary roles of macroeconomic variables and technical indicators. The figure shows in-sample forecasts of the equity risk premium for the PC-ECON, PC-TECH, and PC-ALL models, which represent in-sample estimates of the expected equity risk premium. The expected equity risk premium for the PC-ECON model in Figure 5, Panel A displays a relatively smooth countercyclical pattern, in line with the estimated factors in Panels A through C of Figure 1.\textsuperscript{15} The countercyclical movements in the expected equity risk premium for the PC-TECH model in Panel B are much more abrupt, in line with Figure 1, Panel D. When the information in the macroeconomic variables and technical indicators is combined in the PC-ALL model in Figure 5, Panel C, the expected equity risk premium falls more abruptly near business-cycle peaks relative to Panel A, while it rises to higher levels around cyclical troughs relative to Panel B. The complementary information in macroeconomic variables and technical indicators thus accentuates the countercyclical fluctuations in the PC-ALL model’s expected equity risk premium.

2.3. Behavior of Expected Equity Risk Premium Around Cyclical Peaks and Troughs

The following regressions provide further insight into the behavior of the expected equity risk premium around business-cycle peaks and troughs:

\begin{equation}
    r_t = a_A + \sum_{m=4}^{-2} b_{A,m} I_{t-m}^P + \sum_{m=4}^{-2} b_{A,m} T_{t-m}^T + u_{A,t},
\end{equation}

\textsuperscript{14}The volume-based technical indicators are possible exceptions, as they respond somewhat strongly to $\hat{F}_{2,t}^{\text{ALL}}$ and $\hat{F}_{4,t}^{\text{ALL}}$.

\textsuperscript{15}The countercyclical pattern in the expected equity risk premium in Figure 5, Panel A is similar to the countercyclical pattern reported in Fama and French (1989), Ferson and Harvey (1991), Whitelaw (1994), Harvey (2001), and Lettau and Ludvigson (2010), among others.
\[
\hat{r}_t = \alpha_{FC} + \sum_{m=4}^{-2} b_{FC,m} I_{t-m}^P + \sum_{m=4}^{-2} b_{FC,m}^T I_{t-m}^T + u_{FC,t},
\]  

(16)

where \( \hat{r}_t \) is the in-sample equity risk premium forecast for the PC-ECON, PC-TECH, or PC-ALL model and \( I_{t}^P \) (\( I_{t}^T \)) is an indicator variable equal to unity when month \( t \) is an NBER-dated business-cycle peak (trough) and zero otherwise. Each \( b_{A,m}^P \) (\( b_{A,m}^T \)) coefficient in (15) measures the average change in the actual equity risk premium \( m \) months from a cyclical peak (trough), while each \( b_{FC,m}^P \) (\( b_{FC,m}^T \)) coefficient does likewise for the expected equity risk premium. Because the equity market is forward looking, we use an asymmetric window that includes the four months before and two months after a peak or trough.\(^\text{16}\)

Figure 6 presents OLS estimates of the slope coefficients in (15) and (16), along with 90% confidence intervals. Panel A of Figure 6 indicates that the actual equity risk premium declines significantly on average for most of the months around a cyclical peak, with an average decline of nearly 400 basis points for some months. Panel B shows that the expected equity risk premium for the PC-ECON model only experiences a significant decline for a few of the months around a peak. In contrast, the PC-TECH model’s expected equity risk premium in Panel C falls significantly for all of the months near a peak, better matching the depressed actual equity risk premium. Similarly to the PC-TECH model, Panel D shows that the expected equity risk premium for the PC-ALL model also falls significantly for most of the months around a peak. In addition, the coefficient magnitudes are larger for the PC-ALL model in Panel D relative to those for the PC-ECON and PC-TECH models in Panels B and C, respectively, so that the PC-ALL model better captures the typically depressed actual equity risk premium near a peak.

Panel E of Figure 6 demonstrates that, in contrast to a cyclical peak, the actual equity risk premium typically rises significantly on average several months prior to a cyclical trough. Generally in line with this behavior, the expected equity risk premium for the PC-ECON model in Panel F increases significantly during the months around a trough. The expected equity risk premium for the PC-TECH model in Panel G rises around a trough, but the increase is not significant. The PC-ALL model’s average expected equity risk premium increases significantly for many of the months around a trough, and the increase in the expected equity risk premium is large during and after a trough, again helping the PC-ALL model to better match the rise in the actual equity risk premium around a trough.

Overall, Figure 6 indicates that the information in technical indicators is more useful than that in macroe-
onomic variables for detecting the typical decline in the equity risk premium around a business-cycle peak, while macroeconomic variables provide more useful information than technical indicators for ascertaining the typical rise in the equity risk premium near a cyclical trough. By incorporating information from both macroeconomic variables and technical indicators, the PC-TECH model exploits the information in each set of predictors to produce an expected equity risk premium that better tracks the substantial countercyclical fluctuations in the equity risk premium.

2.4. Sentiment and Conditional Asset Pricing

Sections 2.1 and 2.2 show that technical indicators predict the equity risk premium. To further establish that technical indicators contain meaningful economic information, we ask two questions. First, do technical indicators forecast changes in investor sentiment, which are known to be correlated with stock returns? Second, do technical indicators have significant effects in a conditional asset pricing model? Positive answers to these questions provide further evidence of the economic relevance of technical indicators.

Positive answers to these questions also allay data-mining concerns, which are relevant for stock return predictability (e.g., Ferson, Sarkissian, and Simin, 2003). In particular, exploring the economic relevance of technical indicators along additional dimensions reduces the likelihood that the significant predictive ability of technical indicators is a spurious result of excessively searching among meaningless predictors. Our out-of-sample tests in Section 3, including a modified version of White’s (2000) reality check, also address data-mining concerns.

We answer the first question using the monthly sentiment-changes index from Baker and Wurgler (2007). This index is based on changes in six sentiment proxies from Baker and Wurgler (2006): trading volume (measured by NYSE turnover); dividend premium (average market-to-book ratios of dividend paying and nonpaying firms); closed-end fund discount; IPO number and first-day returns; equity share of total equity and debt issues by all corporations. The sentiment-changes index, ΔSENT, is the first principal component extracted from the changes in the six sentiment proxies. We use an updated ΔSENT series for 1965:08 to 2010:12. Baker and Wurgler (2007) point out that aggregate market returns and changes in sentiment will be positively correlated if the average stock is affected by sentiment. In support of this notion, they report that the contemporaneous correlation between a capitalization-weighted market return index and ΔSENT is a sizable and statistically significant 0.32 for 1966:01 to 2005:12; the correlation between the equity risk

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17 We thank the anonymous referees for suggesting these two interesting ideas.
18 The updated series is available from Jeffrey Wurgler’s homepage at http://people.stern.nyu.edu/jwurgler/.
premium and ∆SENT is also a sizable and statistically significant 0.28 for the updated 1965:08 to 2010:12 sample.

Because the equity risk premium and ∆SENT are sizably contemporaneously correlated, if an equity risk premium predictor also predicts ∆SENT, this suggests that the variable’s ability to predict the equity risk premium stems in part from its ability to predict changes in sentiment. We investigate this idea using the same predictive regression framework as before, with $r_{t+1}$ replaced by ∆SENT$_{t+1}$ in (1), (10), (12), (13), and (14). Table 3 reports the results. None of the individual macroeconomic variables evinces significant predictive ability in the bivariate predictive regressions in Table 3, Panel A, and the $R^2$ statistics in the third column for these regressions are all less than or equal to 0.37%. The first three principal components extracted from the 14 macroeconomics variables are also insignificant in the predictive regression in Panel B, and the $R^2$ is a paltry 0.07% for this regression. Furthermore, the second through fourth principal components extracted from the entire set of 14 macroeconomic variables and 14 technical indicators, which are strongly related to the macroeconomic variables but not the technical indicators, display no significant predictive ability in Panel C.

In sharp contrast to the macroeconomic variables, the technical indicators exhibit significant predictive ability for ∆SENT both individually and as a group. Twelve of the 14 individual indicators display significant predictive ability in Panel A for the bivariate predictive regressions, with ten of the $R^2$ statistics greater than 0.5%. The first principal component extracted from the 14 technical indicators is a significant predictor of ∆SENT at the 1% level in Panel B, and the $R^2$ is 0.96% for this predictive regression. In addition, the first principal component extracted from the 14 macroeconomic variables and 14 technical indicators taken together, which is heavily influenced by the technical indicators and essentially unaffected by the macroeconomic variables, exhibits significant predictive ability in Panel C. The $R^2$ statistics computed separately for expansions and recessions indicate that the predictive ability of technical indicators in Table 3 is concentrated during recessions, following the pattern for the technical indicators in Table 2. In sum, the differential information useful for predicting the equity risk premium found in technical indicators appears to relate in part to changes in investor sentiment, particularly during recessions.\(^{19}\)

\(^{19}\)Of course, the results in Table 3 alone do not establish whether the changes in sentiment themselves reflect a rational time-varying equity risk premium or irrational fluctuations in investor sentiment (or both). Determining the sources of the changes in investor sentiment requires a full-fledged model of equilibrium returns, which is beyond the scope of the present paper. Also note that the results in Table 3 are similar when we use an adjusted sentiment-changes index constructed as the residual from a regression of ∆SENT on industrial production growth; real growth in durable, nondurable, and services consumption; employment growth; and an NBER recession indicator. This is not surprising, as Baker and Wurgler (2007) report that this adjustment has little effect on the sentiment-changes index.
Turning to the second question, in the spirit of Ferson and Harvey (1999), we estimate a conditional version of the Fama and French (1993) three-factor model:

\[
R_{i,t+1} - R_{f,t+1} = \alpha_{i,t} + \beta_{i,t}^{MKT} MKT_{t+1} + \beta_{i,t}^{SMB} SMB_{t+1} + \beta_{i,t}^{HML} HML_{t+1} + \varepsilon_{i,t+1},
\]  

(17)

where \( R_{i,t+1} \) is the (simple) return on portfolio \( i \), \( R_f \) is the risk-free return, \( MKT \) is the excess market return, \( SMB \) (\( HML \)) is the size (value) premium, and

\[
\alpha_{i,t} = \alpha_{i,0} + \sum_{k=1}^{4} \alpha_{i,k} F_{k,t}^{\text{ALL}},
\]

(18)

\[
\beta_{i,t}^{j} = \beta_{i,0}^{j} + \sum_{k=1}^{4} \beta_{i,k}^{j} F_{k,t}^{\text{ALL}} \text{ for } j = MKT, SMB, HML.
\]

(19)

Equation (17) is a conditional asset pricing model in that it permits time variation in both “alpha” via (18) and the factor exposures via (19). We estimate (17) for ten momentum-sorted portfolios, as well as the “up-minus-down” (UMD) zero-investment momentum portfolio, using data from Kenneth French’s Data Library.\(^{20}\) Momentum portfolios present challenges for the unconditional Fama-French three-factor model (e.g., Fama and French 1996, Carhart 1997), and we examine whether the information in lagged macroeconomic variables and technical indicators, as captured by \( F_{k,t}^{\text{ALL}} \) (\( j = 1, \ldots, 4 \)), enters significantly into a conditional version of the model.

For each of the eleven momentum portfolios, we first test the joint null hypothesis,

\[
\alpha_{i,1} = \beta_{i,1}^{MKT} = \beta_{i,1}^{SMB} = \beta_{i,1}^{HML} = 0.
\]

(20)

Because \( F_{k,t}^{\text{ALL}} \) corresponds closely to the technical indicators, (20) essentially tests the significance of the technical indicators as a group in the conditional asset pricing model. Using heteroskedasticity-robust \( \chi^2 \)-statistics, we reject the restrictions in (20) for ten of the eleven momentum portfolios. Technical indicators thus significantly explain returns in the conditional asset pricing model given by (17) for nearly all portfolios, which provides additional evidence that technical indicators represent genuine economic information.\(^{21}\)

\(^{20}\)The data are available at http://mba.tuck.dartmouth.edu/pages/faculty/ken.french/data_library.html.

\(^{21}\)The complete set of \( \chi^2 \)-statistics is reported in the Online Appendix.
We next test the joint null hypothesis,

\[
\alpha_{i,k} = \beta_{i,k}^{MKT} = \beta_{i,k}^{SMB} = \beta_{i,k}^{HML} = 0 \quad \text{for} \quad k = 2, 3, 4.
\]  

(21)

Because \( \hat{F}_{2,t}^{ALL} \), \( \hat{F}_{3,t}^{ALL} \), and \( \hat{F}_{4,t}^{ALL} \) correspond closely to the macroeconomic variables, (21) tests the significance of the macroeconomic variables as a group. We reject the restrictions in (21) for all eleven momentum portfolios; like technical indicators, macroeconomic variables significantly explain portfolio returns in the conditional asset pricing model. We also test the null,

\[
\alpha_{i,k} = \beta_{i,k}^{MKT} = \beta_{i,k}^{SMB} = \beta_{i,k}^{HML} = 0 \quad \text{for} \quad k = 1, 2, 3, 4,
\]  

(22)

which tests the significance of the technical indicators and macroeconomic variables taken together. We also reject the restrictions in (22) for all eleven portfolios. In accord with our predictive regression results, we thus find that macroeconomic variables and technical indicators both enter significantly in the conditional Fama-French three-factor model.\(^{22}\)

3. Out-of-Sample Analysis

As a robustness check, this section reports out-of-sample forecasting statistics for the 14 macroeconomic variables and 14 technical indicators. The month-\((t + 1)\) out-of-sample equity risk premium forecast based on an individual macroeconomic variable in (1) and data through month \(t\) is given by

\[
\tilde{r}_{t+1} = \hat{\alpha}_{t,i} + \hat{\beta}_{t,i} x_{i,t},
\]  

(23)

where \( \hat{\alpha}_{t,i} \) and \( \hat{\beta}_{t,i} \) are the OLS estimates from regressing \( \{r_{s,t}\}_{s=2}^{t} \) on a constant and \( \{x_{i,s}\}_{s=1}^{t-1} \). We use 1950:12 to 1965:12 as the initial estimation period, so that the forecast evaluation period spans 1966:01 to 2011:12 (552 observations). The length of the initial in-sample estimation period balances having enough observations for reasonably precisely estimating the initial parameters with our desire for a relatively long out-of-sample period for forecast evaluation.\(^{23}\)

\(^{22}\)We also estimated a conditional version of the Fama-French three-factor model that does not permit time variation in the alphas, so that \( \alpha_{i,t} = \alpha_{i,0} \) in (18). The qualitative results are unchanged for tests of relevant versions of (20), (21), and (22).

\(^{23}\)Hansen and Timmermann (2012) show that out-of-sample tests of predictive ability have better size properties when the forecast evaluation period is a relatively large proportion of the available sample, as in our case. Note that we generate forecasts using a recursive (i.e., expanding) window for estimating \( \alpha_{t,i} \) and \( \beta_{t,i} \) in (1). We could also generate forecasts using a rolling window (which drops earlier observations as additional observations become available), in recognition of potential structural instability. Pesaran
The out-of-sample forecast based on an individual technical indicator in (10) is given by

\[ \hat{r}_{t+1} = \hat{\alpha}_{t,i} + \hat{\beta}_{t,i}S_{t,i}, \]  

(24)

where \( \hat{\alpha}_{t,i} \) and \( \hat{\beta}_{t,i} \) are the OLS estimates from regressing \( \{r_s\}_{s=2}^{t} \) on a constant and \( \{S_{t,s}\}_{s=1}^{t-1} \). We also generate out-of-sample forecasts based on principal components, as in (12), (13), and (14):

\[ \hat{r}_{j,t+1} = \hat{\alpha}_t + \sum_{k=1}^{K} \hat{\beta}_{t,k} \hat{F}_{j,t,k,t} \quad \text{for} \quad j = \text{ECON, TECH, or ALL}; \]  

(25)

where \( \hat{F}_{j,t,k,t} \) is the \( k \)th principal component extracted from the 14 macroeconomic variables (\( j = \text{ECON} \)), 14 technical indicators (\( j = \text{TECH} \)), or 14 macroeconomic variables and 14 technical indicators taken together (\( j = \text{ALL} \)), based on data through \( t \); and \( \hat{\alpha}_t \) and \( \hat{\beta}_{t,k} \) (\( k = 1, \ldots, K \)) are the OLS estimates from regressing \( \{r_s\}_{s=2}^{t} \) on a constant and \( \{\hat{F}_{j,t,s}\}_{s=1}^{t-1} \) (\( k = 1, \ldots, K \)).

We compare the forecasts given by (23), (24), and (25) to the historical average forecast:

\[ \hat{r}_{HA,t+1} = \frac{1}{t} \sum_{s=1}^{t} r_s. \]  

(26)

This popular benchmark forecast (e.g., Goyal and Welch 2003, 2008, Campbell and Thompson 2008, Ferreira and Santa-Clara 2011) assumes a constant expected equity risk premium (\( r_{t+1} = \alpha + \epsilon_{t+1} \)). Goyal and Welch (2003, 2008) show that (26) is a very stringent out-of-sample benchmark: predictive regression forecasts based on individual macroeconomic variables typically fail to outperform the historical average.

We analyze forecasts in terms of the Campbell and Thompson (2008) out-of-sample \( R^2 \) (\( R^2_{\text{OS}} \)) and Clark and West (2007) MSFE-adjusted statistics. The \( R^2_{\text{OS}} \) statistic measures the proportional reduction in mean squared forecast error (MSFE) for the predictive regression forecast relative to the historical average. A positive value thus indicates that the predictive regression forecast outperforms the historical average in terms of MSFE, while a negative value signals the opposite. Like their in-sample counterparts, monthly \( R^2_{\text{OS}} \) statistics appear small at first glance, due to the inherently large unpredictable component in stock returns; nevertheless, a monthly \( R^2_{\text{OS}} \) statistic near 0.5% is economically significant (Campbell and Thompson 2008). and Timmermann (2007) and Clark and McCracken (2009), however, show that the optimal estimation window for a quadratic loss function generally includes pre-break data due to the familiar bias-efficiency tradeoff. Although we use a recursive estimation window, we obtain similar results using rolling estimation windows of various sizes.

\(^{24}\)We select \( K \) via the adjusted \( R^2 \) based on data through \( t \).
The MSFE-adjusted statistic tests the null hypothesis that the historical average MSFE is less than or equal to the predictive regression MSFE against the one-sided (upper-tail) alternative hypothesis that the historical average MSFE is greater than the predictive regression MSFE (corresponding to \( H_0: R^2_{OS} \leq 0 \) against \( H_A: R^2_{OS} > 0 \)).

Panel A of Table 4 reports out-of-sample results for bivariate predictive regression forecasts based on individual macroeconomic variables and technical indicators. Only three of the \( R^2_{OS} \) statistics are positive in the third column of Panel A; the vast majority of individual macroeconomic variables thus fail to outperform the historical average benchmark in terms of MSFE. The three positive \( R^2_{OS} \) statistics (for DY, RVOL, and LTR) only range from 0.05% to 0.29%. Nevertheless, the MSFEs for these three predictors are significantly less than the historical average MSFE at conventional levels according to the MSFE-adjusted statistics in the fourth column. It is interesting to note that the MSFE-adjusted statistics indicate that the MSFEs for TBL, LTY, and TMS are significantly less than that of the historical average, despite the negative \( R^2_{OS} \) statistics for these forecasts. Although this result appears strange, it is possible when comparing nested model forecasts (Clark and McCracken 2001, Clark and West 2007, McCracken 2007). Reminiscent of Goyal and Welch (2003, 2008), individual macroeconomic variables display limited out-of-sample predictive ability in Table 4, Panel A. Similarly to the in-sample results in Table 2, a number of macroeconomic variables—including DP, DY, TBL, LTR, and TMS—predict the equity risk premium better during recessions than expansions on an out-of-sample basis.

Overall, individual technical indicators appear to perform as well as, or better than, individual macroeconomic variables in terms of MSFE. All of the \( R^2_{OS} \) statistics are positive in the eleventh column of Table 4, Panel A; each of the technical indicators thus delivers a lower MSFE than the historical average benchmark. Three of the \( R^2_{OS} \) statistics exceed 0.70%, and the MSFEs for six of the technical indicators are significantly less than the historical average MSFE based on the MSFE-adjusted statistics. Again matching the in-sample results, the out-of-sample predictive ability of technical indicators is uniformly stronger for recessions relative to expansions.

\(^{25}\)Clark and West (2007) develop the MSFE-adjusted statistic by modifying the familiar Diebold and Mariano (1995) and West (1996) statistic so that it has an approximately standard normal asymptotic distribution when comparing forecasts from nested models. Comparing a predictive regression forecast to the historical average entails comparing nested models, as the predictive regression model reduces to the constant expected equity risk premium model under the null hypothesis. The MSFE-adjusted statistic accounts for the negative expected difference between the historical average MSFE and predictive regression MSFE under the null, so that it can reject the null even if the \( R^2_{OS} \) statistic is negative.

\(^{26}\)Intuitively, under the null hypothesis that the constant expected equity risk premium model generates the data, the predictive regression model produces a noisier forecast than the historical average benchmark, because it estimates slope parameters with zero population values. We thus expect the benchmark model MSFE to be smaller than the predictive regression model MSFE under the null. The MSFE-adjusted statistic accounts for the negative expected difference between the historical average MSFE and predictive regression MSFE under the null, so that it can reject the null even if the \( R^2_{OS} \) statistic is negative.
To get a sense of potential bias-efficiency tradeoffs in the forecasts, Table 4 also report a decomposition of MSFE into squared-bias and variance components:

\[ \text{MSFE} = (\hat{\epsilon})^2 + \text{Var}(\hat{\epsilon}), \]  

where \( \hat{\epsilon} \) signifies the forecast error, \( (\hat{\epsilon})^2 \) is the squared forecast bias, and \( \text{Var}(\hat{\epsilon}) \) is forecast error variance. The squared bias (error variance) is 0.07 (20.16) for the historical average forecast. DP, DY, EP, DE, and INFL have squared biases well below that of the historical average. The forecast error variances of these five variables, however, exceed that of the historical average, and only DY has a smaller MSFE than the historical average. The squared biases are substantially higher than that of the historical average for RVOL, NTIS, TMS, and DFY, ranging from 0.13 to 0.23. Among these variables, only RVOL has a smaller forecast error variance (and MSFE) than the historical average. The squared biases are much more similar across the technical indicators, and all of them are less than or equal to the historical average squared bias. In addition, the forecast error variances for the technical indicators are all less than or equal to (or only slightly above) that of the historical average. Thus, forecasts based on the technical indicators are generally both less biased and more efficient than the historical average.

Panel B of Table 4 reports out-of-sample results for the principal component predictive regression forecasts based on macroeconomic variables or technical indicators. Although the \( R^2_{\text{OS}} \) is negative for the PC-ECON forecast, its MSFE is significantly less (at the 1% level) than that of the historical average according to the MSFE-adjusted statistic.\(^ {27} \) The \( R^2_{\text{OS}} \) is 0.65% for the PC-TECH forecast, and the MSFE-adjusted statistic indicates that the MSFE for the PC-TECH forecast is significantly below that of the historical average.\(^ {28} \) The PC-ECON and PC-TECH forecasts have smaller squared biases than the historical average. The PC-ECON forecast error variance, however, substantially exceeds that of the historical average; in contrast, the PC-TECH forecast error variance is well below that of the historical average. Both the PC-ECON and PC-TECH forecasts manifest much stronger out-of-sample predictive ability in recessions than in expansions.

We next compare the information content of the PC-ECON and PC-TECH forecasts using encompassing

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\(^{27}\)See footnote 26 for the intuition behind this seemingly strange result.

\(^{28}\)Because the first principal component extracted from the 14 technical indicators loads nearly uniformly on the individual indicators, the PC-TECH forecast is similar to a combination forecast that takes the form of the average of the 14 bivariate predictive regression forecasts based on the technical indicators (Rapach, Strauss, and Zhou 2010). The \( R^2_{\text{OS}} \) for the simple combination forecast is 0.53%; the corresponding MSFE-adjusted statistic is 1.38 (which is significant at the 10% level).
tests. Harvey, Leybourne, and Newbold (1998) develop a statistic for testing the null hypothesis that a given forecast contains all of the relevant information found in a competing forecast (i.e., the given forecast encompasses the competitor) against the alternative that the competing forecast contains relevant information beyond that in the given forecast. We reject the null hypothesis that the PC-ECON forecast encompasses the PC-TECH forecast, as well as the null that the PC-TECH forecast encompasses the PC-ECON (both at the 1% level; the complete results are omitted for brevity). The PC-ECON and PC-TECH forecasts thus fail to encompass each other, indicating that there are gains to using information from macroeconomic variables and technical indicators in conjunction.

In accord with the encompassing test results, the PC-ALL forecast has an $R_{OS}^2$ of 1.79% in Table 4, Panel C, which easily exceeds all of the other $R_{OS}^2$ statistics in Table 4. The PC-ALL MSFE is also significantly less than the historical average MSFE at the 1% level according to the MSFE-adjusted statistic. The squared bias and forecast error variance for the PC-ALL forecast are below the respective values for the historical average; indeed, the PC-ALL forecast error variance is well below that of any of the other forecast error variances. The out-of-sample results in Table 4 thus confirm the in-sample results in Section 2: macroeconomic variables and technical indicators capture different types of information relevant for forecasting the equity risk premium. The $R_{OS}^2$ for the PC-ALL forecast is a very sizable 11.24% for recessions, while it is $-2.80\%$ for expansions, so that the out-of-sample predictive power of the macroeconomic variables and technical indicators taken together is concentrated in recessions.

Figure 7 reveals that the PC-ECON, PC-TECH, and PC-ALL out-of-sample equity risk premium forecasts behave similarly to the in-sample forecasts in Figure 5. The PC-ECON and PC-ALL out-of-sample forecasts are considerably more volatile during the early stages of the forecast evaluation period, however, due to the relatively small samples available for estimating the principal components and predictive regression parameters. The PC-ALL forecast in Figure 7 again exhibits a marked countercyclical pattern.

To control for data mining—which becomes a concern when considering many predictors—we use Clark and McCracken’s (2012) modified version of White’s (2000) reality check. The Clark and McCracken

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$^{29}$The PC-ALL forecast also has a lower MSFE than the constant 0.5% equity risk premium benchmark forecast used by Simin (2008). Rapach, Strauss, and Zhou (2010) show that a combination forecast of the equity risk premium based on individual predictive regressions with macroeconomic variables delivers consistent out-of-sample gains. Using the same approach, we form a combination forecast as the mean of the 14 bivariate predictive regression forecasts in Table 4, Panel A, and its $R_{OS}^2$ is 1.16%. Ferreira and Santa-Clara (2011) propose an intriguing “sum-of-the-parts” equity risk premium forecast as the sum of a 20-year moving average of earnings growth and the current dividend-price ratio (minus the risk-free rate). We compute a sum-of-the-parts forecast, and its $R_{OS}^2$ is 1.32%. The PC-ALL forecast thus appears to be the best-to-date out-of-sample forecast of the equity risk premium.
(2012) reality check is based on a wild fixed-regressor bootstrap and is appropriate for comparing forecasts from multiple models, all of which nest the benchmark model, as in our framework. We use the Clark and McCracken (2012) maxMSFE-$F$ statistic to test the null hypothesis that the historical average MSFE is less than or equal to the minimum MSFE of all the 28 bivariate predictive regression forecasts and three principal component predictive regression forecasts in Table 4. The maxMSFE-$F$ statistic rejects the null that none of the competing forecasts outperforms the historical average, with a bootstrapped $p$-value of 0.03, so that data mining cannot readily explain the significant out-of-sample predictive power of the PC-ALL forecast.\textsuperscript{30}

4. Asset Allocation Exercise

As a final exercise, we measure the economic value of equity risk premium forecasts for a risk-averse investor. Following Campbell and Thompson (2008) and Ferreira and Santa-Clara (2011), among others, we compute the certainty equivalent return (CER) for a mean-variance investor who optimally allocates across equities and risk-free bills using various equity risk premium forecasts. This exercise also addresses the weakness of many existing studies of technical indicators that fail to incorporate risk aversion into the asset allocation decision.

The mean-variance investor’s expected utility can be expressed as

\[ U(R_p) = E(R_p) - \frac{1}{2} \gamma \text{Var}(R_p), \]  

(28)

where $R_p$ is the (simple) return on the investor’s portfolio, $E(R_p)$ is the expected portfolio return, $\text{Var}(R_p)$ is the variance of the portfolio return, and $\gamma$ is the investor’s coefficient of relative risk aversion. At the end of month $t$, the investor optimally allocates the following share of the portfolio to equities during month $t + 1$:

\[ w_t = \left( \frac{1}{\gamma} \right) \left( \frac{\hat{r}_{t+1}}{\hat{\sigma}^2_{t+1}} \right), \]  

(29)

where $\hat{r}_{t+1}$ is a forecast of the (simple) equity risk premium and $\hat{\sigma}^2_{t+1}$ is a forecast of its variance. The share $1 - w_t$ is allocated to risk-free bills, and the month-$(t + 1)$ portfolio return is given by

\[ R_{p,t+1} = w_t r_{t+1} + R_{f,t+1}, \]  

(30)

\textsuperscript{30}Ferson, Sarkissian, and Simin (2003) demonstrate that size distortions related to the Stambaugh bias can exacerbate data-mining problems for in-sample predictive regressions with persistent predictors. Busetti and Marcucci (2012), however, show that out-of-sample tests of predictive ability are not afflicted by size distortions in the presence of persistent predictors, so that the issues raised by Ferson, Sarkissian, and Simin (2003) do not appear of great concern for our out-of-sample analysis.
where $R_{f,t+1}$ is the risk-free return. Following Campbell and Thompson (2008), we assume that the investor uses a five-year moving window of past monthly returns to estimate the variance of the equity risk premium and constrain $w_t$ to lie between 0 and 1.5.31

The CER for the portfolio is

$$\text{CER}_p = \hat{\mu}_p - \frac{1}{2} \gamma \hat{\sigma}^2_p, \tag{31}$$

where $\hat{\mu}_p$ and $\hat{\sigma}^2_p$ are the mean and variance, respectively, for the investor’s portfolio over the forecast evaluation period. The CER can be interpreted as the risk-free rate of return that an investor is willing to accept instead of adopting the given risky portfolio. The CER gain is the difference between the CER for the investor who uses a predictive regression forecast of the equity risk premium based on (23), (24), or (25) and the CER for an investor who uses the historical average forecast given by (26).32 We multiply this difference by 1200, so that it can be interpreted as the annual percentage portfolio management fee that an investor would be willing to pay to have access to the predictive regression forecast instead of the historical average forecast.

The second and ninth columns of Table 5, Panel A present CER gains for an investor with a relative risk coefficient of five who relies on the bivariate predictive regression forecast given by (23) or (24), respectively, instead of the historical average forecast; for the historical average forecast, the table reports the CER level.33 Table 5 also reports additional portfolio performance measures. The monthly Sharpe ratio in the fifth and twelfth columns is the mean portfolio return in excess of the risk-free rate divided by the standard deviation of the excess portfolio return. The sixth and thirteenth columns report average monthly turnover, where monthly turnover is the percentage of wealth traded each month (DeMiguel, Garlappi, Nogales, and Uppal 2009, DeMiguel, Garlappi, and Uppal 2009). For the portfolio based on the historical average forecast, the table gives the average monthly turnover; for the other portfolios, it gives the relative average turnover (average monthly turnover divided by the average monthly turnover for the portfolio based on the historical average). The seventh and final columns report CER gains net of transactions costs, where the costs are calculated using the monthly turnover measures and assuming a proportional transactions cost equal to 50 basis points per transaction (Balduzzi and Lynch 1999).

Table 5 reports that the CER for the portfolio based on the historical average forecast is 3.54% for

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31This imposes realistic portfolio constraints by precluding short sales and preventing more than 50% leverage.
32The investor always uses the same five-year moving window to estimate the equity risk premium variance, so that differences in the portfolio weights are solely due to differences in equity risk premium forecasts.
33We obtain similar results for other reasonable relative risk coefficient values.
1966:01 to 2011:12. The CER gains are positive for nine of the 14 macroeconomic variables in the second column of Table 5, Panel A, with TBL, LTY, LTR, and TMS providing gains of over 100 basis points. In accord with the $R^2_{OS}$ statistics in Table 4, the CER gains are substantially larger for recessions vis-à-vis expansions for many of the macroeconomic variables. Eight of the macroeconomic predictors produce higher Sharpe ratios than that of the historical average, with TMS generating the highest ratio of 0.12. The average turnover is 2.09% for the historical average. Portfolios based on many of the macroeconomic variables turn over approximately three to five times more often than the historical average portfolio, and the LTR portfolio turns over nearly 24 times as much. After accounting for transactions costs, the relatively high turnovers for NTIS, LTR, DFR, and INFL reduce the CER gains from positive to negative values.

The last six columns of Table 5, Panel A reveal that portfolios based on technical indicators generally outperform those based on macroeconomic variables. The CER gains in the ninth column are positive for all of the technical indicators, reaching a maximum of 317 basis points. Again in accord with the $R^2_{OS}$ statistics, the CER gains are uniformly larger during recessions relative to expansions, and the gains for recessions are greater than 1,000 basis points for 10 of the 14 individual technical indicators. Portfolios based on the technical indicators turn over approximately two to five times more often than the historical average portfolio. Despite this turnover, the net-of-transactions-costs CER gains are positive—and as high as 282 basis points—for all of the technical indicators.

Panels B and C of Table 5 report performance measures for portfolios based on the principal component predictive regression forecasts given by (25). PC-ECON delivers a sizable CER gain of 224 basis points in the second column of Panel B, and its Sharpe ratio of 0.10 is twice that of the historical average. The CER gain for PC-ECON is much larger for recessions (1,269 basis points) compared to expansions (9 basis points). Although the PC-ECON portfolio turns over nearly seven times more often than the historical average portfolio, it still improves the net-of-transactions-costs CER by 151 basis points. PC-TECH generates a CER gain of 249 basis points in the ninth column of Panel B, 25 basis points more than PC-ECON, and a Sharpe ratio of 0.10, matching that of PC-ECON. PC-TECH provides substantially larger CER gains for recessions (1,637 basis points) relative to expansions (−29 basis points). Because the PC-TECH portfolio turns over much less than the PC-ECON portfolio, the net-of-transactions-costs CER gain for PC-TECH remains well above 200 basis points.

The performance of PC-ALL in Table 5, Panel C stands out. The CER gain for PC-ALL in the second column of Panel C is more than 170 basis points higher than that of any of the other portfolios in Table 5.
PC-ALL also produces the highest Sharpe ratio, 0.16, and the highest net-of-transactions-costs CER gain, 412 basis points, of all the portfolios. The CER gain accruing to PC-ALL reaches a very sizable 2,621 basis points for recessions compared to 70 basis points for expansions, again in line with the $R^2_{os}$ statistics in Table 4. The asset allocation exercise demonstrates the substantial economic value of combining information from macroeconomic variables and technical indicators.

5. Conclusion

We utilize technical indicators to directly forecast the equity risk premium and compare their performance with that of macroeconomic variables. Our results show that technical indicators exhibit statistically and economically significant in-sample and out-of-sample forecasting power for the monthly equity risk premium, clearly on par with that of well-known macroeconomic variables from the literature. Furthermore, we find that technical indicators and macroeconomic variables capture different types of information relevant for forecasting the equity risk premium; in particular, technical indicators (macroeconomic variables) better detect the typical decline (rise) in the equity risk premium near business-cycle peaks (troughs). In line with this finding, we demonstrate that combining information from both technical indicators and macroeconomic variables produces superior equity risk premium forecasts and offers substantial utility gains to investors by better tracking the substantial countercyclical fluctuations in the equity risk premium.

While numerous theories explain why technical indicators may work (as reviewed in the introduction), little is known about their ability to explain key stylized facts concerning stock market returns, such as the equity risk premium puzzle (i.e., the average equity risk premium appears too large in light of conventional risk considerations). In contrast, more traditional asset pricing models, such as the habit model of Campbell and Cochrane (1999, 2000) and long-run risk model of Bansal and Yaron (2004), can explain important stylized facts, but they leave no role for technical analysis. Given the growing empirical evidence supporting the predictive power of technical indicators, which is in line with the behavior of many practitioners, it appears important to bridge the gap between theoretical models of technical analysis and more traditional asset asset pricing models. Exploring the connections between these two types of models holds the promise of significantly improving our understanding of the economic forces that drive the equity risk premium and cross-section of expected asset returns.
References


Table 1  Summary Statistics, 1950:12 to 2011:12

<table>
<thead>
<tr>
<th>Variable</th>
<th>Mean</th>
<th>Standard deviation</th>
<th>Minimum</th>
<th>Maximum</th>
<th>Autocorrelation</th>
<th>Sharpe ratio</th>
</tr>
</thead>
<tbody>
<tr>
<td>Log equity risk premium</td>
<td>0.47</td>
<td>4.26</td>
<td>-24.84</td>
<td>14.87</td>
<td>0.06</td>
<td>0.11</td>
</tr>
<tr>
<td>DP</td>
<td>-3.49</td>
<td>0.42</td>
<td>-4.52</td>
<td>-2.60</td>
<td>0.99</td>
<td></td>
</tr>
<tr>
<td>DY</td>
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<td>0.42</td>
<td>-4.53</td>
<td>-2.59</td>
<td>0.99</td>
<td></td>
</tr>
<tr>
<td>EP</td>
<td>-2.78</td>
<td>0.44</td>
<td>-4.84</td>
<td>-1.90</td>
<td>0.99</td>
<td></td>
</tr>
<tr>
<td>DE</td>
<td>-0.71</td>
<td>0.30</td>
<td>-1.24</td>
<td>1.38</td>
<td>0.99</td>
<td></td>
</tr>
<tr>
<td>RVOL</td>
<td>0.14</td>
<td>0.05</td>
<td>0.05</td>
<td>0.32</td>
<td>0.96</td>
<td></td>
</tr>
<tr>
<td>BM</td>
<td>0.54</td>
<td>0.25</td>
<td>0.12</td>
<td>1.21</td>
<td>0.99</td>
<td></td>
</tr>
<tr>
<td>NTIS</td>
<td>0.02</td>
<td>0.02</td>
<td>-0.06</td>
<td>0.05</td>
<td>0.98</td>
<td></td>
</tr>
<tr>
<td>TBL</td>
<td>4.67</td>
<td>2.95</td>
<td>0.01</td>
<td>16.30</td>
<td>0.99</td>
<td></td>
</tr>
<tr>
<td>LTY</td>
<td>6.32</td>
<td>2.68</td>
<td>2.21</td>
<td>14.82</td>
<td>0.99</td>
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</tr>
<tr>
<td>LTR</td>
<td>0.56</td>
<td>2.76</td>
<td>-11.24</td>
<td>15.23</td>
<td>0.05</td>
<td></td>
</tr>
<tr>
<td>TMS</td>
<td>1.64</td>
<td>1.42</td>
<td>-3.65</td>
<td>4.55</td>
<td>0.96</td>
<td></td>
</tr>
<tr>
<td>DFY</td>
<td>0.96</td>
<td>0.45</td>
<td>0.32</td>
<td>3.38</td>
<td>0.97</td>
<td></td>
</tr>
<tr>
<td>DFR</td>
<td>0.01</td>
<td>1.38</td>
<td>-9.75</td>
<td>7.37</td>
<td>-0.09</td>
<td></td>
</tr>
<tr>
<td>INFL</td>
<td>0.30</td>
<td>0.35</td>
<td>-1.92</td>
<td>1.79</td>
<td>0.61</td>
<td></td>
</tr>
</tbody>
</table>

Notes. The table reports summary statistics for the log equity risk premium (in percent) and 14 macroeconomic variables. The data are from Amit Goyal’s web page at http://www.hec.unil.ch/agoyal/. The mnemonics are defined as follows: DP = log dividend-price ratio, DY = log dividend yield, EP = log earnings-price ratio, DE = log dividend-payout ratio, RVOL = equity risk premium volatility, BM = book-to-market ratio, NTIS = net equity expansion, TBL = Treasury bill rate (annual %), LTY = long-term bond yield (annual %), LTR = long-term bond return (%), TMS = term spread (annual %), DFY = default yield spread (annual %), DFR = default return spread (%), INFL = inflation rate (%). The Sharpe ratio is the mean of the log equity risk premium divided by its standard deviation.
Table 2 Predictive Regression Estimation Results, 1951:01 to 2011:12

<table>
<thead>
<tr>
<th>Macroeconomic variables</th>
<th>Technical indicators</th>
</tr>
</thead>
<tbody>
<tr>
<td>Predictor</td>
<td>Slope coefficient</td>
</tr>
</tbody>
</table>

**Panel A: Bivariate Predictive Regressions**

<table>
<thead>
<tr>
<th>Predictor</th>
<th>Slope coefficient</th>
<th>$R^2$</th>
<th>$R^2_{\text{EXP}}$</th>
<th>$R^2_{\text{REC}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>DP</td>
<td>0.78 [1.98]</td>
<td>0.58%</td>
<td>0.40%</td>
<td>1.00%</td>
</tr>
<tr>
<td>DY</td>
<td>0.84 [2.13]**</td>
<td>0.67%</td>
<td>0.32%</td>
<td>1.48%</td>
</tr>
<tr>
<td>EP</td>
<td>0.43 [0.97]</td>
<td>0.20%</td>
<td>0.22%</td>
<td>0.14%</td>
</tr>
<tr>
<td>DE</td>
<td>0.59 [0.93]</td>
<td>0.17%</td>
<td>0.09%</td>
<td>0.35%</td>
</tr>
<tr>
<td>RVOL</td>
<td>7.41 [2.45]***</td>
<td>0.73%</td>
<td>0.54%</td>
<td>1.18%</td>
</tr>
<tr>
<td>BM</td>
<td>0.54 [0.75]</td>
<td>0.10%</td>
<td>0.01%</td>
<td>0.29%</td>
</tr>
<tr>
<td>NTIS</td>
<td>0.66 [0.06]</td>
<td>0.00%</td>
<td>0.04%</td>
<td>-0.08%</td>
</tr>
<tr>
<td>TBL</td>
<td>0.11 [1.90]**</td>
<td>0.56%</td>
<td>0.42%</td>
<td>0.90%</td>
</tr>
<tr>
<td>LTY</td>
<td>0.08 [1.25]**</td>
<td>0.23%</td>
<td>0.22%</td>
<td>0.23%</td>
</tr>
<tr>
<td>LTR</td>
<td>0.13 [2.05]**</td>
<td>0.76%</td>
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<td>3.41%</td>
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<td>TMS</td>
<td>0.20 [1.74]**</td>
<td>0.44%</td>
<td>0.03%</td>
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</tr>
<tr>
<td>DFY</td>
<td>0.16 [0.37]</td>
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<td>0.04%</td>
<td>0.00%</td>
</tr>
<tr>
<td>DFR</td>
<td>0.16 [0.89]</td>
<td>0.26%</td>
<td>0.05%</td>
<td>0.74%</td>
</tr>
<tr>
<td>INFL</td>
<td>0.10 [0.18]</td>
<td>0.01%</td>
<td>0.07%</td>
<td>-0.14%</td>
</tr>
<tr>
<td>MA(1,9)</td>
<td>0.67 [1.78]**</td>
<td>0.54%</td>
<td>-0.39%</td>
<td>2.66%</td>
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<tr>
<td>MA(1,12)</td>
<td>0.87 [2.22]**</td>
<td>0.87%</td>
<td>-0.18%</td>
<td>3.27%</td>
</tr>
<tr>
<td>MA(2,9)</td>
<td>0.70 [1.88]**</td>
<td>0.59%</td>
<td>-0.26%</td>
<td>2.53%</td>
</tr>
<tr>
<td>MA(2,12)</td>
<td>0.94 [2.42]***</td>
<td>1.03%</td>
<td>-0.09%</td>
<td>3.58%</td>
</tr>
<tr>
<td>MA(3,9)</td>
<td>0.77 [2.04]**</td>
<td>0.69%</td>
<td>0.03%</td>
<td>2.22%</td>
</tr>
<tr>
<td>MA(3,12)</td>
<td>0.54 [1.39]*</td>
<td>0.34%</td>
<td>-0.12%</td>
<td>1.39%</td>
</tr>
<tr>
<td>MOM(9)</td>
<td>0.55 [1.40]*</td>
<td>0.34%</td>
<td>-0.09%</td>
<td>1.33%</td>
</tr>
<tr>
<td>MOM(12)</td>
<td>0.58 [1.45]*</td>
<td>0.37%</td>
<td>-0.36%</td>
<td>2.04%</td>
</tr>
<tr>
<td>VOL(1,9)</td>
<td>0.68 [1.86]**</td>
<td>0.56%</td>
<td>-0.51%</td>
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</tr>
<tr>
<td>VOL(1,12)</td>
<td>0.89 [2.31]***</td>
<td>0.92%</td>
<td>-0.20%</td>
<td>3.49%</td>
</tr>
<tr>
<td>VOL(2,9)</td>
<td>0.74 [2.02]**</td>
<td>0.67%</td>
<td>-0.17%</td>
<td>2.58%</td>
</tr>
<tr>
<td>VOL(2,12)</td>
<td>0.74 [1.94]**</td>
<td>0.65%</td>
<td>-0.04%</td>
<td>2.21%</td>
</tr>
<tr>
<td>VOL(3,9)</td>
<td>0.48 [1.27]</td>
<td>0.27%</td>
<td>-0.17%</td>
<td>1.29%</td>
</tr>
<tr>
<td>VOL(3,12)</td>
<td>0.85 [2.25]***</td>
<td>0.85%</td>
<td>0.21%</td>
<td>2.30%</td>
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**Panel B: Principal Component Predictive Regressions**

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<th>Predictor</th>
<th>Slope coefficient</th>
<th>$R^2$</th>
<th>$R^2_{\text{EXP}}$</th>
<th>$R^2_{\text{REC}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$F^\text{ECON}_1$</td>
<td>0.04 [0.48]</td>
<td>1.18%</td>
<td>0.79%</td>
<td>2.07%</td>
</tr>
<tr>
<td>$F^\text{ECON}_2$</td>
<td>0.07 [0.61]</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$F^\text{ECON}_3$</td>
<td>0.31 [2.48]***</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$F^\text{TECH}_1$</td>
<td>0.12 [2.12]**</td>
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</table>

**Panel C: Principal Component Predictive Regression, All Predictors Taken Together**

<table>
<thead>
<tr>
<th>Predictor</th>
<th>Slope coefficient</th>
<th>$R^2$</th>
<th>$R^2_{\text{EXP}}$</th>
<th>$R^2_{\text{REC}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$F^\text{ALL}_1$</td>
<td>0.11 [1.98]**</td>
<td>2.02%</td>
<td>0.29%</td>
<td>5.95%</td>
</tr>
<tr>
<td>$F^\text{ALL}_2$</td>
<td>0.08 [0.93]</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$F^\text{ALL}_3$</td>
<td>0.18 [1.51]*</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$F^\text{ALL}_4$</td>
<td>0.26 [2.30]***</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Notes. Panel A reports estimation results for the bivariate predictive regression model,

$$r_{t+1} = \alpha_i + \beta_i q_{i,t} + \epsilon_{i,t+1},$$

where $r_{t+1}$ is the log equity risk premium (in percent) and $q_{i,t}$ is one of the 14 macroeconomic variables (14 technical indicators) given in the first (sixth) column. Panels B and C report estimation results for a predictive regression model based on principal components,

$$r_{t+1} = \alpha + \sum_{k=1}^{K} \beta_k \hat{F}^j_{k,t} + \epsilon_{t+1},$$

where $\hat{F}^j_{k,t}$ is the $k$th principal component extracted from the 14 macroeconomic variables ($j = \text{ECON}$), 14 technical indicators ($j = \text{TECH}$), or the 14 macroeconomic variables and 14 technical indicators taken together ($j = \text{ALL}$). $K$ is selected via the adjusted $R^2$. The brackets to the immediate right of the estimated slope coefficients report heteroskedasticity-consistent $t$-statistics; *, **, and *** indicate significance at the 10%, 5%, and 1% levels, respectively, based on one-sided (upper-tail) wild bootstrapped $p$-values; 0.00 indicates less than 0.005 in absolute value. The $R^2$ statistics in the third and eighth columns are computed for the full sample. The $R^2_{\text{EXP}}$ ($R^2_{\text{REC}}$) statistics in the fourth and ninth (fifth and tenth) columns are computed for NBER-dated business-cycle expansions (recessions), as given by (11) in the text.
Table 3  Predictive Regression Estimation Results for the Sentiment-Changes Index, 1965:08 to 2010:12

<table>
<thead>
<tr>
<th>Macroeconomic variables</th>
<th>Slope coefficient</th>
<th>$R^2$</th>
<th>$R^2_{\text{EXP}}$</th>
<th>$R^2_{\text{REC}}$</th>
<th>Technical indicators</th>
<th>Slope coefficient</th>
<th>$R^2$</th>
<th>$R^2_{\text{EXP}}$</th>
<th>$R^2_{\text{REC}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Predictor</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>Predictor</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>DP</td>
<td>0.12 [0.92]</td>
<td>0.26%</td>
<td>0.38%</td>
<td>−0.25%</td>
<td>MA(1,9)</td>
<td>0.20 [2.26]**</td>
<td>0.94%</td>
<td>−0.04%</td>
<td>4.94%</td>
</tr>
<tr>
<td>DY</td>
<td>0.15 [1.10]</td>
<td>0.37%</td>
<td>0.45%</td>
<td>0.08%</td>
<td>MA(1,12)</td>
<td>0.24 [2.48]**</td>
<td>1.19%</td>
<td>0.24%</td>
<td>5.07%</td>
</tr>
<tr>
<td>EP</td>
<td>0.09 [0.83]</td>
<td>0.17%</td>
<td>0.51%</td>
<td>−1.25%</td>
<td>MA(2,9)</td>
<td>0.16 [1.75]**</td>
<td>0.56%</td>
<td>−0.11%</td>
<td>3.27%</td>
</tr>
<tr>
<td>DE</td>
<td>0.02 [0.15]</td>
<td>0.00%</td>
<td>−0.05%</td>
<td>0.23%</td>
<td>MA(2,12)</td>
<td>0.26 [2.83]**</td>
<td>1.47%</td>
<td>0.62%</td>
<td>4.95%</td>
</tr>
<tr>
<td>RVOL</td>
<td>−0.41 [−0.55]</td>
<td>0.05%</td>
<td>0.16%</td>
<td>−0.40%</td>
<td>MA(3,9)</td>
<td>0.11 [1.25]</td>
<td>0.28%</td>
<td>−0.22%</td>
<td>2.31%</td>
</tr>
<tr>
<td>BM</td>
<td>0.19 [1.06]</td>
<td>0.27%</td>
<td>0.55%</td>
<td>−0.86%</td>
<td>MA(3,12)</td>
<td>0.14 [1.50]*</td>
<td>0.42%</td>
<td>0.06%</td>
<td>1.87%</td>
</tr>
<tr>
<td>NTIS</td>
<td>−0.27 [−0.14]</td>
<td>0.00%</td>
<td>0.05%</td>
<td>−0.18%</td>
<td>MOM(9)</td>
<td>0.19 [2.01]**</td>
<td>0.75%</td>
<td>0.35%</td>
<td>2.35%</td>
</tr>
<tr>
<td>TBL</td>
<td>0.02 [1.13]</td>
<td>0.20%</td>
<td>−0.13%</td>
<td>1.56%</td>
<td>MOM(12)</td>
<td>0.20 [2.15]**</td>
<td>0.84%</td>
<td>0.40%</td>
<td>2.64%</td>
</tr>
<tr>
<td>LTY</td>
<td>0.02 [1.20]</td>
<td>0.24%</td>
<td>0.25%</td>
<td>0.22%</td>
<td>VOL(1,9)</td>
<td>0.17 [1.88]**</td>
<td>0.63%</td>
<td>−0.02%</td>
<td>3.27%</td>
</tr>
<tr>
<td>LTR</td>
<td>−0.01 [−0.63]</td>
<td>0.07%</td>
<td>0.04%</td>
<td>0.17%</td>
<td>VOL(1,12)</td>
<td>0.18 [1.93]**</td>
<td>0.70%</td>
<td>0.14%</td>
<td>2.97%</td>
</tr>
<tr>
<td>TMS</td>
<td>0.01 [0.23]</td>
<td>0.01%</td>
<td>−0.13%</td>
<td>0.57%</td>
<td>VOL(2,9)</td>
<td>0.19 [2.10]*</td>
<td>0.86%</td>
<td>0.31%</td>
<td>3.07%</td>
</tr>
<tr>
<td>DFY</td>
<td>0.07 [0.77]</td>
<td>0.12%</td>
<td>−0.24%</td>
<td>1.59%</td>
<td>VOL(2,12)</td>
<td>0.20 [2.18]**</td>
<td>0.92%</td>
<td>0.57%</td>
<td>2.35%</td>
</tr>
<tr>
<td>DFR</td>
<td>−0.04 [−1.15]</td>
<td>0.30%</td>
<td>0.76%</td>
<td>−1.56%</td>
<td>VOL(3,9)</td>
<td>0.12 [1.23]</td>
<td>0.31%</td>
<td>0.10%</td>
<td>1.16%</td>
</tr>
<tr>
<td>INFL</td>
<td>0.05 [0.45]</td>
<td>0.04%</td>
<td>−0.08%</td>
<td>0.51%</td>
<td>VOL(3,12)</td>
<td>0.15 [1.54]*</td>
<td>0.47%</td>
<td>0.19%</td>
<td>1.60%</td>
</tr>
</tbody>
</table>

Panel A: Bivariate Predictive Regressions

Panel B: Principal Component Predictive Regressions

<table>
<thead>
<tr>
<th>Predictor</th>
<th>Slope coefficient</th>
<th>$R^2$</th>
<th>$R^2_{\text{EXP}}$</th>
<th>$R^2_{\text{REC}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\hat{F}_1^{\text{ECON}}$</td>
<td>0.01 [0.42]</td>
<td>0.07%</td>
<td>0.00%</td>
<td>0.38%</td>
</tr>
<tr>
<td>$\hat{F}_2^{\text{ECON}}$</td>
<td>0.01 [0.32]</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\hat{F}_3^{\text{ECON}}$</td>
<td>0.01 [0.25]</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\hat{F}_1^{\text{TECH}}$</td>
<td>0.03 [2.31]**</td>
<td>0.96%</td>
<td>0.28%</td>
<td>3.72%</td>
</tr>
</tbody>
</table>

Panel C: Principal Component Predictive Regression, All Predictors Taken Together

<table>
<thead>
<tr>
<th>Predictor</th>
<th>Slope coefficient</th>
<th>$R^2$</th>
<th>$R^2_{\text{EXP}}$</th>
<th>$R^2_{\text{REC}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\hat{F}_1^{\text{ALL}}$</td>
<td>0.03 [2.15]**</td>
<td>1.11%</td>
<td>0.10%</td>
<td>5.21%</td>
</tr>
<tr>
<td>$\hat{F}_2^{\text{ALL}}$</td>
<td>0.02 [0.93]</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\hat{F}_3^{\text{ALL}}$</td>
<td>0.02 [0.61]</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\hat{F}_4^{\text{ALL}}$</td>
<td>0.01 [0.26]</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Notes. Panel A reports estimation results for the bivariate predictive regression model,

$$\Delta \text{SENT}_{t+1} = \alpha + \beta_t q_{i,t} + \epsilon_{t+1},$$

where $\Delta \text{SENT}_{t+1}$ is the sentiment-changes index and $q_{i,t}$ is one of the 14 macroeconomic variables (14 technical indicators) given in the first (sixth) column. Panels B and C report estimation results for a predictive regression model based on principal components,

$$\Delta \text{SENT}_{t+1} = \alpha + \sum_{k=1}^{K} \beta_k \hat{F}_k^{1} + \epsilon_{t+1},$$

where $\hat{F}_k^{1}$ is the $k$th principal component extracted from the 14 macroeconomic variables ($j = \text{ECON}$), 14 technical indicators ($j = \text{TECH}$), or the 14 macroeconomic variables and 14 technical indicators taken together ($j = \text{ALL}$). The brackets to the immediate right of the estimated slope coefficients report heteroskedasticity-consistent $t$-statistics; ‘*’, ‘**’, and ‘***’ indicate significance at the 10%, 5%, and 1% levels, respectively, based on one-sided (upper-tail) wild bootstrapped $p$-values; 0.00 indicates less than 0.005 in absolute value. The $R^2$ statistics in the third and eighth columns are computed for the full sample. The $R^2_{\text{EXP}}$ ($R^2_{\text{REC}}$) statistics in the fourth and ninth (fifth and tenth) columns are computed for NBER-dated business-cycle expansions (recessions), as given by (11) in the text.
Table 4  Out-of-Sample Forecasting Results, 1966:01 to 2011:12

<table>
<thead>
<tr>
<th>Macroeconomic variables</th>
<th>Technical indicators</th>
</tr>
</thead>
<tbody>
<tr>
<td>Predictor</td>
<td>MSFE</td>
</tr>
<tr>
<td>HA</td>
<td>20.23</td>
</tr>
</tbody>
</table>

Panel A: Bivariate Predictive Regression Forecasts

| Predictor | MSFE | $R^2_{OS}$ | $R^2_{OS, \text{adjusted}}$ | $R^2_{OS, \text{expansion}}$ | $R^2_{OS, \text{recession}}$ | (\hat{\epsilon})^2 | Var(\hat{\epsilon}) | Predictor | MSFE | $R^2_{OS}$ | $R^2_{OS, \text{adjusted}}$ | $R^2_{OS, \text{expansion}}$ | $R^2_{OS, \text{recession}}$ | (\hat{\epsilon})^2 | Var(\hat{\epsilon}) |
| DP         | 20.23 | -0.02%  | 1.27 | -0.79% | 1.55% | 0.00 | 20.23 | MA(1,9) | 20.18 | 0.24% | 0.98 | -0.81% | 2.39% | 0.05 | 20.13 |
| DY         | 20.22 | 0.05% | 1.41* | -1.08% | 2.39% | 0.00 | 20.22 | MA(1,12) | 20.10 | 0.63% | 1.52* | -0.66% | 3.30% | 0.05 | 20.05 |
| EP         | 20.35 | -0.58% | 0.02 | -0.29% | -1.18% | 0.02 | 20.32 | MA(2,9) | 20.16 | 0.32% | 1.16 | -0.75% | 2.54% | 0.05 | 20.11 |
| DE         | 20.39 | -0.78% | 0.73 | -1.59% | 0.89% | 0.00 | 20.39 | MA(2,12) | 20.07 | 0.78% | 1.69** | -0.56% | 3.53% | 0.05 | 20.02 |
| RVOL       | 20.19 | 0.19% | 1.59* | 0.02% | 0.53% | 0.13 | 20.06 | MA(3,9) | 20.15 | 0.41% | 1.41* | -0.82% | 2.94% | 0.05 | 20.09 |
| BM         | 20.48 | -1.23% | -1.27 | -0.22% | -3.31% | 0.08 | 20.40 | MA(3,12) | 20.21 | 0.08% | 0.63 | -0.46% | 1.19% | 0.06 | 20.16 |
| NTIS       | 20.43 | -0.97% | 0.38 | -0.21% | -2.54% | 0.17 | 20.26 | MOM(9) | 20.21 | 0.11% | 0.61 | -0.49% | 1.34% | 0.06 | 20.15 |
| TBL        | 20.46 | -1.12% | 2.04** | -2.35% | 1.42% | 0.08 | 20.38 | MOM(12) | 20.20 | 0.15% | 0.69 | -0.45% | 1.39% | 0.06 | 20.14 |
| LTY        | 20.42 | -0.95% | 1.56* | -1.88% | 0.98% | 0.09 | 20.33 | VOL(1,9) | 20.15 | 0.40% | 1.25 | -0.67% | 2.61% | 0.06 | 20.09 |
| LTR        | 20.17 | 0.29% | 2.00** | -1.95% | 4.90% | 0.10 | 20.07 | VOL(1,12) | 20.07 | 0.80% | 1.76** | -0.24% | 2.94% | 0.05 | 20.02 |
| TMS        | 20.43 | -0.99% | 2.08** | -3.44% | 4.06% | 0.23 | 20.20 | VOL(2,9) | 20.14 | 0.44% | 1.36* | -0.01% | 1.37% | 0.07 | 20.07 |
| DFY        | 20.36 | -0.64% | -0.34 | -0.55% | -0.83% | 0.13 | 20.23 | VOL(2,12) | 20.16 | 0.33% | 1.12 | 0.16% | 0.68% | 0.06 | 20.10 |
| DFR        | 20.32 | -0.46% | 0.05 | 0.33% | -2.06% | 0.06 | 20.26 | VOL(3,9) | 20.23 | 0.01% | 0.46 | -0.41% | 0.89% | 0.06 | 20.17 |
| INFL       | 20.32 | -0.45% | 0.32 | -0.08% | -1.21% | 0.02 | 20.30 | VOL(3,12) | 20.09 | 0.71% | 1.68** | 0.13% | 1.90% | 0.05 | 20.04 |

Panel B: Principal Component Predictive Regression Forecasts

| Predictor | MSFE | $R^2_{OS}$ | $R^2_{OS, \text{adjusted}}$ | $R^2_{OS, \text{expansion}}$ | $R^2_{OS, \text{recession}}$ | (\hat{\epsilon})^2 | Var(\hat{\epsilon}) | Predictor | MSFE | $R^2_{OS}$ | $R^2_{OS, \text{adjusted}}$ | $R^2_{OS, \text{expansion}}$ | $R^2_{OS, \text{recession}}$ | (\hat{\epsilon})^2 | Var(\hat{\epsilon}) |
| PC-ECON    | 20.40 | -0.86% | 2.58*** | -3.95% | 5.51% | 0.02 | 20.38 | PC-TECH | 20.10 | 0.65% | 1.46** | -0.42% | 2.84% | 0.05 | 20.04 |

Panel C: Principal Component Predictive Regression Forecasts, All Predictors Taken Together

| Predictor | MSFE | $R^2_{OS}$ | $R^2_{OS, \text{adjusted}}$ | $R^2_{OS, \text{expansion}}$ | $R^2_{OS, \text{recession}}$ | (\hat{\epsilon})^2 | Var(\hat{\epsilon}) | Predictor | MSFE | $R^2_{OS}$ | $R^2_{OS, \text{adjusted}}$ | $R^2_{OS, \text{expansion}}$ | $R^2_{OS, \text{recession}}$ | (\hat{\epsilon})^2 | Var(\hat{\epsilon}) |
| PC-ALL     | 19.87 | 1.79% | 3.28*** | -2.80% | 11.24% | 0.04 | 19.83 |

Notes. The historical average (HA) forecast is given by

$$\hat{r}_{t+1}^{HA} = \frac{1}{t} \sum_{s=1}^{t} r_s,$$

where $r_s$ is the log equity risk premium (in percent). Each bivariate predictive regression forecast in Panel A is given by

$$\hat{r}_{t+1} = \hat{\alpha}_t + \hat{\beta}_t q_{t,t},$$
where \(q_{i,t}\) is one of the 14 macroeconomic variables (14 technical indicators) given in the first (ninth) column and \(\hat{\alpha}_{t,i}\) and \(\hat{\beta}_{t,i}\) are the OLS estimates computed from regressing \(\{r_{s}\}_{s=1}^{T}\) on a constant and \(\{q_{i,s}\}_{s=1}^{T-1}\). The PC-ECON, PC-TECH, and PC-ALL forecasts in Panels B and C are given by

\[
\hat{r}_{t+1}^{j} = \hat{\alpha}_{t} + \sum_{k=1}^{K} \hat{\beta}_{t,k} \hat{F}_{1:t,k}^{j} \quad \text{for \ } j = \text{ECON, TECH, or ALL;}
\]

where \(\hat{F}_{1:t,k}^{j}\) is the \(k\)th principal component extracted from the 14 macroeconomic variables \((j = \text{ECON})\), 14 technical indicators \((j = \text{TECH})\), or 14 macroeconomic variables and 14 technical indicators taken together \((j = \text{ALL})\), based on data through \(t\); and \(\hat{\alpha}_{t}\) and \(\hat{\beta}_{t,k} (k = 1, \ldots, K)\) are the OLS estimates computed from regressing \(\{r_{s}\}_{s=2}^{T}\) on a constant and \(\{\hat{F}_{1:t,k}^{j}\}_{s=1}^{T-1}\) \((k = 1, \ldots, K)\). \(K\) is selected via the adjusted \(R^2\) based on data through \(t\). MSFE is the mean squared forecast error. \(R_{OS}^2\) measures the reduction in MSFE for the competing forecast given in the first or ninth column relative to the historical average forecast. \textit{MSFE-adjusted} is the Clark and West (2007) statistic for testing the null hypothesis that the historical average forecast MSFE is less than or equal to the competing forecast MSFE against the one-sided (upper-tail) alternative hypothesis that the historical average forecast MSFE is greater than the competing forecast MSFE; \(*\), \(\ast\), and \(\ast\ast\ast\) indicate significance at the 10%, 5%, and 1% levels, respectively; 0.00 indicates less than 0.005 in absolute value. \(R_{OS}^2\) statistics are also reported separately for NBER-dated expansions and recessions. \((\hat{e})^2\) and \(\text{VAR}(\hat{e})\) are the squared forecast bias and forecast error variance, respectively.
### Table 5  Portfolio Performance Measures, 1966:01 to 2011:12

<table>
<thead>
<tr>
<th>Macroeconomic variables</th>
<th>Δ (ann.)</th>
<th>Δ (ann.), expansion</th>
<th>Δ (ann.), recession</th>
<th>Sharpe ratio</th>
<th>Relative average turnover</th>
<th>Δ (ann.), cost = 50bps</th>
<th>Technical indicators</th>
<th>Δ (ann.)</th>
<th>Δ (ann.), expansion</th>
<th>Δ (ann.), recession</th>
<th>Sharpe ratio</th>
<th>Relative average turnover</th>
<th>Δ (ann.), cost = 50bps</th>
</tr>
</thead>
<tbody>
<tr>
<td>Predictor</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>Predictor</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>HA</td>
<td>3.54%</td>
<td></td>
<td></td>
<td>0.05</td>
<td>2.09%</td>
<td>3.40%</td>
<td>MA(1,9)</td>
<td>1.69%</td>
<td>-0.51%</td>
<td>12.69%</td>
<td>0.08</td>
<td>4.40%</td>
<td>1.22%</td>
</tr>
<tr>
<td>Panel A: Bivariate predictive regression forecasts</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>DP</td>
<td>-0.26%</td>
<td>-0.98%</td>
<td>2.94%</td>
<td>0.03</td>
<td>2.17</td>
<td>-0.38%</td>
<td>MA(1,12)</td>
<td>2.91%</td>
<td>-0.27%</td>
<td>18.91%</td>
<td>0.11</td>
<td>3.94%</td>
<td>2.51%</td>
</tr>
<tr>
<td>DY</td>
<td>0.27%</td>
<td>-1.13%</td>
<td>6.89%</td>
<td>0.04</td>
<td>3.05</td>
<td>0.02%</td>
<td>MA(2,9)</td>
<td>2.08%</td>
<td>-0.49%</td>
<td>14.08%</td>
<td>0.09</td>
<td>4.48%</td>
<td>1.63%</td>
</tr>
<tr>
<td>EP</td>
<td>0.42%</td>
<td>-0.01%</td>
<td>2.43%</td>
<td>0.05</td>
<td>1.72</td>
<td>0.34%</td>
<td>MA(2,12)</td>
<td>3.17%</td>
<td>-0.07%</td>
<td>19.17%</td>
<td>0.12</td>
<td>3.62%</td>
<td>2.82%</td>
</tr>
<tr>
<td>DE</td>
<td>-0.19%</td>
<td>-1.26%</td>
<td>4.99%</td>
<td>0.04</td>
<td>2.17</td>
<td>-0.34%</td>
<td>MA(3,9)</td>
<td>2.54%</td>
<td>-0.37%</td>
<td>17.54%</td>
<td>0.11</td>
<td>4.60%</td>
<td>2.08%</td>
</tr>
<tr>
<td>RVOL</td>
<td>-0.52%</td>
<td>-0.11%</td>
<td>-2.97%</td>
<td>0.08</td>
<td>4.20</td>
<td>-0.90%</td>
<td>MA(3,12)</td>
<td>1.40%</td>
<td>-0.39%</td>
<td>10.40%</td>
<td>0.08</td>
<td>2.69%</td>
<td>1.18%</td>
</tr>
<tr>
<td>BM</td>
<td>-1.26%</td>
<td>-0.16%</td>
<td>-6.69%</td>
<td>0.03</td>
<td>2.52</td>
<td>-1.45%</td>
<td>MOM(9)</td>
<td>1.38%</td>
<td>-0.41%</td>
<td>10.38%</td>
<td>0.07</td>
<td>2.58%</td>
<td>1.16%</td>
</tr>
<tr>
<td>NTIS</td>
<td>0.15%</td>
<td>0.65%</td>
<td>-2.30%</td>
<td>0.08</td>
<td>3.52</td>
<td>-0.18%</td>
<td>MOM(12)</td>
<td>1.32%</td>
<td>-0.40%</td>
<td>9.32%</td>
<td>0.07</td>
<td>2.19%</td>
<td>1.16%</td>
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<tr>
<td>TBL</td>
<td>1.62%</td>
<td>0.76%</td>
<td>5.81%</td>
<td>0.08</td>
<td>1.52</td>
<td>1.56%</td>
<td>VOL(1,9)</td>
<td>1.61%</td>
<td>-0.72%</td>
<td>13.61%</td>
<td>0.08</td>
<td>5.21%</td>
<td>1.05%</td>
</tr>
<tr>
<td>LTY</td>
<td>1.65%</td>
<td>0.48%</td>
<td>7.40%</td>
<td>0.07</td>
<td>1.03</td>
<td>1.65%</td>
<td>VOL(1,12)</td>
<td>2.63%</td>
<td>-0.26%</td>
<td>17.63%</td>
<td>0.11</td>
<td>4.59%</td>
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</tr>
<tr>
<td>LTR</td>
<td>1.07%</td>
<td>-0.63%</td>
<td>9.17%</td>
<td>0.09</td>
<td>23.94</td>
<td>-1.87%</td>
<td>VOL(2,9)</td>
<td>1.48%</td>
<td>-0.07%</td>
<td>9.48%</td>
<td>0.08</td>
<td>2.94%</td>
<td>1.23%</td>
</tr>
<tr>
<td>TMS</td>
<td>1.88%</td>
<td>0.42%</td>
<td>8.95%</td>
<td>0.12</td>
<td>4.45</td>
<td>1.44%</td>
<td>VOL(2,12)</td>
<td>1.32%</td>
<td>0.10%</td>
<td>7.32%</td>
<td>0.08</td>
<td>2.40%</td>
<td>1.13%</td>
</tr>
<tr>
<td>DFY</td>
<td>-0.82%</td>
<td>-0.19%</td>
<td>-4.01%</td>
<td>0.05</td>
<td>2.70</td>
<td>-1.03%</td>
<td>VOL(3,9)</td>
<td>0.71%</td>
<td>-0.42%</td>
<td>6.71%</td>
<td>0.06</td>
<td>2.52%</td>
<td>0.52%</td>
</tr>
<tr>
<td>DFR</td>
<td>0.26%</td>
<td>0.66%</td>
<td>-1.68%</td>
<td>0.06</td>
<td>10.16</td>
<td>-0.91%</td>
<td>VOL(3,12)</td>
<td>2.22%</td>
<td>-0.05%</td>
<td>13.22%</td>
<td>0.10</td>
<td>2.80%</td>
<td>1.99%</td>
</tr>
<tr>
<td>INFL</td>
<td>0.38%</td>
<td>0.03%</td>
<td>2.13%</td>
<td>0.06</td>
<td>7.77</td>
<td>-0.49%</td>
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<tr>
<td>Panel B: Principal Component Predictive Regression Forecasts</td>
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<tr>
<td>PC-ECON</td>
<td>2.24%</td>
<td>0.09%</td>
<td>12.69%</td>
<td>0.10</td>
<td>6.73</td>
<td>1.51%</td>
<td>PC-TECH</td>
<td>2.49%</td>
<td>-0.29%</td>
<td>16.37%</td>
<td>0.10</td>
<td>3.58%</td>
<td>2.15%</td>
</tr>
<tr>
<td>Panel C: Principal Component Predictive Regression Forecasts, All Predictors Taken Together</td>
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<tr>
<td>PC-ALL</td>
<td>4.94%</td>
<td>0.70%</td>
<td>26.21%</td>
<td>0.16</td>
<td>7.51</td>
<td>4.12%</td>
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</tbody>
</table>

Notes. The table reports portfolio performance measures for a mean-variance investor with relative risk aversion coefficient of five who allocates monthly between equities and risk-free bills using either an historical average (HA) or predictive regression equity risk premium forecast. Each forecast in Panel A is based on one of the 14 macroeconomic variables (14 technical indicators) given in the first (eighth) column. The forecasts in Panels B and C are based on the 14 macroeconomic variables (PC-ECON), 14 technical indicators (PC-TECH), or all 14 macroeconomic variables and 14 technical indicators taken together (PC-ALL). Δ is the annualized certainty equivalent return (CER) gain for an investor who uses the predictive regression forecast instead of the historical average forecast; for the historical average forecast, the table reports the CER level. Δ statistics are also reported separately for NBER-dated expansions and recessions. Relative average turnover is the average turnover for the portfolio based on the predictive regression forecast divided by the average turnover for the portfolio based on the historical average forecast; for the historical average forecast, the table reports the average turnover level. Δ, cost = 50bps is the CER gain assuming a proportional transactions cost of 50 basis points per transaction.
Figure 1  Principal Components Extracted From 14 Macroeconomic Variables and 14 Technical Indicators, 1950:12 to 2011:12

Notes. Panels A through C depict the first three principal components, respectively, extracted from 14 macroeconomic variables. Panel D depicts the first principal component extracted from 14 technical indicators. Autocorrelations for the principal components are reported in the upper right corner of the panels. Vertical bars depict NBER-dated recessions.
Figure 2  Loadings on Principal Components Extracted From 14 Macroeconomic Variables and 14 Technical Indicators, 1950:12 to 2011:12

Notes. Panels A through C depict loadings for 14 individual macroeconomic variables on the first three principal components, respectively, extracted from the 14 macroeconomic variables. Panel D depicts loadings for 14 technical indicators on the first principal component extracted from the 14 technical indicators.
Figure 3  Principal Components Extracted From 14 Macroeconomic Variables and 14 Technical Indicators Taken Together, 1950:12 to 2011:12

Notes. Panels A through D depict the first four principal components, respectively, extracted from 14 macroeconomic variables and 14 technical indicators taken together. Autocorrelations for the principal components are reported in the upper right corner of the panels. Vertical bars depict NBER-dated recessions.
Figure 4  Loadings on Principal Components Extracted From 14 Macroeconomic Variables and 14 Technical Indicators Taken Together, 1950:12 to 2011:12

Notes. Panels A through D depict loadings for 14 macroeconomic variables and 14 technical indicators on the first four principal components, respectively, extracted from the 14 macroeconomic variables and 14 technical indicators taken together.
Figure 5  In-Sample Log Equity Risk Premium Forecasts Based on 14 Macroeconomic Variables and 14 Technical Indicators, 1951:01 to 2011:12

A. Principal component forecast based on macroeconomic variables

B. Principal component forecast based on technical indicators

C. Principal component forecast based on macroeconomic variables and technical indicators taken together

Notes. Black lines delineate monthly log equity risk premium forecasts (in percent); gray lines delineate the average log equity risk premium over the sample. Panel A (B) depicts the forecast for a predictive regression model with a constant and the first three principal components extracted from 14 macroeconomic variables (first principal component extracted from 14 technical indicators) serving as regressors. Panel C depicts the forecast for a predictive regression model with a constant and the first four principal components extracted from the 14 macroeconomic variables and 14 technical indicators taken together serving as regressors. Vertical bars depict NBER-dated recessions.
Figure 6  Average Behavior of the Log Equity Risk Premium and Forecasts Around Business-Cycle Peaks and Troughs, 1951:01 to 2011:12

Notes. Panel A (E) depicts the average change in the monthly log equity risk premium (in percent) around a business-cycle peak (trough). Panel B (F) depicts the average change in an in-sample forecast based on 14 macroeconomic variables around a peak (trough). Panel C (G) depicts the average change in an in-sample forecast based on 14 technical indicators around a peak (trough). Panel D (H) depicts the average change in an in-sample forecast based on the 14 macroeconomic variables and 14 technical indicators taken together around a peak (trough). Average changes are reported for the four months preceding, month of, and two months following a peak or trough. Bands indicate 90% confidence intervals.
Figure 7  Out-of-Sample Log Equity Risk Premium Forecasts Based on 14 Macroeconomic Variables and 14 Technical Indicators, 1966:01 to 2011:12

A. Principal component forecast based on macroeconomic variables

B. Principal component forecast based on technical indicators

C. Principal component forecast based on macroeconomic variables and technical indicators taken together

Notes. Black lines delineate monthly principal component log equity risk premium forecasts (in percent); gray lines delineate the historical average log equity risk premium forecast. Panel A (B) depicts the forecast for a predictive regression model with a constant and up to the first three principal components (first principal component) extracted from 14 macroeconomic variables (14 technical indicators) serving as regressors. Panel C depicts the forecast for a predictive regression model with a constant and up to the first four principal components extracted from the 14 macroeconomic variables and 14 technical indicators taken together serving as regressors. Vertical bars depict NBER-dated recessions.