Changes in the Second-Moment Properties of Disaggregated Capital Flows

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Changes in the Second-Moment Properties of Disaggregated Capital Flows*

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Abstract

Using formal statistical tests, we detect (i) significant volatility increases for various types of capital flows for a period of changes in business cycle comovement among the G7 countries, and (ii) mixed evidence of changes in covariances and correlations with a set of macroeconomic variables.

JEL Classification Numbers: E32, F21, F32, F36

Keywords: Capital Flows, International Business Cycles.

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1 Introduction

Gross capital flows among industrialized countries expanded by 722% between 1991 and 2005. This increase exceeded real GDP growth (approximately 29%) and international trade growth (about 151%) in advanced economies. During those years macroeconomic comovement among the G7 economies was lower than in previous decades.\(^1\) Did the cyclical behavior of capital flows change during this period of increased financial globalization and decreased comovement?

Most empirical research on capital flows has focused on aggregate net flows, flows between specific country pairs, and single components of flows. In the present work we revisit an idea originally suggested by Doyle and Faust (2005, DF, henceforth) in the international business cycle (IBC) literature and use formal statistical tests for changes in the volatility of capital flows and in the comovement between flows and macroeconomic variables over business cycle breaks in G7 countries.

We use data on total net and disaggregated gross flows between 1975:Q1 and 2005:Q4 and compute the ratio between each flow and domestic GDP.\(^2\) We take the log of real GDP, the ratio between gross fixed capital formation and GDP (Source: OECD Quarterly National Accounts), and the real interest rate (Source: IFS), and estimate the cyclical components of each transformed macroeconomic and capital flow series using standard filtering techniques. We find that recent changes in international business cycles are not associated with systematic changes in the second-moment properties of disaggregated flows, except for a general volatility increase.\(^3\)

1.1 Related Literature

Numerous studies in applied macroeconometrics and IBC, among them McConnell and Quiros (2000) and Heathcote and Perri (2004), examine changes in domestic volatility and cross-country correlation of macroeconomic aggregates over the past three decades. DF detect falling volatility in macroeconomic variables of G7 countries, but no variation in cross-country comovement. Stock and Watson (2005) suggest

\(^1\)Heathcote and Perri (2004) and Stock and Watson (2005).

\(^2\)We analyze 11 flows (International Financial Statistics, IFS, by IMF) for each country: inward FDI (iFDI), inward Foreign Portfolio Investment (iFPI), inward debt (iDebt), total inward flows (iTot); outward FDI (oFDI), outward Portfolio Investment (oFPI), outward debt (oDebt), total outward flows (oTot); net total flows (noTot), defined as outward flows net of inward flows; net FDI (noFDI), net FPI (noFPI), net debt (noDebt), defined analogously. These ratios are conceptually similar to net exports-to-GDP ratios in the IBC literature. See Neumeyer and Perri (2005).

\(^3\)In this work a single capital flow is said to be procyclical (countercyclical) with respect to a reference macroeconomic variable if the correlation of the cyclical component of the ratio between that capital flow and GDP and the cyclical component of the reference macroeconomic variable is positive (negative), and significantly different from zero.
that the widespread drop in volatility was mostly associated with a reduction in the magnitude of common international shocks. De Pace (2010) uses parametric bootstrap techniques to describe comovement changes in IBC within free-trade areas and the European currency union and finds some evidence of positive variations.

Levy-Yeyati, Panizza, and Stein (2007) study north-south FDI and find that outward FDI is countercyclical with respect to output and interest rate cycles in the US and Europe (but mildly procyclical in Japan), and that FDI and local investment in the source country are negatively correlated. Kaminsky, Reinhart, and Vegh (2005) show that net capital inflows are procyclical (borrowing increases in boom times and vice versa) in a sample of 104 countries. Levchenko and Mauro (2007) look at 142 countries between 1970 and 2003 and show that FDI is the least volatile capital flow and is remarkably more stable than other types of flows during sudden stops episodes, whereas bank lending flows drop dramatically and take a long time to recover. Smith and Valderrama (2009) consider emerging markets and find that debt and portfolio flows (FPI) are more correlated with investment than with GDP, whereas FDI is more correlated with GDP. Contessi, De Pace, and Francis (2010) look at disaggregated flows in 22 countries and find that, while inward flows are procyclical, outward and net outward flows are countercyclical for most industrial and emerging countries, except the G7. Results for individual flows are ambiguous, except for inward FDI flows, which are procyclical in industrial countries, countercyclical in emerging countries.

2 Breakpoint Analysis

We test for changes in volatility and comovement using the nonparametric bootstrap procedure described in De Pace (2010). We use two exogenous breaks, \( Br, 1992:Q2 \), estimated by DF for GDP and 1993:Q1 for investment. These breaks mark the most likely change dates in comovement among G7 countries between the 1980s and the 1990s. We use 1992:Q2 for the real interest rate. To test for second moment shifts in time series pairs (covariances and correlations) or in single time series (variances), we bootstrap nonparametrically the difference of the second moments over two subsequent subsamples. Let \( \theta \) be the parameter of interest (variance, covariance, or the correlation coefficient), \( \theta_1 \) its true value over the first sample, \( \theta_2 \) its true value over the second sample. We test whether the parameter shift, \( \Delta \theta = (\theta_2 - \theta_1) \), is statistically significant. Formally, we run the statistical test with size \((1 - \alpha) \in (0, 1)\), \( H_0 : \Delta \theta = (\theta_2 - \theta_1) = 0 \) against the alternative \( H_1 : \Delta \theta = (\theta_2 - \theta_1) \neq 0 \). Two-sided, \( \alpha \)-level, and equal-tailed
confidence intervals, constructed from the bootstrap distribution of $\hat{\Delta}\theta$, are used to detect significant shifts and infer the sign of their direction. Bootstrap iteration is applied to estimate confidence intervals with improved accuracy as described in DiCiccio, Martin, and Young (1992). Shifts significant at the 10% level signal parameter instability.

### 2.1 Constructing the Bootstrap Distribution for $\hat{\Delta}\theta$

Let $X_{A,t} = \{X_{A,s}\}_{s=1}^T$ and $X_{B,t} = \{X_{B,s}\}_{s=1}^T$ denote two observed time series for countries $A$ and $B$. Let $Br \in (1,T)$ be an exogenous breakpoint, which splits $X_{A,t}$ and $X_{B,t}$ into two subsamples, $X_{A,t}^1 = \{X_{A,s}\}_{s=1}^{Br}$, $X_{B,t}^1 = \{X_{B,s}\}_{s=1}^{Br}$, $X_{A,t}^2 = \{X_{A,s}\}_{s=Br+1}^T$, and $X_{B,t}^2 = \{X_{B,s}\}_{s=Br+1}^T$. Let $\theta$ be either the correlation coefficient or the covariance. In the first subsample, let $w_{A,i,l}$ and $w_{B,i,l}$ respectively denote the blocks $\{X_{A,s}\}_{s=i}^{i+l-1}$ and $\{X_{B,s}\}_{s=i}^{i+l-1}$ of length $l$ starting at $X_{A,i}$ and $X_{B,i}$, with $X_{A,i} = X_{A,1}+((i-1) \text{ mod } Br)$, $X_{B,i} = X_{B,1}+((i-1) \text{ mod } Br)$, $X_{A,0} = X_{A,Br}$, and $X_{B,0} = X_{B,Br}$. Finally, let $I_1, I_2, ...$ be a stream of random numbers uniform on the integers $1, ..., Br$, and let $L_1, L_2, ...$ be a stream of random numbers independently drawn from a geometric distribution, $\text{Prob}(L = l) = \lambda (1-\lambda)^{l-1}$ with $l = 1, 2, ...$. The inverse of $\lambda$ is the expected block length, $E(L) = \frac{1}{\lambda}$, to be estimated through an inner procedure based on an automatic rule that minimizes an appropriate objective function. Given $(\frac{1}{\lambda})$, the algorithm that generates a couple of stationary bootstrap time series replicates over the first subsample, $X_{A,t}^1$ and $X_{B,t}^1$, runs as follows: (i) set $X_{A,t}^1 = w_{A,I_1,L_1}$, $X_{B,t}^1 = w_{B,I_1,L_1}$, and $j = 1$; (ii) while $\text{length}(X_{A,t}^1) < Br$, increment $j$ by 1 and redefine $X_{A,t}^1$ and $X_{B,t}^1$ as $X_{A,t}^1 := X_{A,t}^1 \cup w_{A,I_j,L_j}$ and $X_{B,t}^1 := X_{B,t}^1 \cup w_{B,I_j,L_j}$; (iii) if $\text{length}(X_{A,t}^1) > Br$, discard the two series of pseudo-data just generated and restart resampling from (i) after drawing new streams of $I_j$’s and $L_j$’s. We apply this scheme to both the first and the second subsamples $N_O^B$ times. At each complete resample of the original data, we estimate and collect $\hat{\Delta}\theta^* = \{\hat{\theta}(X_{A,t}^1, X_{B,t}^1) - \hat{\theta}(X_{A,t}^1, X_{B,t}^1)\}$ to compose the bootstrap distribution of $\hat{\Delta}\theta$. The same logic applies with just one time series, if the statistic of interest is the variance.

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4 We resample blocks of random length. Length is sampled from an independent geometric distribution whose expected value equals the expected block size. The original series should be wrapped around a circle to fill blocks going past the last observation. Optimal expected length is estimated through an inner (smaller) bootstrap procedure. This resampling scheme is known as stationary bootstrap.
2.2 Estimating Accurate Confidence Intervals for $\Delta \theta$

Let $X_{A,t}$ and $X_{B,t}$ be two variables and $I_0\left(\alpha; X_{A,t}, X_{B,t}; X_{A,t}^*, X_{B,t}^*\right)$ the uncorrected bootstrap percentile confidence interval of nominal coverage probability $\alpha$ for $\Delta \theta$, where $\theta$ is either the correlation or the covariance.\footnote{The framework is adjusted accordingly when only one time series is used to estimate variance changes.} $X_{A,t}^*$ and $X_{B,t}^*$ are two generic resamples with replacement from $X_{A,t}$ and $X_{B,t}$. $I_0$ is constructed from sample and resample information. Usually, in empirical applications, the coverage probability of $I_0$, namely $P(\alpha) = \text{Prob}\left\{\Delta \theta \in I_0\left(\alpha; X_{A,t}, X_{B,t}; X_{A,t}^*, X_{B,t}^*\right)\right\}$, differs from $\alpha$. There exists a real number, $\varrho_0$, such that $P(\varrho_0) = \alpha$.

Let $I_0\left(\alpha; X_{A,t}^*, X_{B,t}^*; X_{A,t}^{**}, X_{B,t}^{**}\right)$ be a version of $I_0\left(\alpha; X_{A,t}, X_{B,t}; X_{A,t}^*, X_{B,t}^*\right)$ computed using information from $X_{A,t}^*$, $X_{B,t}^*$, $X_{A,t}^{**}$, and $X_{B,t}^{**}$. $X_{A,t}^{**}$ and $X_{B,t}^{**}$ are resamples with replacement of $X_{A,t}^*$ and $X_{B,t}^*$. An estimate of $P(\alpha)$ is $\widehat{P}(\alpha) = \text{Prob}\left\{\Delta \theta \in I_0\left(\alpha; X_{A,t}^*, X_{B,t}^*; X_{A,t}^{**}, X_{B,t}^{**}|X_{A,t}, X_{B,t}\right)\right\}$. Let $N^B_O$ be the number of bootstrap replications at the outer level of resampling, then $\widehat{P}(\alpha)$ is calculated as

$$\widehat{P}(\alpha) = \frac{\sum_{n^B_O=1}^{N^B_O} 1\{\Delta \theta \in I_{\varrho_0,n^B_O}\left(\alpha; X_{A,t}^*, X_{B,t}^*; X_{A,t}^{**}, X_{B,t}^{**}\right)\}}{N^B_O}.$$ 

Since distribution information on $X_{A,t}^{**}$ and $X_{B,t}^{**}$ given $X_{A,t}^*$ and $X_{B,t}^*$ is unavailable, an inner level of resamples (say, $N^B_I$ resamples for each outer resample, $n^B_O$) from $X_{A,t}^*$ and $X_{B,t}^*$ is used to outline the features of that distribution.\footnote{We use 1,000 replications for the outer bootstrap; 500 for the inner bootstrap. Bootstrap samples are drawn using the same nonparametric method in the main and nested bootstraps. We choose the smallest value $\widehat{\varrho}_0$ such that $\widehat{P}(\varrho_0)$ is as close as possible to $\alpha$, i.e., such that $|\widehat{P}(\varrho_0) - \alpha|$ is minimized over a grid of values and additional conditions defining tolerance are satisfied (De Pace, 2010).}

The bootstrap estimate for $\varrho_0$ is the solution, $\widehat{\varrho}_0$, to the equation $\widehat{P}(\varrho_0) = \alpha \therefore \widehat{\varrho}_0 = \widehat{P}^{-1}(\alpha)$. The iterated bootstrap confidence interval for $\Delta \theta$ is then $I_1\left(\widehat{\varrho}_0; X_{A,t}, X_{B,t}; X_{A,t}^*, X_{B,t}^*\right)$.

3 Shifts in Second Moments

Inward and outward FDI and FPI exhibit a positive trend from the mid-90s, with peaks in the late 1990s and early 2000s. Debt flows have high volatility, but no clear pattern, except for an upward trend in the US. Five-year rolling standard deviations (SDs) generally increase and then slightly rebound due to the boom and subsequent slowdown in capital flows in the late 1990s and early 2000s. The SD of inward debt flows is high and rising roughly throughout the sample in Canada, Italy, and the US. The SD of outward debt flows trends upwards in Italy and the US only.
Inward and outward flows are dominated by movements in debt and exhibit only a mildly increasing trend. Their volatility increases throughout the sample in most countries. There is little trend in the volatility of net flows, except in France and the US (increasing volatility), and the UK (declining volatility). Net outward flows exhibit a slightly increasing trend except in the US, where they markedly trend downwards. Net flow volatility is lower than both inward and outward flow volatility for most G7 countries.\textsuperscript{7} Debt is the most volatile type of capital flow.

In Table 1, we summarize the number and sign of correlations between the cyclical components of disaggregated capital flows and real GDP ($g$), investment to GDP ratio ($i$), and real interest rate ($r$) over the periods 1975-1992, 1992-2005, and 1975-2005. We test whether each correlation is significant at the 10\% level using the nonparametric framework described above. A particular flow is procyclical (countercyclical) with respect to a reference macroeconomic variable if the majority of significant correlations is positive (negative). Its cyclical properties are ambiguous if the number of significantly positive correlations equals the number of significantly negative correlations and non-significantly positive and negative values are equal in number.

**Aggregate Flows.** (1A) Inward flows are procyclical with respect to GDP, investment, and the real interest rate. (1B) Outward flows are procyclical with respect to GDP and investment, and to some extent to the real interest rate. (1C) Net outward flows are countercyclical with respect to GDP and investment, and to some extent to the real interest rate.

**Disaggregated Flows.** (2A) Inward and outward FDI tend to be procyclical with all three reference macroeconomic variables. Net outward FDI is procyclical with respect to investment. (2B) Inward FPI and debt tend to be procyclical in most countries. (2C) Outward FPI and net outward FPI are countercyclical with respect to the real interest rate.

In Table 2, we describe the second-moment variations between net, gross, and disaggregated capital flows and the reference macroeconomic variables.

**Variance Changes: Macroeconomic Variables.** Almost all sample variance shifts in GDP, investment, and the real interest rate are negative. Many are significant. This decrease in correlation is linked to the Great Moderation and consistent with DF and Stock and Watson (2005).

**Variance Changes: Disaggregated Capital Flows.** Sample variances generally increase over

\textsuperscript{7}Contessi et al. (2010) show that this pattern does not extend to other OECD and emerging-market countries.
the breaks for net, total, and disaggregated flows. The majority of these shifts is statistically significant. This finding suggests the existence of an underlying common factor affecting the volatility properties of total inward and outward flows across countries, whose existence would not clearly emerge if we only considered net flows (as in Kaminsky, Reinhart, and Vegh 2005), for which we observe a few negative point estimates.

Since most of the variances of macroeconomic variables decrease and most of the variances of capital flows increase, the correlation variations depend on the size of the covariance changes between these variables relative to the changes in their standard deviations.

**Correlation and Covariance Changes.** Results are heterogeneous across types of flows and macro aggregates. In general, we cannot identify specific patterns. Pointwise, covariance changes usually have the same sign as correlation changes, with only few exceptions due to the relative idiosyncratic variations in the standard deviations. Furthermore, the proportion of significant shifts is modest.

### 4 Conclusion and Discussion

We run formal statistical tests to make inferences on the variations of volatility, covariance, and correlation between capital flows and a set of macroeconomic variables in the G7 countries. Second-moment shifts show mixed signs over recent breaks in international business cycles. We detect a clear statistically significant increase in the variance of all types of flows.

The lack of a uniform pattern in the correlation changes is explained by the fact that increases in the volatility of capital flows are usually countered by decreases in the idiosyncratic variation of the macroeconomic variables. Since the covariances between macro aggregates and capital flows change in different directions, a clear pattern for the correlation shifts is unlikely to emerge. The correlation coefficients and the common variations between individual capital flows and macro variables tend to move together over the breaks, although the idiosyncratic variabilities typically shift in opposite directions.

Standard international business cycle theories predict that deeper financial integration allows capital to flow to countries that experience positive productivity shocks and relatively more growth. This, in turn, induces higher synchronization among net capital inflows and output, lower output correlations, increased risk-sharing at the international level, and a higher volatility in the capital flows (Backus, Kehoe, and Kydland, 1992). Doyle and Faust (2005) do not detect statistically significant comovement changes in
output and consumption over the breaks they estimate for the G7 economies. Our results show that net inflows do not become more procyclical after the breaks, consistent with the established findings of little or no increase in risk-sharing.

Although more volatile capital flows can be interpreted as evidence of more highly integrated financial markets among the G7 countries, it is possible that better risk-sharing could be achieved only with substantially larger capital flows than those observed to date (see, e.g. Forbes, 2010, for an analysis of the low exposure of foreign investors to U.S. markets for equity and bonds).

References


De Pace, P., 2010. Currency union, free-trade areas, and business cycle synchronization, Pomona College, manuscript.


<table>
<thead>
<tr>
<th>Year</th>
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<th>Negative</th>
<th>Average</th>
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<td>2 (1)</td>
<td>3 (1)</td>
<td>+: procyclical, -: countercyclical, ?: ambiguous</td>
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Note. In each cell, second-moment changes refer to correlation, covariance, variance in the cyclical component of capital flow, variance in the macroeconomic variable. U: significantly positive change, u: non-significantly positive change, d: non-significantly negative change, D: significantly negative change.

Table 2: Changes in Second Moments. Breaks Based on Doyle and Faust (2005)