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# APPENDIX 3

# UNITS OF MEASUREMENT AND MATHEMATICAL FORMULAS

# UNITS OF MEASUREMENT

Measure	Symbol	Unit of measurement	Symbol of the unit of measurement	Some equivalencies
Area	А	<ul> <li>Square metre (square centimetre)</li> </ul>	m <sup>2</sup> (cm <sup>2</sup> )	1 m <sup>2</sup> =10 000 cm <sup>2</sup>
Concentration	С	<ul><li>Gram of solute per litre of solution</li><li>Part per million</li></ul>	g L ppm	$\frac{1 \text{ g}}{1 \text{ L}} = \frac{1 \text{ g}}{1000 \text{ mL}}$ $1 \text{ ppm} = \frac{1 \text{ mg}}{1000 \text{ g}}$ Aqueous solution: $1 \text{ ppm} \simeq \frac{1 \text{ mg}}{1 \text{ L}}$
Current intensity	1	◆ Ampere	A	$1 A = \frac{1 C}{1 s}$ $1 A = \frac{1 V}{1 \Omega}$
Distance travelled	d	<ul><li>Metre (kilometre)</li></ul>	m (km)	1 km = 1000 m
Electrical charge	q or Q	<ul><li>Coulomb</li></ul>	С	$1 \text{ C} = 6.25 \times 10^{18}$ elementary charges
Electrical power	P <sub>e</sub>	<ul><li>Watt (kilowatt)</li></ul>	W (kW)	1 kW = 1000 W 1 W = $\frac{1 J}{1 s}$ 1 W = 1 A × 1 V
Electrical resistance	R	● Ohm	Ω	$1 \Omega = \frac{1 V}{1 A}$
Energy  - Kinetic energy  - Mechanical energy  - Gravitational potential energy  - Thermal energy  - Electrical energy	E E <sub>k</sub> E <sub>m</sub> E <sub>p</sub>	<ul><li>Joule (kilojoule)</li><li>Kilowatt hour</li></ul>	J (kJ)	1 J = 1 N × 1 m 1 J = 1 $\frac{\text{kg} \times \text{m}^2}{\text{s}^2}$ 1 kJ = 1000 J 1 kWh = 3600 kJ
Force  - Electrical force  - Gravitational force  - Buoyant force	F F <sub>e</sub> F <sub>g</sub> F <sub>b</sub>	<ul><li>Newton</li></ul>	N	$1 N = 1 \frac{kg \times m}{s^2}$ On Earth: $1 N \approx 100 g$
Heat	Q	<ul><li>Joule</li></ul>	J	1 kJ = 1000 J
Height	h	<ul><li>Metre (kilometre)</li></ul>	m (km)	1 km = 1000 m

Measure	Symbol	Unit of measurement	Symbol of the unit of measurement	Some equivalencies
Intensity of the gravitational field or gravitational acceleration	g	<ul><li>Newton per kilogram</li></ul>	N kg	$1 \frac{N}{kg} = 1 \frac{m}{s^2}$
		Metre per second squared	$\frac{m}{s^2}$	
Length	L	Metre (kilometre)	m (km)	1 km = 1000 m
Mass	m	<ul><li>Gram (milligram, kilogram)</li><li>Tonne</li></ul>	g (mg, kg)	1 kg = 1000 g 1 tonne = 1000 kg
Molar concentration	С	Mole of solute per litre of solution	mol L	$\frac{1 \text{ mol}}{1 \text{ L}} = \frac{6.02 \times 10^{23} \text{ entities}}{1 \text{ L}}$
Molar mass	М	Gram per mole	g mol	$\frac{1 \text{ g}}{1 \text{ mol}} = \frac{1 \text{ g}}{6.02 \times 10^{23} \text{ entities}}$
Number of moles	n	<ul><li>Mole</li></ul>	mol	1 mol = $6.02 \times 10^{23}$ entities
Potential difference or voltage	V	<ul><li>Volt</li></ul>	V	$1 V = \frac{1 J}{1 C}$ $1 V = 1 A \times 1 \Omega$
Pressure	Р	Pascal (kilopascal)	Pa (kPa)	1 Pa = $\frac{1 \text{ N}}{1 \text{ m}^2}$ 1 kPa = 1000 Pa
		Millimetre of mercury	mm Hg	1 mm Hg = 0.13 kPa
Specific heat capacity <sup>1</sup>	С	Joule per gram per degree Celsius	J g°C	$1 \frac{J}{g^{\circ}C} = 1 \frac{1 kJ}{kg^{\circ}C}$
Temperature <sup>1</sup>	Т	Degree Celsius     Kelvin	°C K	0°C = 273 K
Time	t	<ul><li>Second</li><li>Minute</li><li>Hour</li></ul>	s min h	1 min = 60 s 1 h = 60 min 1 h = 3600 s
Velocity / speed	v	Metre per second	<u>m</u> s	$1\frac{m}{s} = 3.6 \frac{km}{h}$
		Kilometre per hour	km h	
Volume	V	Cubic metre (cubic centimetre, cubic decimetre) Litre (millilitre)	m <sup>3</sup> (cm <sup>3</sup> , dm <sup>3</sup> ) L (mL)	1 mL = 1 cm <sup>3</sup> 1 L = 1 dm <sup>3</sup> 1 L = 1000 mL
Weight	w	<ul><li>Newton</li></ul>	N	$1 \text{ N} = 1 \frac{\text{kg} \times \text{m}}{\text{s}^2}$
Work	W	<ul><li>Joule</li></ul>	J	1 J = 1 N × 1 m

<sup>1.</sup> In this textbook, we use the degree Celsius (°C) rather than the kelvin, which is the SI base unit.

# MATHEMATICAL FORMULAS

#### THE MATERIAL WORLD

# **AVERAGE SPEED**

$$v = \frac{d}{\Delta t}$$
 where  $v$  is the average speed (in m/s)  $d$  is the distance travelled (in m)

 $\Delta t$  is the time variation—in other words, the travelling time (in s)

#### CONCENTRATION

$$C = \frac{m}{V}$$
 where  $C$  is the concentration (in g/L)  
 $m$  is the mass of the solute (in g)

V is the volume of solution (in L)

 $C = \frac{n}{V}$  where C is the concentration (in mol/L)

n is the amount of solute (in mol) V is the volume of solution (in L)

#### COULOMB'S LAW

$$F_e = \frac{kq_1q_2}{r^2}$$
 where  $F_e$  is the electrical force (in N)

k is Coulomb's constant, which is  $9 \times 10^9 \text{ Nm}^2/\text{C}^2$ 

 $q_1$  is the charge of the first particle (in C)  $q_2$  is the charge of the second particle (in C) r is the distance between the two particles (in m)

#### **CURRENT INTENSITY**

$$I = \frac{q}{\Lambda +}$$
 where I is the current intensity (in A)

q is the charge (in C)  $\Delta t$  is the time interval (in s)

#### EFFECTIVE FORCE (USEFUL TRIGONOMETRIC FUNCTIONS)

$$Sin A = \frac{side opposite to angle A}{hypotenuse}$$

$$Cos A = \frac{\text{side adjacent to angle } A}{\text{hypotenuse}}$$

$$Tan A = \frac{\text{side opposite to angle } A}{\text{side adjacent to angle } A}$$

Note: Most scientific calculators immediately give the sine (sin), cosine (cos) and tangent (tan or tg) values of any angle. However, make sure the calculator measures angles in degrees (and not in radians or grads).

#### **ELECTRICAL ENERGY USED**

 $E = P_e \Delta t$  where E is the electrical energy used (in J or kWh)  $P_e$  is the electrical power (in W or kW)

 $\Delta t$  is the time interval (in s or h)

#### **ELECTRICAL POWER**

 $P_e = \frac{W}{\Delta t}$  where  $P_e$  is the electrical power (in W)

W is the work (in J)

 $\Delta t$  is the time required (in s)

 $P_e = VI$  where  $P_e$  is the electrical power (in W)

V is the potential difference (in V)
I is the current intensity (in A)

#### GRAVITATIONAL POTENTIAL ENERGY

 $E_p = mgh$  where  $E_p$  is the gravitational potential energy (in J)

m is the mass of the object (in kg)

g is the gravitational field intensity (in N/kg)

h is the height of the object above the reference surface (in m)

#### **HEAT AND THERMAL ENERGY**

 $Q = \Delta E_t$  where Q is the heat (in J)

 $\Delta E_t$  is the variation in thermal energy (in J)

 $Q = mc\Delta T$  where Q is the heat (in J)

m is the mass (in g)

c is the specific heat capacity (in J/g $^{\circ}$ C)  $\Delta T$  is the temperature variation (in  $^{\circ}$ C)

 $\Delta T = T_f - T_i$  where  $T_f$  is the final temperature (in °C)

 $T_i$  is the initial temperature (in °C)

#### **KINETIC ENERGY**

 $E_k = \frac{1}{2} mv^2$  where  $E_k$  is the kinetic energy of the object (in J)

m is the mass of the object (in kg)v is the velocity of the object (in m/s)

#### MECHANICAL ENERGY

 $E_m = E_k + E_p$  where  $E_m$  is the mechanical energy (in J)

 $E_k$  is the kinetic energy (in J)  $E_D$  is the potential energy (in J)

# MOLAR MASS

 $M = \frac{m}{n}$  where M is the molar mass (in g/mol)

m is the mass (in g)

n is the number of moles (in mol)

#### OHM'S LAW

V = RI where V is the potential difference (in V)

R is the resistance (in  $\Omega)$  I is the current intensity (in A)

#### POTENTIAL DIFFERENCE

 $V = \frac{E}{G}$  where V is the potential difference (in V)

 $\boldsymbol{E}$  is the energy transferred (in J)

q is the charge (in C)

#### **PRESSURE**

 $P = \frac{F}{A}$  where P is the pressure (in Pa)

F is the force perpendicular to the surface (in N) A is the surface area subjected to the force (in  $m^2$ )

#### **WEIGHT AND GRAVITATIONAL FORCE**

 $w = F_q = mg$  where w is the weight (in N)

 $F_q$  is the gravitational force (in N)

m is the mass (in kg)

g is the gravitational field intensity (in N/kg)

#### WORK

 $W = \Delta E$  where W is the work (in J)

 $\Delta E$  is the variation in energy in an object or a system (in J)

W = F//d where W is the work (in J)

F// is the force or the force component parallel to the direction of travel (in N)

d is the distance travelled by the object (in m)

#### THE LIVING WORLD

#### **POPULATION DENSITY**

Population density =  $\frac{\text{Number of individuals}}{\text{Space (area or volume) occupied}}$ 

#### POPULATION SIZE, ESTIMATED USING SAMPLE AREAS

Population size =  $\frac{\text{Average number of individuals per section} \times \text{Total study area}}{\text{Area of a section}}$ 

#### POPULATION SIZE, ESTIMATED USING THE MARK-RECAPTURE METHOD