

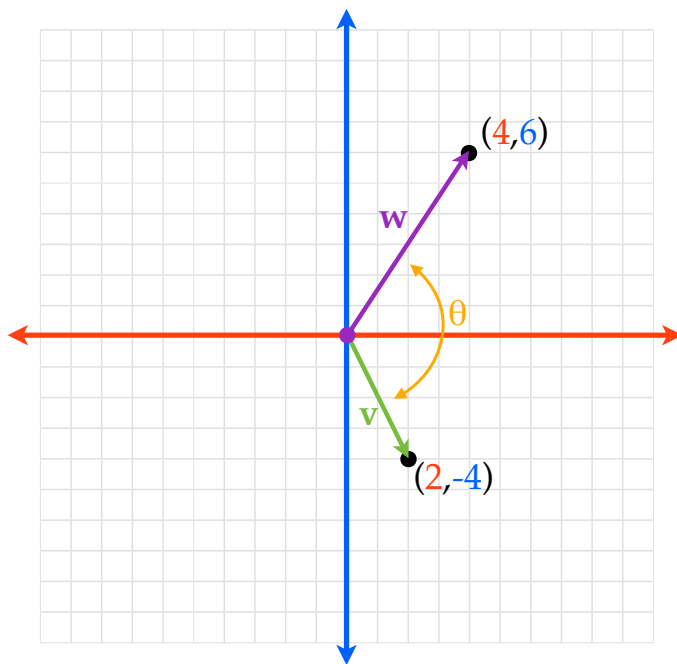
## Finding the Angle Between Two Vectors

Given  $\mathbf{v}$  and  $\mathbf{w}$ , the angle  $\theta$  ( $0^\circ \leq \theta \leq 180^\circ$ ) between  $\mathbf{v}$  and  $\mathbf{w}$  is determined by

$$\cos \theta = \frac{\mathbf{v} \cdot \mathbf{w}}{\|\mathbf{v}\| \|\mathbf{w}\|}$$

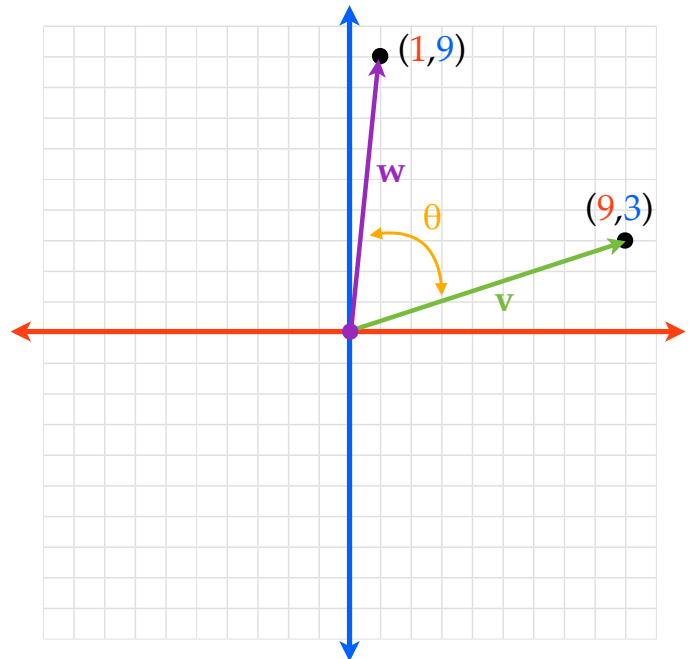
$$\cos \theta = \frac{\mathbf{v} \cdot \mathbf{w}}{\|\mathbf{v}\| \|\mathbf{w}\|}$$

Find the angle between  $\mathbf{v}$  and  $\mathbf{w}$ ,  
given  $\mathbf{v} = \langle 2, -4 \rangle$  and  $\mathbf{w} = \langle 4, 6 \rangle$



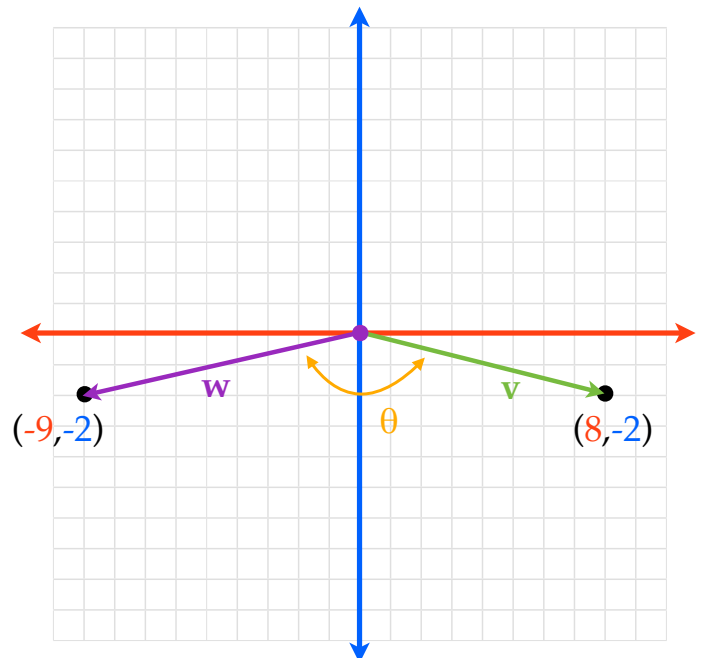
$$\cos \theta = \frac{\mathbf{v} \cdot \mathbf{w}}{\|\mathbf{v}\| \|\mathbf{w}\|}$$

Find the angle between  $\mathbf{v}$  and  $\mathbf{w}$ ,  
given  $\mathbf{v} = 9\mathbf{i} + 3\mathbf{j}$  and  $\mathbf{w} = \mathbf{i} + 9\mathbf{j}$



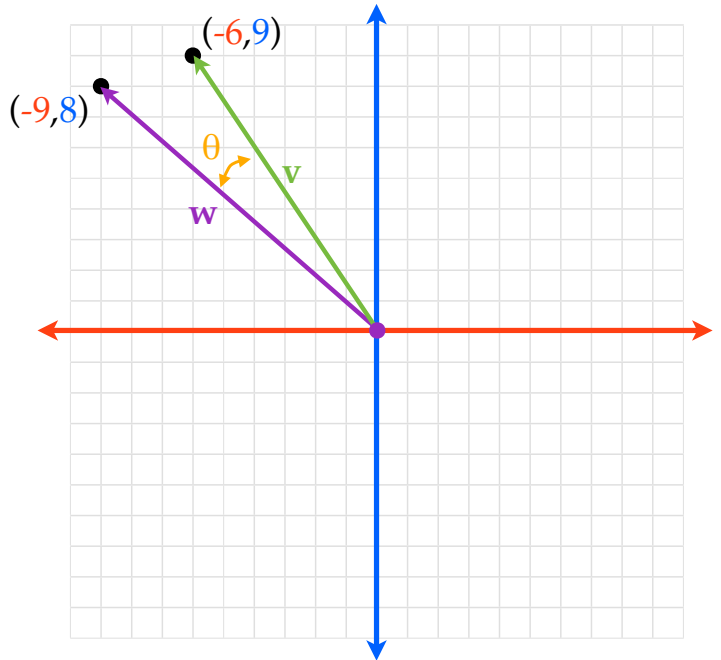
$$\cos \theta = \frac{\mathbf{v} \cdot \mathbf{w}}{\|\mathbf{v}\| \|\mathbf{w}\|}$$

Find the angle between  $\mathbf{v}$  and  $\mathbf{w}$ ,  
given  $\mathbf{v} = \langle 8, -2 \rangle$  and  $\mathbf{w} = \langle -9, -2 \rangle$



$$\cos \theta = \frac{\mathbf{v} \cdot \mathbf{w}}{\|\mathbf{v}\| \|\mathbf{w}\|}$$

Find the angle between  $\mathbf{v}$  and  $\mathbf{w}$ ,  
given  $\mathbf{v} = -6\mathbf{i} + 9\mathbf{j}$  and  $\mathbf{w} = -9\mathbf{i} + 8\mathbf{j}$



Given  $\mathbf{v}$  and  $\mathbf{w}$ , the angle  $\theta$  ( $0^\circ \leq \theta \leq 180^\circ$ ) between  $\mathbf{v}$  and  $\mathbf{w}$  is determined by

$$\cos \theta = \frac{\mathbf{v} \cdot \mathbf{w}}{\|\mathbf{v}\| \|\mathbf{w}\|}$$