$\frac{\tan^2\theta}{1+\tan^2\theta}=\sin^2\theta$

Prove the following identities

$$\sin \theta (1 + \cot^2 \theta) = \csc \theta$$

Prove the following identities

$$\csc^2 \theta \sin^2 \theta - \sin^2 \theta = \cos^2 \theta$$

Prove the following identities

$$\sec \theta - \tan \theta = \frac{\cos \theta}{1 + \sin \theta}$$

Prove the following identities

$$(\sin \theta + \cos \theta)^2 + (\sin \theta - \cos \theta)^2 = 2$$

Prove the following identities

$$\tan \theta + \cot \theta = \sec \theta \csc \theta$$

Prove the following identities

$$\tan \theta + \frac{\cos \theta}{1 + \sin \theta} = \sec \theta$$