

Proving the Power Rule for Real Exponents

Let n be any real number and let u be a differentiable function of x .

$$\frac{d}{dx}[x^n] = n \cdot x^{n-1} \qquad \frac{d}{dx}[u^n] = n \cdot u^{n-1} \cdot u'$$

Proof:

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