

Given the following...

$$\lim_{x \rightarrow c} f(x) = \infty \quad \lim_{x \rightarrow c} g(x) = L$$

Sum or Difference Property

$$\lim_{x \rightarrow c} [f(x) \pm g(x)] = \lim_{x \rightarrow c} f(x) \pm \lim_{x \rightarrow c} g(x) = \infty \pm L = \infty$$

Infinity always dominates

Given the following...

$$\lim_{x \rightarrow c} f(x) = -\infty \quad \lim_{x \rightarrow c} g(x) = L$$

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$$\lim_{x \rightarrow c} [f(x) \pm g(x)] = \lim_{x \rightarrow c} f(x) \pm \lim_{x \rightarrow c} g(x) = -\infty \pm L = -\infty$$

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Product Property

$$\begin{aligned} \lim_{x \rightarrow c} [f(x) \cdot g(x)] &= \lim_{x \rightarrow c} f(x) \cdot \lim_{x \rightarrow c} g(x) = \infty \cdot L = \infty, \quad L > 0 \\ &= \infty \cdot L = -\infty, \quad L < 0 \end{aligned}$$

Infinity always dominates

Given the following...

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Product Property

$$\begin{aligned} \lim_{x \rightarrow c} [f(x) \cdot g(x)] &= \lim_{x \rightarrow c} f(x) \cdot \lim_{x \rightarrow c} g(x) = -\infty \cdot L = -\infty, \quad L > 0 \\ &= -\infty \cdot L = \infty, \quad L < 0 \end{aligned}$$

Infinity always dominates

Given the following...

$$\lim_{x \rightarrow c} f(x) = \infty \quad \lim_{x \rightarrow c} g(x) = L$$

Quotient Property

$$\lim_{x \rightarrow c} \frac{g(x)}{f(x)} = \frac{\lim_{x \rightarrow c} g(x)}{\lim_{x \rightarrow c} f(x)} = \frac{L}{\infty} = 0$$

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Quotient Property

$$\lim_{x \rightarrow c} \frac{g(x)}{f(x)} = \frac{\lim_{x \rightarrow c} g(x)}{\lim_{x \rightarrow c} f(x)} = \frac{L}{-\infty} = 0$$

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