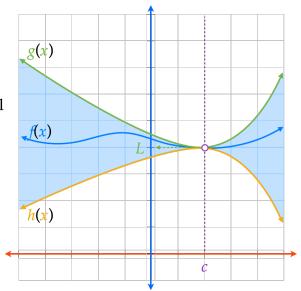
## The Squeeze Theorem

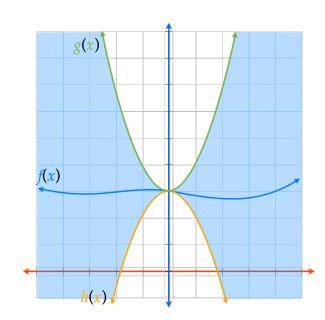
If  $h(x) \le f(x) \le g(x)$  for all x in an open interval containing point c (except possibly c), and if...

$$\lim_{x \to c} h(x) = L = \lim_{x \to c} g(x)$$

then 
$$\lim_{x \to c} f(x) = L$$



Given
$$3 - x^2 \le f(x) \le 3 + x^2$$
show  $\lim_{x \to 0} f(x) = 3$ 



$$3x \le f(x) \le x^3 + 2, \text{ for } 0 \le x \le 2$$

$$\lim_{x \to 1} f(x)$$

$$4 \le f(x) \le x^2 + 6x - 3, \text{ for all } x$$

$$\lim_{x \to 1} f(x)$$

## Given

$$1 + x^2 \le f(x) \le \cos x, \text{ for all } x$$

$$\lim_{x \to 0} f(x)$$

Find  $\lim_{x \to 0} x^2 \cdot \cos \frac{1}{x^2}$