

Standard Forms of Conic Sections

Parabola

$$(y - k)^2 = 4a(x - h)$$

$$(x - h)^2 = 4a(y - k)$$

Ellipse

$$\frac{(x - h)^2}{a^2} + \frac{(y - k)^2}{b^2} = 1$$

Circle

$$(x - h)^2 + (y - k)^2 = r^2$$

Hyperbola

$$\frac{(x - h)^2}{a^2} - \frac{(y - k)^2}{b^2} = 1$$

$$\frac{(y - k)^2}{a^2} - \frac{(x - h)^2}{b^2} = 1$$

Classify the following conics that each equation represents

$$\frac{(x - 2)^2}{16} + \frac{(y + 4)^2}{25} = 1$$

$$(x - 5)^2 + (y + 4)^2 = 64$$

$$(x + 2)^2 = -(y + 6)$$

$$\frac{(x + 2)^2}{1} - \frac{(y - 5)^2}{81} = 1$$

$$\frac{(y - 2)^2}{4} - \frac{(x + 4)^2}{9} = 1$$

$$(y - 5)^2 = 8(x + 4)$$

Classify the following conics that each equation represents

$$x^2 + 4x - y - 4 = 0$$

$$2y^2 + 2x^2 + 6y + 4x - 10 = 0$$

$$9x^2 - 18x + 4y^2 + 16y - 11 = 0$$

$$y^2 + 12y + x + 1 = 0$$

$$x^2 + 8x - 3y^2 - 6y + 4 = 0$$

$$x^2 + 9y^2 + 6x - 18y = -9$$

Classifying Conics (Analyze the Squared Terms)			
Parabola	1 squared term		
Circle	2 squared terms	same sign	same coefficient
Ellipse	2 squared terms	same sign	different coefficients
Hyperbola	2 squared terms	different signs	

Classify the following conics that each equation represents

$$y^2 - 2y - 4x^2 - 16x = 19$$

$$4x^2 + 8x + 4y^2 + 16y + 6 = 0$$

$$4x^2 + 8x + 3y^2 - 6y - 5 = 0$$

$$2y^2 - x^2 + 2x + 8y + 3 = 0$$

$$x^2 + 2x + 5y - 13 = 0$$

$$4y^2 + 8y - 5x = 6$$

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Classify the following conics that each equation represents

Parabola

Circle

Ellipse

Hyperbola

$$\begin{array}{l}
 (y - k)^2 = 4a(x - h) \quad (x - h)^2 + (y - k)^2 = r^2 \quad \frac{(x - h)^2}{a^2} + \frac{(y - k)^2}{b^2} = 1 \quad \frac{(x - h)^2}{a^2} - \frac{(y - k)^2}{b^2} = 1 \\
 (x - h)^2 = 4a(y - k) \quad \frac{(y - k)^2}{a^2} - \frac{(x - h)^2}{b^2} = 1
 \end{array}$$

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