

What is a Parabola?

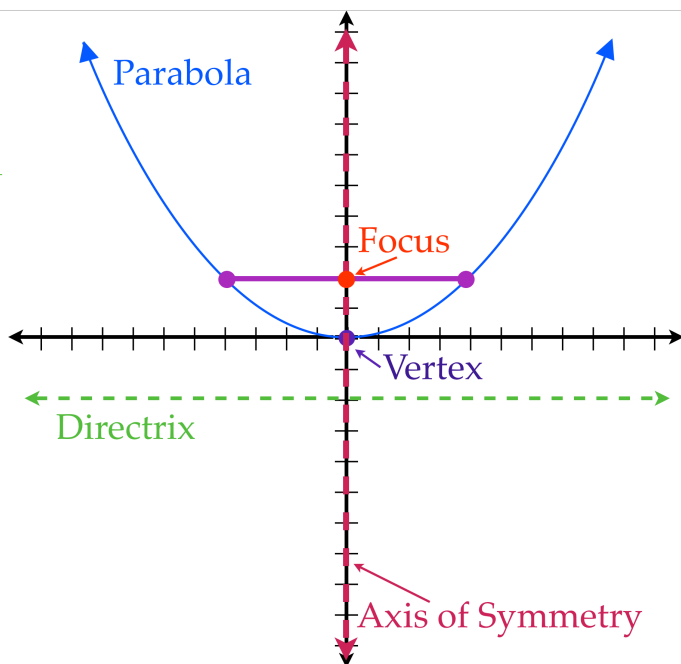
Parabola - the set of all points that are the same distance from a **given point** and a **given line** in a plane.

The given point is called the **Focus** and the given line is called the **Directrix**.

The midpoint of the perpendicular segment from the **focus** to the **directrix** is called the **Vertex**.

The line that passes through the **Vertex** and the **Focus** is called the **Axis of Symmetry**.

The **width** of the parabola at the **focus** is called the **Latus Rectum** or **Focal Width**.



Equation of a Parabola

with vertex (0,0)

$$x^2 = 4ay$$

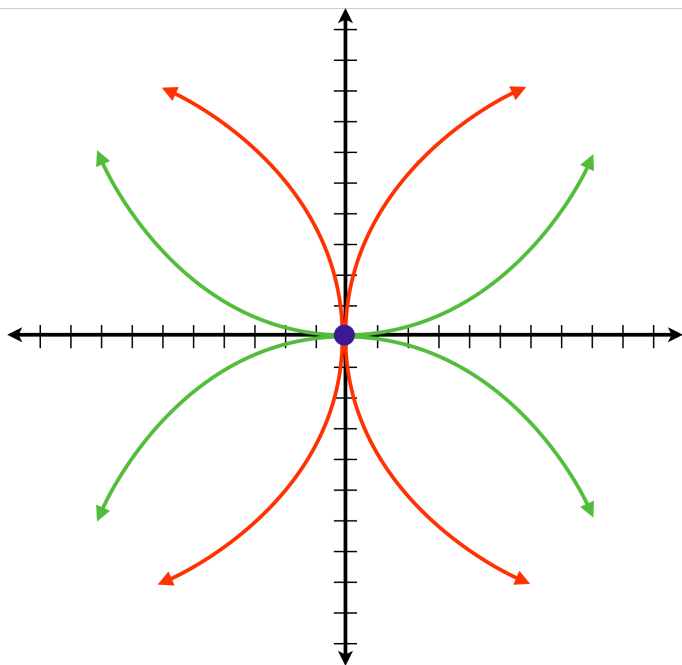
up/down

$a > 0$; opens up $a < 0$; opens down

$$y^2 = 4ax$$

right/left

$a > 0$; opens right $a < 0$; opens left



Pieces of a Parabola?

$$x^2 = 4ay$$

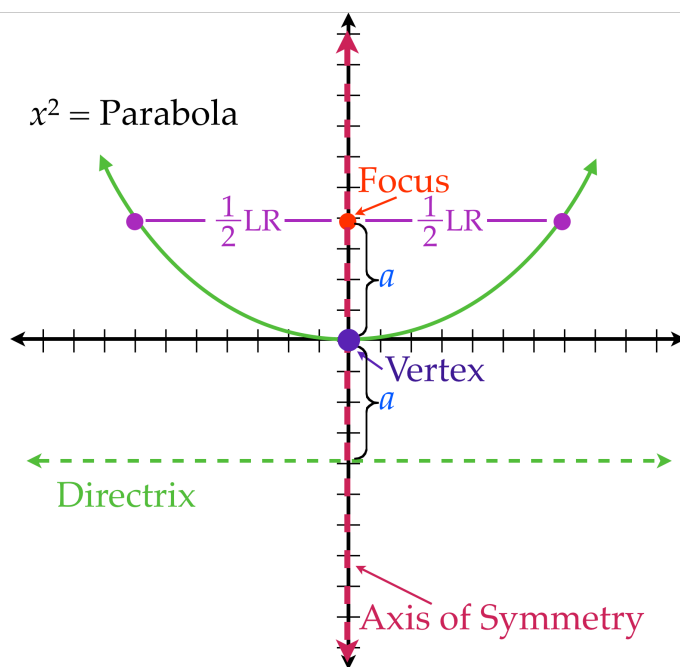
Vertex (0,0)

Focus (0,a)

Directrix $y = -a$

Axis of Symmetry $x = 0$

Latus Rectum $LR = |4a|$



Pieces of a Parabola?

$$y^2 = 4ax$$

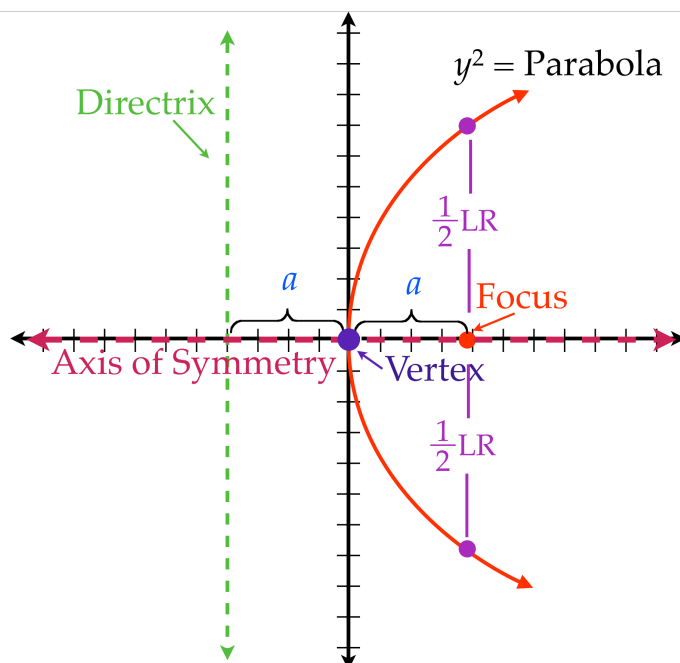
Vertex (0,0)

Focus (a,0)

Directrix $x = -a$

Axis of Symmetry $y = 0$

Latus Rectum $LR = |4a|$



Parabolas

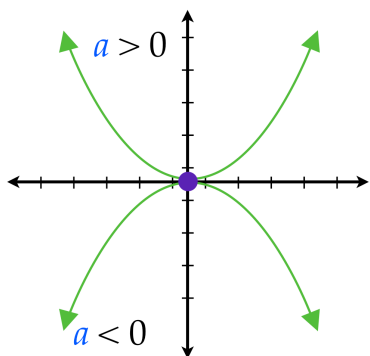
$$x^2 = 4ay$$

Vertex (0,0)

Directrix $y = -a$

Focus (0,a)

Axis of Symmetry $x = 0$



Latus Rectum

$$LR = |4a|$$

$$y^2 = 4ax$$

Vertex (0,0)

Directrix $x = -a$

Focus (a,0)

Axis of Symmetry $y = 0$

