

Linear Systems: Solving by Elimination

Date Lesson Notes

MINDS ON:

When adding $2765 + 1948$, or subtracting $7549 - 3616$ it's easier when you stack them:

$$\begin{array}{r} 2968 \\ + 1748 \\ \hline 4716 \end{array}$$

$$\begin{array}{r} 7649 \\ - 3516 \\ \hline 4233 \end{array}$$

The same is true for polynomials. $(3x + 2y) + (2x - 5y)$ can be written as:

$$\begin{array}{r} 3x + 2y \\ + 2x - 5y \\ \hline 5x - 3y \end{array}$$

IMPORTANT:

You want to stack the x's on top of each other and the y's on top of each other so they line up.

EXAMPLES:

Subtraction can be tricky because you need to remember to subtract each term...

$$1. (4x - 7y) - (3x - 2y) \longrightarrow \begin{array}{r} 4x - 7y \\ - (3x - 2y) \\ \hline = x - 5y \end{array}$$

$$2. (-5x + 3y) - (-2x + 8y) \longrightarrow \begin{array}{r} -5x + 3y \\ - (-2x + 8y) \\ \hline = -3x - 5y \end{array}$$

YOUR TURN!

$$3. (4x + 2y) + (-9x + y) \begin{array}{r} 4x + 2y \\ + (-9x + y) \\ \hline -5x + 3y \end{array}$$

$$4. (-3x - 5y) - (7x + 2y) \begin{array}{r} -3x - 5y \\ - (7x + 2y) \\ \hline -10x - 7y \end{array}$$

QUESTION:

How would you make the following equal to zero? Would you add or would you subtract the terms?

$$\begin{array}{r} -3x \\ -3x \\ \hline 0 \end{array} \text{ SUBTRACT} \quad \begin{array}{r} -5y \\ +5y \\ \hline 0 \end{array} \text{ ADD} \quad \begin{array}{r} 12x \\ +12x \\ \hline 0 \end{array} \text{ ADD} \quad \begin{array}{r} -100y \\ -100y \\ \hline 0 \end{array} \text{ SUBTRACT}$$

TO MAKE A TERM ZERO.... If the signs are OPPOSITE, then ADD.

If the signs are the SAME, then SUBTRACT.

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EXAMPLE 1 - Use ELIMINATION to solve this system.

<p>STEP 1: Determine which variable you will eliminate and decide on the operation to be used. (addition or subtraction?)</p>	<p>Same coefficient $4x - 5y = 7$ ① $+ -4x + 3y = -5$ ②</p>								
<p>STEP 2: Add or subtract the like-terms (be careful with the signs)</p>	<p>ADD Because opposite signs. $0 - 2y = 2$ $-2y = 2$</p>								
<p>STEP 3: Solve the resulting equation.</p>	<p>$\frac{-2y}{-2} = \frac{2}{-2}$ $y = -1$</p>								
<p>STEP 4: Substitute the value found for one variable into either equation to solve for the other variable.</p>	<p>Sub $y = -1$ into ① $4x - 5(-1) = 7$ $4x + 5 = 7$ $4x = 7 - 5$ $\frac{4x}{4} = \frac{2}{4}$ $x = \frac{1}{2}$</p>								
<p>STEP 5: State the point of intersection</p>	<p>\therefore POI is $(\frac{1}{2}, -1)$</p>								
<p>Check your solution in both original equations.</p>									
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<p>STEP 1: Determine which variable you will eliminate and decide on the operation to be used. (addition or subtraction?)</p>	$\begin{array}{r} 2x + 3y = 5 \quad (1) \\ -4x + 3y = 1 \quad (2) \\ \hline \end{array}$								
<p>STEP 2: Add or subtract the like-terms (be careful with the signs)</p>	<p>SUBTRACT (same signs)</p> $-2x + 0 = 4$								
<p>STEP 3: Solve the resulting equation.</p>	$\begin{array}{r} -2x = 4 \\ \hline -2 \quad -2 \\ \hline x = -2 \end{array}$								
<p>STEP 4: Substitute the value found for one variable into either equation to solve for the other variable.</p>	<p>Sub. $x = -2$ into (1)</p> $\begin{array}{l} 2(-2) + 3y = 5 \\ -4 + 3y = 5 \\ 3y = 5 + 4 \\ 3y = 9 \\ \frac{3y}{3} = \frac{9}{3} \end{array} \quad \boxed{y = 3}$								
<p>STEP 5: State the point of intersection</p>	<p>POI. is $(-2, 3)$</p>								
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PRACTICE QUESTIONS: Solve the following systems using Elimination ...

<p>a) $2x + y = 7$ ① $- x + y = 5$ ② SUBTRACT</p> $\begin{array}{r} x + 0 = 2 \\ \boxed{x = 2} \end{array}$ <p>Sub. $x = 2$ into ②</p> $\begin{array}{r} (2) + y = 5 \\ y = 5 - 2 \\ \boxed{y = 3} \end{array}$ <p>\therefore POI is $(2, 3)$.</p>	<p>b) $2x + 3y = 4$ ① $+ -2x - 7y = 16$ ② ADD</p> $\begin{array}{r} 0 - 4y = 20 \\ -4y = 20 \\ \frac{-4}{-4} \quad \frac{20}{-4} \\ \boxed{y = -5} \end{array}$ <p>sub $y = -5$ into ①</p> $\begin{array}{r} 2x + 3(-5) = 4 \\ 2x - 15 = 4 \\ 2x = 4 + 15 \\ \frac{2x}{2} = \frac{19}{2} \quad \boxed{x = \frac{19}{2}} \end{array}$ <p>\therefore POI is $(\frac{19}{2}, -5)$</p>
<p>Rearrange first so the x's and y's line up!</p> <p>c) $5y = -3x + 14$ ① $3x + 5y = 14$ $2x - 5y = 1$ ②</p> <p>ADD</p> $\begin{array}{r} 3x + 5y = 14 \\ 2x - 5y = 1 \\ \hline 5x + 0 = 15 \\ 5x = 15 \\ \frac{5}{5} \quad \frac{15}{5} \\ \boxed{x = 3} \end{array}$ <p>Sub. $x = 3$ into ②</p> $\begin{array}{r} 2(3) - 5y = 1 \\ 6 - 5y = 1 \\ -5y = 1 - 6 \\ -5y = -5 \\ \frac{-5}{-5} \quad \frac{-5}{-5} \\ \boxed{y = 1} \end{array}$	<p>Rearrange first so the x's and y's line up!</p> <p>d) $-2y + x = -19$ ① $5x = -2y + 1$ ② $\rightarrow 2y + 5x = 1$ ③</p> $\begin{array}{r} -2y + x = -19 \\ + 2y + 5x = 1 \\ \hline 0 + 6x = -18 \\ 6x = -18 \\ \frac{6}{6} \quad \frac{-18}{6} \\ \boxed{x = -3} \end{array}$ <p>Sub $x = -3$ into ①</p> $\begin{array}{r} -2y + (-3) = -19 \\ -2y - 3 = -19 \\ -2y = -19 + 3 \\ -2y = -16 \\ \frac{-2}{-2} \quad \frac{-16}{-2} \\ \boxed{y = 8} \end{array}$ <p>\therefore POI is $(-3, 8)$</p>