

Barabasi “Bose-Einstein Condensation in (so called) ‘Complex’ -Networks” **Rediscovery** of Siegel Artificial-Neural-Networks
 “EUREKA” + “SHAZAM” Optimizing Optimization-Problems Optimally (OOPO) Automatic-Mathematical-Catastrophe
 (“AUTMATHCAT”) Crossover from Slow Memory-Hogging “Simulated-Annealing” + “Boltzmann-Machine” to “Bose-Einstein
 CONDENSATION Machine”

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“FUZZYICS”[®]™

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@ La Jolla Institute for Biochemopsychotechnoinformaticoscientifico(so called)”complexity”...-Babble Spin-Doctoring Media-Hype

P.-R. “Bushwaaaaah” Disambiguation (LaJ-B...A...D)

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Fuzzy-Logic/Physics “FUZZYICS” “Fuzzycity” Optimizing Optimization-Problems Optimally (OOPO) of Neural-Networks (N-N’s) Via
Quantum-Statistics Crossover Equivalence to Switching-Function Sigmoidal→**Anti**-Sigmoidal Crossover Equivalence to “Noise”
 Power-Spectrum Crossover “Noise-‘Induced’/ ‘Driven’-Phase-Transitions (NIT’s) **Vast-Acceleration Control** Via “NIT-Picking”:
 “Eureka” and “Shazam” N-N *Bose-Einstein Condensation Automatic Optimality*

Horsthemke-Lefever-Moss-McClintock-Hongler-Siegel-...) “‘noise’-‘induced’/‘driven’/ concomitance phase-transition” (“NIT”) between power-spectrum critical-exponents: $P(\omega)=[“1”/\omega^{n=0}\text{-White}]\text{-to-}\rightarrow P(\omega)=(...“1”/\omega^{\frac{1.000...}{...}}\text{-}\underline{\text{Hyperbolicity}}...)$, with *control* (“NIT-picking”) implementation *two-step* application **vastly-accelerates** neural-network (N-N) inefficiency. “Eureka”: by-rote sigmoid switching-function $1/[1+e^{-E/T}]=1/[1+e^{-E/T}]$ (Lipmann-Siegel) identification as *Fermi-Dirac* (F-D): $1/[e^{\frac{h\omega}{kT}}+1]=1/[e^{E/T}+1]$ *quantum-statistics exactly-wrong* (Pauli exclusion-principle/Hund’s-rule) **automatic non-optimal local-minima trapping** (a.k.a. “chemical-elements”). *Sign-change/crossover to exact-opposite Bose-Einstein (B-E) quantum-statistics* (F-D): $1/[e^{\frac{h\omega}{kT}}+1]=1/[1+e^{-E/T}]=1/[1+e^{-E/T}]\text{-crossover}\rightarrow$ (B-E): $1/[e^{\frac{h\omega}{kT}}-1]=1/[e^{E/T}-1]$ equivalence to *anti-sigmoidal switching-function* $1/[1+e^{-E/T}]\text{-crossover}\rightarrow 1/[-1+e^{-E/T}]$ **completely-avoids** such inefficiency via Siegel quantum-statistics low-argument/infra-red ($E \ll T$)-limit $e^{E/T}$ Taylor/power-series-expansion: (F-D): $1/[e^{\frac{h\omega}{kT}}+1]=1/[1+e^{-E/T}]\cong 1/[1+[1+(E/T)+...]]\cong 1/[2+(E/T)]\cong 1/2\cong [“1”/\omega^{n=0}\text{-White}]\text{-crossover}\rightarrow$ (B-E): $1/[e^{\frac{h\omega}{kT}}-1]=1/[-1+e^{-E/T}]\cong 1/[1+[1+(E/T)+...]]\cong 1/(E/T)\cong “1”/E=(...“1”/\omega^{\frac{1.000...}{...}}\text{-}\underline{\text{Hyperbolicity}}...)$. “Shazam”: *infinite-numerator-limit*: $\lim_{\# \rightarrow \infty} \{ \#/[e^{\frac{h\omega}{kT}}-1] \} = \lim_{\# \rightarrow \infty} \{ \#/[-1+e^{-E/T}] \} \cong \lim_{\# \rightarrow \infty} \{ \# / E \} = \lim_{\# \rightarrow \infty} \{ (... \# / \omega^{\frac{1.000...}{...}}\text{-}\underline{\text{Hyperbolicity}}...) \} \cong d(w-0)$ effects N-N *Bose-Einstein Condensation automatic optimality*! (versus both Hsu’s long-predicted/never-implemented accidentally/partially Demuth-Beale/Matlab-NN-toolbox (only 5×10^3) Gaussian- $2^{-x \cdot x}$!)

Barabasi-Bianconi[Phys. Rev. Lett. 86, 24, 5632 (2001)] (BB) “Bose-Einstein Condensation in (so called) ‘Complex’ -Networks” is manifestly-demonstrated to be a **rediscovery** of Siegel “EUREKA” + “SHAZAM” **purposeful** Bose-Einstein Condensation **of** artificial neural-networks (ANNs) via a Horsthemke-Lefever[Noise Induced Phase-Transitions, Springer (1983)]-Moss-McClintock[Noise in Physical-Systems, (1990)]-Hongler[Chaotic and Stochastic Behavior in Automatic Production Lines, Springer (1994)]-Siegel[Symp. on Fractals..., M.R.S. Fall Mtg., Boston (1989)-5 papers!] “(so called) ‘noise’-induced/driven phase-transition” (“NIT”) via *control* “NIT-picking” to replace slow cumbersome “simulated-annealing” + “Boltzmann-machine” with a “Bose-Einstein Condensation (BEC)-machine” to force ANN from local nonoptimal-minima to the global optimum-minimum (if one exists), to optimize optimization-problems optimally (OOPO).

Subsequently, the Demuth-Beale Mathworks Matlab ANN-Toolbox achieved same by

Barabasi-Bianconi (BB) “Bose-Einstein Condensation *in* (so called) ‘Complex’-Networks”/Random-Graphs Summary and Metamorphosis to Siegel “Bose-Einstein Condensation *of* (so called) ‘Complex’-Networks”

Barabasi-Bianconi[Phys. Rev. Lett. 86, 24, 5632 (2001)] (BB) “Bose-Einstein Condensation *in* (so called) ‘Complex’-Networks” is summarized and its metamorphosis to a *rediscovery* of Siegel “Bose-Einstein Condensation *of* (so called) ‘Complex’-Networks” detailed.

Barabasi-Bianconi[Phys. Rev. Lett. 86, 24, 5632 (2001)] (BB) “Bose-Einstein Condensation *in* (so called) ‘Complex’-Networks” Summary

In detail, Barabasi-Bianconi[Phys. Rev. Lett. 86, 24, 5632 (2001)] (BB) “Bose-Einstein Condensation *in* (so called) ‘Complex’-Networks” is both summarized, critiqued, and identified as a metamorphosis of/ relative to/ vis a vis much-earlier original Siegel[Symp. on Fractals..., M. R. S. Fall Mtg., Boston (1989)-5-papers!; Schrodinger Centenary Symp., Imperial College, London (1987); I. B. M. (a.k.a. “Reich-III”) Conf. On Computers and Mathematics, Stanford (1986)] “Bose-Einstein condensation *of* (so called) ‘Complex’-Networks”.

BB abstract emphasizes for their object of study, (so called) “complex”-networks/random-graphs, hence their results, universality:

- Lawrence-Giles[Nature (London) 400, 107 (1999)] World Wide Web (www) site competition for URLs to enhance their visibility,
- Kermin[J. Evol. Econ. 4, 339 (1997)] business world company competition for links to consumers,
- Redner[Euro. Phys. J. B, 4, 131 (1998)] scientific-community scientists and publications competition for citations as a (false!) measure of their impact on “the” field (typical B. U. - B. S.!),

Common-feature identified is Lawrence-Giles-Redner- Adamic-Huberman[Science 287, 2115 (2000)]-Albert-Jeong-Barabasi [Nature (London) 401, 130 (1999)]-Watts-Strogatz[Nature (London) 393, 440 (1998)] “nodes (so called) ‘self-organization’ (media-hype P. R. spin-doctoring “bushwaaah!” into (so called) ‘complex’-networks/random-graphs, whose ‘topology and evolution ‘reflect’ the dynamics (dynamics = time-dependence *is* evolution!) and outcome of this ‘competition’ (a.k.a. (so called) ‘frustration’ (another trendy Irlon-Anderson-Pines-Laughlin-Frauenfelder...-‘ICAM’ [New Scientist 32 (6/11/2001)] buzzword media-hype P.R. spin-doctoring bushwaaah!; known long ago by so very many: Cohen[in Transition-Metal Magnetism, Fermi School in Physics, T. Moriya ed., Academic (1967)]-Moriya[ibid]-Penn[Phys. Rev. ??? (~1966)]-Siegel-Kemeny[Doctoral Dissertation, M. S. U. (1970); Phys. Stat. Sol.: (b) 50, 593 (1972); (b) 55, 817 (1973); J. Mag. Mag. Mtls. (1976-1980) - many-papers; Mag. Lett. (1980) -2-papers!;...]”.

BB claim to show, despite nonequilibriumness and irreversibility, that evolving/dynamic networks/random-graphs can be “1:1-mapped” onto an equilibrium ((so called) “complex”/evolving-network/random-graph nodes/vertices/entities corresponding to quantum energy-levels, with links corresponding to particles) Bose-gas, and in doing so, are actually *rederiving* a central portion of Siegel[Symp. on Fractals..., M. R. S. Fall Mtg., Boston (1989)-5-papers!; Schrodinger Centenary Symp., Imperial College, London (1987); I. B. M. (a.k.a. “Reich-III”) Conf. On Computers and Mathematics, Stanford (1986)] “Synergetics Paradigm & Dichotomy” (S.P.D.) “**FUZZYICS**” **INEVITABILITY -WEB**, and Siegel[(1998); Am. Math. Soc. Mtgs. (1998-2000); SIAM Ann. Mtg., San Diego (2001); Am. Math. Soc. Ann. Mtg., San Diego (2002)] ostensibly “pure-mathematics” DIGITS’ “NeWBe”-law inter-digit (*on average*) statistical logarithmic-correlations INVERSION to *only Bose-Einstein quantum-statistics physics!*, (DIGITS in decimal-number (so called) “complex”/evolving-network/random-graph nodes/vertices/entities corresponding to quantum energy-levels ‘spin(e)less-boZos’ (SoBs)”, with links ((on average) inter-digit statistical logarithmic-interactions) corresponding to particles), wherein decimal-numbers are a DIGIT-gas with (*on average*) inter-digit statistical logarithmic-correlations caused by (*on average*) inter-digit statistical logarithmic-interactions, necessarily in the dual-integral-transform-space inverse (\underline{k} , ω)-space(s) Hubbard-like Hamiltonian.

BB’s “1:1-mapping” predicts common-sense epithets characterizing competition/(so called)“frustration”: “winner takes all”, “fit get rich” (FGR), “first mover advantage” “emerging”(another/still more media-hype P.R. spin-doctoring buzzword bushwaaah!) naturally as topologically and thermodynamically distinct-phases of underlying (so called)“complex”/evolving-network/random-graph.

BB in particular predict (so called)“complex”/evolving-network/random-graph **Bose-Einstein CONDENSATION** (BEC), in which a single-node/vertex/entity captures a macroscopic-fraction of links.

BB, falling back upon “specificity-of-(so called)complexity” (SoC)-tactics:..., models:..., here their fitness-model[Barabasi-Bianconi, Europhys. Lett. - to be pub.] of a (so called) “complex”/evolving-network/random-graph growing by new nodes/ vertices/ entities acquisition, their generic (SoC)-tactics:..., model,... of:

- new webpages creation,
- new companies emergence,

or

- new papers publication.

Nodes acquisition of links rate can vary widely, as Adamic-Huberman[Science 287, 2115 (2000)] www-network, and Redner [Euro. Phys. J. B, 4, 131 (1998)] citation-networks and economic-networks measurements ascertain.

BB assign a fitness-parameter \mathbf{h} , representing nodes'/vertices'/entities' different-ability to compete for/capture links, from a fitness-parameter distribution $\mathbf{r}(\mathbf{h})$, to account for differences in, generically:

- webpages' contents
- products' quality
- companies' marketing,
- a publications' findings importance.

New-node'/vertex'/entity's interconnection one of its m links to a network's/graph's already-present node/vertex/entity i probability Π_i depends on links-number k_i and node/vertex/entity-fitness \mathbf{h}_i via $\Pi_i = \frac{\mathbf{h}_i}{\sum_l \mathbf{h}_l k_l}$, summarizing Barabasi-Albert-

Jeong [Science 286, 509 (1999); Physica 281A, 69 (2000)] tendency for new-nodes/vertices/entities to preferentially link to higher- k (links-number) nodes/vertices/entities, most simply possible:

- connecting to more-visible websites,
- favoring more-established companies,
- citing more-cited papers,

and with larger node/vertex/entity-fitness \mathbf{h}_i :

- connecting to better-content websites,
- favoring better-products and better-sales-practices companies,
- citing more-novel-results papers.

Node/vertex/entity-fitness \mathbf{h}_i and links-number k_i jointly determine node/vertex/entity attractiveness and evolution/dynamics.

Crucial “1:1-mapping” to **only Bose**-gas dominated by **only Bose-Einstein quantum-statistics** is in several steps:

- (1) assign to each node/vertex/entity an energy \mathbf{e}_i determined by its node/vertex/entity-fitness \mathbf{h}_i via $\mathbf{e}_i = -\frac{1}{b} \log \mathbf{h}_i$,

inter-nodes i and j , with respectively: energies \mathbf{e}_i and \mathbf{e}_j , and fitnesses \mathbf{h}_i and \mathbf{h}_j , link corresponds to two non-interacting-particles on energy-levels \mathbf{e}_i and \mathbf{e}_j . Adding a new node/vertex/entity to a network/random-graph corresponds to adding a new energy-level \mathbf{e}_i and $2m$ particles. Of these $2m$, m occupy energy-level \mathbf{e}_i (corresponding to m outgoing links possessed by node i) versus the other m being distributed among the other energy-levels (representing links pointing to existing m -nodes/vertices/entities),

with particle landing on level i probability $\Pi_i = \frac{\mathbf{h}_i}{\sum_l \mathbf{h}_l k_l}$. [deposited particles, forbidden to jump to other energy-levels, are inert].

Each-node/vertex/entity/energy-level added at time t_i with energy \mathbf{e}_i is characterized by occupation-number $k_i(\mathbf{e}_i, t, t_i)$ denoting links-number/particles a node/vertex/entity/energy-level occupies at time t .

Rate at which energy-level/node/vertex/entity \mathbf{e}_i acquires new particles/links-number k_i is $\frac{\mathcal{I} k_i(\mathbf{e}_i, t, t_i)}{\mathcal{I} t} = m \frac{e^{-b\mathbf{e}_i} k_i(\mathbf{e}_i, t, t_i)}{Z_t}$

in terms of partition-function $Z_t \equiv \sum_{j=1}^t e^{-b\mathbf{e}_j} k_j(\mathbf{e}_j, t, t_j)$.

BB assume each-node/vertex/entity “**increases its connectivity**” [meaning its **topological-connectivity dimension** $d_T^C \equiv (2 \cdot \text{genus} + 1) \equiv (2 \cdot g + 1)$ lower-bound on upper-bounded by geometric-embedding dimension $d_G^E \equiv d^s = (d^s + d^t) = (d^s + 1)$ **lower-bound increase** $\Delta d_T^C \equiv (2 \cdot \Delta \text{genus} + 1) \equiv (2 \cdot \Delta g + 1) \leq D_{\text{FRACTAL}} \leq d^{st} \equiv (d^s + d^t) = (d^s + 1)$] by a power-law $k_i(\mathbf{e}_i, t, t_i) = m \left(\frac{t}{t_i} \right)^{f(\mathbf{e}_i)}$ in terms on an energy-dependent dynamic-exponent $f(\mathbf{e})$.

Randomly-chosen node/vertex/entity-fitness \mathbf{h} from node/vertex/entity-fitness - distribution $\mathbf{r}(\mathbf{h})$ causes energy-levels/ nodes/ vertices/entities to be chosen from a causes energy-levels/ nodes/ vertices/entities - distribution $g(\mathbf{e}) = b\mathbf{r}(e^{-b\mathbf{e}})e^{-b\mathbf{e}}$, averaging

over which determines partition-function $Z_t \equiv \sum_{j=1}^t e^{-be_j} k_j(\mathbf{e}_j, t, t_j)$ as average partition-function

$$\langle Z_t \rangle = \int d\mathbf{e} g(\mathbf{e}) \int_1^t dt_0 e^{-be_i} k(\mathbf{e}, t, t_0) = \frac{m}{z} t [1 + O(t^{-a})] \text{ in terms of inverse-fugacity } \frac{1}{z} = \int d\mathbf{e} g(\mathbf{e}) \frac{e^{-be}}{1-f(\mathbf{e})} \text{ and } \mathbf{a} = \min_e [1-f(\mathbf{e})] > 0.$$

Since fugacity $z = \frac{1}{\int d\mathbf{e} g(\mathbf{e}) \frac{e^{-be}}{1-f(\mathbf{e})}} > 0$ is positive, for any finite-temperature $\mathbf{b} \neq 0$, BB introduce a *chemical-potential*

$$\mathbf{m} \text{ as } e^{bm} \equiv z = \frac{1}{\int d\mathbf{e} g(\mathbf{e}) \frac{e^{-be}}{1-f(\mathbf{e})}} > 0, \text{ i.e. as } \mathbf{m} \equiv \frac{1}{\mathbf{b}} \ln z = \frac{1}{\mathbf{b}} \ln \left[\frac{1}{\int d\mathbf{e} g(\mathbf{e}) \frac{e^{-be}}{1-f(\mathbf{e})}} \right] > 0 \text{ permitting rewriting of}$$

average partition-function $\langle Z_t \rangle = \int d\mathbf{e} g(\mathbf{e}) \int_1^t dt_0 e^{-be_i} k(\mathbf{e}, t, t_0) = \frac{m}{z} t [1 + O(t^{-a})]$ and inverse-fugacity

$$\frac{1}{z} = \int d\mathbf{e} g(\mathbf{e}) \frac{e^{-be}}{1-f(\mathbf{e})} \text{ together as } e^{-bm} = \lim_{t \rightarrow \infty} \frac{\langle Z_t \rangle}{mt}, \text{ which self-consistently solves energy-level/node/vertex/entity } \mathbf{e}_i$$

acquires new particles/links-number k_i acquisition-rate continuum-equation $\frac{\mathbb{I} k_i(\mathbf{e}_i, t, t_i)}{\mathbb{I} t} = m \frac{e^{-be_i} k_i(\mathbf{e}_i, t, t_i)}{Z_t}$ yielding solution

of assumed each-node/vertex/entity/ energy-level “*connectivity-increase*” [meaning its *topological-connectivity dimension* $d_T^C \equiv (2 \cdot \text{genus} + 1) \equiv (2 \cdot g + 1)$ lower-bound on upper-bounded by geometric-embedding dimension $d_G^E \equiv d^s = (d^s + d^f) = (d^s + 1)$]

power-law form $k_i(\mathbf{e}_i, t, t_i) = m \left(\frac{t}{t_i} \right)^{f(\mathbf{e}_i)}$ with dynamical-exponent $f(\mathbf{e}) = e^{-b(e-m)}$, which combined with

$$\frac{1}{z} = \int d\mathbf{e} g(\mathbf{e}) \frac{e^{-be}}{1-f(\mathbf{e})} \text{ yields chemical-potential as solution of } I(\mathbf{b}, \mathbf{m}) = \int d\mathbf{e} g(\mathbf{e}) \frac{e^{-be}}{e^{b(e-m)} - 1} = 1.$$

BB stress the properties of just-above system that make it unsuitable to be an equilibrium Bose-gas:

- particles’/links’-number inertness is a nonequilibrium-feature,

versus quantum-gas particles’ inter-level/node/vertex/entity jumps causing a temperature-driven equilibrium,

- both eligible energy-levels/nodes/vertices/entities and populating particles/links-number increase *linearly* in time

[“**FUZZYICS**” (relative)-1=time-(...GLOBALITY...) asymptotic-limit antipode],

versus quantum-system fixed system-size [“**FUZZYICS**” (relative)-[LOCALITY] asymptotic-limit antipode].

Yet $I(\mathbf{b}, \mathbf{m}) = \int d\mathbf{e} g(\mathbf{e}) \frac{e^{-be}}{e^{b(e-m)} - 1} = 1$ indicates that in $(t \rightarrow \infty)$ thermodynamic-limit their BB “fitness-model” SoC-tactics

“1:1-maps” onto an *only Bose-gas* obeying *only Bose-Einstein quantum-statistics*!

Since in an ideal-gas of unit-volume ($v = 1$) Huang[Statistical-Mechanics, Wiley (1987)] states a normalization sum-rule

$\int d\mathbf{e} g(\mathbf{e}) n(\mathbf{e})$ in terms of energy-level/node/vertex/entity occupation-number/density-of-states in energy/quantum-statistic $n(\mathbf{e})$,

BB’s just-above derived fitness-model SoC-tactics inspired inert-gas $I(\mathbf{b}, \mathbf{m}) = \int d\mathbf{e} g(\mathbf{e}) \frac{e^{-be}}{e^{b(e-m)} - 1} = 1$ yields

$$\text{only Bose-Einstein quantum-statistics } n(\mathbf{e}) = \frac{1}{e^{b(e-m)} - 1}.$$

Thus BB conclude that their evolving/dynamic-network/random-graph “1:1-maps” onto **only Bose-Einstein quantum-statistics**, the evolving/dynamic-network/random-graph irreversibility and inertness are resolved by the asymptotic-distribution’s stationarity, permitting in $t \rightarrow \infty$ thermodynamic-limit occupation-numbers/link-numbers to obey **only Bose-Einstein quantum-statistics**.

Bose-Einstein quantum-statistics uniquely admit possibility of **Bose-Einstein CONDENSATION**.

$$\text{BB solutions: } k_i(\mathbf{e}_i, t, t_i) = m \left(\frac{t}{t_i} \right)^{f(\mathbf{e}_i)}, \quad \langle Z_t \rangle = \int d\mathbf{e} g(\mathbf{e}) \int_1^t dt_0 e^{-be_i} k(\mathbf{e}, t, t_0) = \frac{m}{z} t [1 + O(t^{-a})], \text{ and } f(\mathbf{e}) = e^{-b(\mathbf{e}-m)}$$

can exist only when there exists a chemical-potential satisfying $I(\mathbf{b}, m) = \int d\mathbf{e} g(\mathbf{e}) \frac{e^{-be}}{e^{b(\mathbf{e}-m)} - 1} = 1$.

But this exhibits a maximum at $m = 0$, i. e. when $I(\mathbf{b}, m) = \int d\mathbf{e} g(\mathbf{e}) \frac{e^{-be}}{e^{b(\mathbf{e}-m)} - 1} < 1$ (for given \mathbf{b} and $g(\mathbf{e})$) there is no solution, a well-known signature of **Bose-Einstein CONDENSATION**, indicating finite-fraction $n_0(\mathbf{b})$ of particles/links condense into lowest energy-level/node/vertex/entity.

Due to mass-conservation at time t, there are t energy-levels/nodes/vertices/entities populated by 2mt particles/links, i. e.

$$2mt = \sum_{t_0=1}^t k(\mathbf{e}_{t_0}, t, t_0) = mt + mtI(\mathbf{b}, m), \text{ such that, when } I(\mathbf{b}, 0) = I(\mathbf{b}, m=0) = \int d\mathbf{e} g(\mathbf{e}) \frac{e^{-be}}{e^{b(\mathbf{e}-0)} - 1} < 1,$$

$$2mt = \sum_{t_0=1}^t k(\mathbf{e}_{t_0}, t, t_0) = mt + mtI(\mathbf{b}, m) \text{ is replaced by } 2mt = mt + mtI(\mathbf{b}, m) + n_0(\mathbf{b}) \text{ with } \frac{n_0(\mathbf{b})}{mt} = 1 - I(\mathbf{b}, 0).$$

Lowest energy-level/node/vertex/entity occupancy corresponds to links-number/particles of energy-level/node/vertex/entity with maximal-fitness in their BB SoC-tactics fitness-model. Thus BB conclude that their **Bose-Einstein CONDENSATION** corresponds to non-zero $n_0(\mathbf{b})$ emergence represents their evolving/dynamical-networks/random-graphs “winner-takes-all” phenomenon, the fittest energy-level/node/vertex/entity/energy-level acquiring a finite-fraction of links/particles, **independent** of network-size/radius/extent/scale! [“**FUZZYICS**” (relative)-(…GLOBALITY…) asymptotic-limit antipode].

BB then predict existence of three “distinct” phases characterizing (so called) “complex”/random-graphs/networks-dynamics/evolution [**all equivalently identically** “**FUZZYICS**” (relative)-(…GLOBALITY…) asymptotic-limit antipode!]:

• (a) **Scale-free/Invariance**,

[“**FUZZYICS**” (relative)-(…**SCALE**-Invariance Symmetry -**RESTORING**…) asymptotic-limit antipode].

versus

• (b) “Fit-Get-Rich” (FGR),

[“**FUZZYICS**” (relative)-[LOCALITY] asymptotic-limit antipode].

“versus”

• (c) **Bose-Einstein CONDENSATION**.

[“**FUZZYICS**” (relative)-(… $\frac{1}{w^{1.000\dots}}$ -**HYPERBOLICITY**…) asymptotic-limit antipode].

(more correctly [“**FUZZYICS**” (relative)-(… $\lim_{\# \rightarrow \infty} \frac{\#}{w^{1.000\dots}} = d(w-0)$ -**HYPERBOLICITY**…) asymptotic-limit antipode])!

BB’s SoC-tactics has *blinded* them to the reality that all three phases are **equivalent**, and **caused** by **only EVEN**-integer degrees-of-freedom/spacetime-dimensionality, via Siegel “**FUZZYICS**”!!!

BB claim three “distinct”-phases, which the “Parsimony-of-Dichotomy” (PoD)-**STRATEGY** of Siegel S.P.D. “**FUZZYICS**” **automatically integrates** (a) to (c), *versus* exact-opposite (b), *together optimally*!:

• (a) **Scale-free/Invariance** (so called) “phase”:

[Siegel S.P.D. “**FUZZYICS**” (relative)-(…GLOBALITY…) asymptotic-limit antipode on *different* S.P.D. “**FUZZYICS**” logic-levels!: here for (a) *both the equivalent*]:

when all-nodes/vertices/entities/energy-levels have same “fitness”, i. e. homogeneity, i. e. [Siegel S.P.D. “**FUZZYICS**” (relative)-(…GLOBALITY…) asymptotic-limit antipode on *different* S.P.D. “**FUZZYICS**” logic-levels!: here for (a) *both the equivalent*]: , i. e.

$$\mathbf{r}(\mathbf{h}) = \mathbf{d}(\mathbf{h} - 1) \quad i.e. \quad [g(\mathbf{e}) = \mathbf{d}(\mathbf{e})], \text{ their “fitness”-model “first-mover-wins”}$$

SoC-tactics reduce to their [Science, 286, 509 (1999); Physica 281A, 69 (2000)]

Scale-free/Invariance model SoC-tactics, introduced to account for diverse-systems power-law connectivity-distribution!:

- www [Albert-Jeong-Barabasi, Nature (London) 401, 130 (1999), Albert-Barabasi, Phys. Rev. Lett. 85, 5234 (2000)],
- coauthorship-networks[Newman, con.-mat./0011144; Barabasi-Jeong-Neda-Ravasz-Schubert-Vicsek, cond.-mat./0104162],
- Internet[Faloutsos x 3, Comput. Commun. Rev. 29, 251 (1999); Barabasi-Albert-Jeong, Nature (London) 406, 378 (2000)],
- citation-networks[Redner, Euro. Phys. B4, 131 (1998)].

Oldest-nodes/vertices/entities/lowest energy-levels acquire most-links/particles, (historical-precedence), “first-mover-wins” SoC-

tactics, has $f(\mathbf{e}) = e^{-b(\mathbf{e}-m)}$ predicting $f(\mathbf{e}) = \frac{1}{2}$, i. e. via $k_i(\mathbf{e}_i, t, t_i) = m \left(\frac{t}{t_i} \right)^{f(\mathbf{e}_i)}$, all nodes exhibit **connectivity-increase**

[**topological-connectivity dimensionality lower-bound increase**:

$$\Delta d_T^C \equiv (2 \cdot \Delta genus + 1) \equiv (2 \cdot \Delta g + 1) \leq D_{FRAC TAL} \leq d^{st} \equiv (d^s + d^t) = (d^s + 1)$$

of form:

$$\Delta d_T^C(t) \equiv (2 \cdot \Delta genus \sim t^{1/2} + 1) \equiv (2 \cdot \Delta g \sim t^{1/2} + 1) \leq D_{FRAC TAL} \leq d^{st} \equiv (d^s + d^t) = (d^s + 1),$$

i. e.

$$\Delta d_T^C(t) \equiv (2 \cdot \Delta genus \sim t^{1/2} + 1) \equiv (2 \cdot \Delta g \sim t^{1/2} + 1) \sim t^{1/2},$$

i. e. the oldest-nodes/vertices/entities/energy-levels with the smaller t_i have the larger k_i .

But the oldest and “richest” node/ vertex/ entity/energy-level is *not* the *absolute* winner, since its share of links/particles

$\frac{k_{\max}(t)}{mt} \sim \frac{1}{t^{1/2}} \equiv t^{-1/2}$ decays to zero in the thermodynamic- $(t \rightarrow \infty)$ -limit: $\lim_{t \rightarrow \infty} \frac{k_{\max}(t)}{mt} \sim \lim_{t \rightarrow \infty} \frac{1}{t^{1/2}} \equiv \lim_{t \rightarrow \infty} t^{-1/2} = 0$, creating a

coexisting continuous-hierarchy of large-nodes/vertices/entities/energy-levels, such that the probability to have a [Barabasi -Albert-Jeong: Science 286, 509 (1999); Physica 281A, 69 (2000); Dorogovisev-Mendes-Samukhin, Phys. Rev. Lett. 85, 4633 (2000)]

k-links/particles per node/vertex/entity/energy-level, the “degree-distribution” exhibits a power-law decay: $P(k) \sim \frac{1}{k^3} \equiv k^{-3}$,

wherein: rewiring, ageing, and other local-processes [Siegel S.P.D. “**FUZZYICS**” (relative)-[LOCALITY] asymptotic-limit antipode] can modify scaling-exponents or introduce [Albert-Barabasi, Phys. Rev. Lett. 85, 5234 (2000); Dorogovisev-Mendes-Samukhin, Phys. Rev. Lett. 85, 4633 (2000); Amaral-Scala-Barthelemy -“Stanley”, Proc. Nat. Acad. Sci. (U.S.A) 97, 11,149 (2000); Krapivsky-Redner-Leyvraz, Phys. Rev. Lett. 85, 4629 (2000); Krapivsky-Redner, cond.-mat/0011094] links/particles-number k-cutoffs, versus leaving their claimed (so called) “phase” unchanged.

versus

- (b) “Fit-Get-Rich” (FGR) (so called) “phase”:

[Siegel S.P.D. “**FUZZYICS**” (relative)-[LOCALITY] asymptotic-limit antipode on *different* S.P.D. “**FUZZYICS**” logic-levels!]:

supposedly distinct “versus” **Scale-free/Invariance**(so called) “phase” (so called buzzword!) “emerges” when nodes/vertices/entities/energy-levels possess different-fitnesses, i. e. [Siegel S.P.D. “**FUZZYICS**” (relative)-[LOCALITY] asymptotic-limit antipode on *different* S.P.D. “**FUZZYICS**” logic-levels] , i. e. heterogeneity, and an equation exists

$$I(\mathbf{b}, \mathbf{m}) = \int d\mathbf{e} \ g(\mathbf{e}) \frac{e^{-be}}{e^{b(e-m)} - 1} = 1 \text{ having a solution. } \frac{k_{\max}(t)}{mt} \sim \frac{1}{t^{1/2}} \equiv t^{-1/2} \text{ which indicates that each node/vertex/}$$

entity/energy-level has a **connectivity-increase** in time:

[Siegel S.P.D. root-cause ultimate-origin at **0. Dimensionality/Degrees-of-Freedom Logic-Level O.**]

topological-connectivity dimensionality lower-bound increase:

$$\Delta d_T^C \equiv (2 \cdot \Delta \text{genus} + 1) \equiv (2 \cdot \Delta g + 1) \leq D_{\text{FRACTAL}} \leq d^{st} \equiv (d^s + d^t) = (d^s + 1)$$

of form:

$$\Delta d_T^C(t) \equiv (2 \cdot \Delta \text{genus} \sim t^{1/2} + 1) \equiv (2 \cdot \Delta g \sim t^{1/2} + 1) \leq D_{\text{FRACTAL}} \leq d^{st} \equiv (d^s + d^t) = (d^s + 1),$$

i. e.

$$\Delta d_T^C(t) \equiv (2 \cdot \Delta \text{genus} \sim t^{1/2} + 1) \equiv (2 \cdot \Delta g \sim t^{1/2} + 1) \sim t^{1/2},$$

i. e. the oldest-nodes/vertices/entities/energy-levels with the smaller t_i have the larger k_i]

but the [Bianconi-Barabasi, Europhys. Lett. (to be pub.)] dynamic-exponent is larger for highest-fitness nodes/vertices/entities/energy-levels, allowing for [Adamic-Huberman, Science 287, 2115 (2000)] fitter-nodes/vertices/entities/energy-levels to join the network at some later time, and to surpass the older but less-fit nodes/vertices/entities/energy-levels by acquiring links/particles at higher-rates, this claimed (so called) “phase” describing their [BB] “get-rich-quick” phenomenon in which, with time, the fitter prevails. But, even though there exists a clear-winner similar to their **Scale-free/Invariance**(so called) “phase”, their fittest-node’s/vertex’s/entity’s/energy-level’s share of all links/particles decreases to zero in thermodynamic- $(t \rightarrow \infty)$ -limit.

Since $f(\mathbf{e}) = e^{-b(e-m)} < 1$, the fittest-node’s/vertex’s/entity’s/energy-level’s **relative-connectivity** decreases as

$$\frac{k(\mathbf{e}_{\min}, t)}{mt} \sim t^{f(\mathbf{e}_{\min})-1}, \text{ such competition again leading to a hierarchy of a few larger-“hubs” accompanied by many less-connected}$$

nodes/vertices/entities/energy-levels.

[Siegel S.P.D. “**FUZZYICS**” (relative)-[LOCALITY] asymptotic-limit antipode on **different** S.P.D. “**FUZZYICS**” logic-levels!].

such that [Bianconi-Barabasi, Europhys. Lett. (to be pub.)] $P(k; g[r(h)]) \sim \frac{1}{k^{g[r(h)]}} \equiv k^{-g[r(h)]}$ holds.

“versus”

• (c) **Bose-Einstein CONDENSATION** (so called) “phase”:

[“**FUZZYICS**” (relative)-(... $\frac{1}{W^{1.000...}}$ -**HYPERBOLICITY**...) asymptotic-limit antipode].

(more correctly [“**FUZZYICS**” (relative)-(... $\lim_{\# \rightarrow \infty} \frac{\#}{W^{1.000...}} = d(w-0)$ -**HYPERBOLICITY**...) asymptotic-limit antipode])!

$$I(\mathbf{b}, \mathbf{m}) = \int d\mathbf{e} \ g(\mathbf{e}) \frac{e^{-be}}{e^{b(e-m)} - 1} < 1 \text{ inequality precludes any (BB) solutions:}$$

$$k_i(\mathbf{e}_i, t, t_i) \neq m \left(\frac{t}{t_i} \right)^{f(\mathbf{e}_i)}, \langle Z_i \rangle = \int d\mathbf{e} g(\mathbf{e}) \int_0^t dt_0 e^{-be_i} k(\mathbf{e}, t, t_0) \neq \frac{m}{z} t \left[1 + O(t^{-a}) \right], \text{ and } f(\mathbf{e}) \neq e^{-b(e-m)},$$

equalities could only exist only when there exists a chemical-potential satisfying $I(\mathbf{b}, \mathbf{m}) = \int d\mathbf{e} \ g(\mathbf{e}) \frac{e^{-be}}{e^{b(e-m)} - 1} = 1$, versus here

this exhibits a maximum at $\mathbf{m} = 0$, i. e. when $I(\mathbf{b}, \mathbf{m}) = \int d\mathbf{e} \ g(\mathbf{e}) \frac{e^{-b\mathbf{e}}}{e^{b(\mathbf{e}-\mathbf{m})} - 1} < 1$ (for given \mathbf{b} and $g(\mathbf{e})$) there is no solution, a well-known signature of **Bose-Einstein CONDENSATION**, indicating finite-fraction $n_0(\mathbf{b})$ of particles/links condense into lowest energy-level/node/vertex/entity.

Inter-node/vertex/entity/energy-level competition for links/particles favors largest-fitness - nodes/vertices/entities/energy-levels, those attracting a finite-fraction $[n_0(\mathbf{b})]$ of links/particles-number. BB interpret this to mean that their **Bose-Einstein CONDENSATION** (so called) “phase” “predicts” a “real” “winner-take-all” phenomenon, wherein the fittest-node/vertex/entity/energy-level is not only the largest, but that which also acquires a finite-fraction of links/particles-number $\frac{n_0(\mathbf{b})}{nt} = 1 - [I(\mathbf{b}, 0) < 1] > 0$ despite continual-“emergence”/acquisition of new nodes/vertices/entities/energy-levels that compete for new links/particles acquisition.

BB claim to demonstrate a “FGR”- (so called) “phase” to **Bose-Einstein CONDENSATION** (so called) “phase” *phase-transition critical-phenomenon*.

But, with identification of BB “FGR”- (so called) “phase” as [“**FUZZYICS**” (relative)-[LOCALITY] asymptotic-limit antipode].

versus

BB **Bose-Einstein CONDENSATION** (so called) “phase” as [“**FUZZYICS**” (relative)-(... $\frac{1}{w^{1.000...}}$ -**HYPERBOLICITY**...) asymptotic-limit antipode].

(more correctly [“**FUZZYICS**” (relative)-(... $\lim_{\# \rightarrow \infty} \frac{1}{w^{1.000...}} = d(w - 0)$ -**HYPERBOLICITY**...) asymptotic-limit antipode])!,

But BB’s claimed ostensibly-disparate (so called) phases:

• (a) **Scale-free/Invariance** ,
[“**FUZZYICS**” (relative)-(...(**SCALE**-Invariance Symmetry -**RESTORING**...) asymptotic-limit antipode].

versus

• (b) “Fit-Get-Rich” (FGR) ,
[“**FUZZYICS**” (relative)-[LOCALITY] asymptotic-limit antipode].

versus

• (c) **Bose-Einstein CONDENSATION** .
[“**FUZZYICS**” (relative)-(... $\frac{1}{w^{1.000...}}$ -**HYPERBOLICITY**...) asymptotic-limit antipode],

(more correctly [“**FUZZYICS**” (relative)-(... $\lim_{\# \rightarrow \infty} \frac{1}{w^{1.000...}} = d(w - 0)$ -**HYPERBOLICITY**...) asymptotic-limit antipode])!

but/versus

• (a) **Scale-free/Invariance** ,
[“**FUZZYICS**” (relative)-(...(**SCALE**-Invariance Symmetry -**RESTORING**...) asymptotic-limit antipode],

at the S.P.D. “**FUZZYICS**” logic-levels:

I. Radius/Extent/Scale/... Logic-Level I.

and

IV. Symmetries/Invariances/Noether's-Theorem Conservation-Laws Logic-Level IV. star of possibilities

(most especially in particular here the:

SCALE-Invariance Symmetry-Restoring / Noether's-Theorem SCALE-4-Current Conservation-Law Logic-Level IV.)

exact equivalence to

• (c) *Bose-Einstein CONDENSATION*

[“**FUZZYICS**” (relative)-(… $\frac{1}{w^{1.000\dots}}$ -**HYPERBOLICITY**…) asymptotic-limit antipode],

(more correctly [“**FUZZYICS**” (relative)-(… $\lim_{\# \rightarrow \infty} \frac{\#}{w^{1.000\dots}} = d(w - 0)$ -**HYPERBOLICITY**…) asymptotic-limit antipode])!,

at the S.P.D. “**FUZZYICS**” logic-levels:

II. Power-Spectrum Logic-Level II.

and

III. Critical-Exponents Logic-Level III.

Thus BB's (so called) *phase-transition critical-phenomenon* is seen to be simply a restatement of the Siegel [Symp. on Fractals...., M. R. S. Fall Mtg., Boston (1989)-5-papers!; I. B. M. (a.k.a. Reich-III) Conf. On Computers and Mathematics, Stanford (1986); Schrodinger Centenary Symp., Imperial College, London (1987)] “automatic-mathematical-catastrophe” (“AUTMATHCAT”) CROSSOVER between the two asymptotic-limit antipodes, most easily seen in S.P.D. “**FUZZYICS**” tabular/list-format analysis!: (below)

BB demonstrate this “FRG” (so called) phase to *Bose-Einstein CONDENSATION* (so called) “phase” by assuming an energy-(fitness)-distribution class $g(\mathbf{e}) = Ce^q$ follows, with free-parameter q and energies/fitnesses chosen such that

$\mathbf{e} \in (0, \mathbf{e}_{\max})$, with normalization giving $C = \frac{(q+1)}{\mathbf{e}_{\max}^{q+1}}$, yielding a *Bose-Einstein CONDENSATION* criterion/condition:

$$\frac{(q+1)}{(\mathbf{e}_{\max})^{q+1}} \int_{\mathbf{e}_{\min}(t)}^{\mathbf{e}_{\max}(t)} \frac{x^q}{e^x - 1} dx < 1$$

where $\mathbf{e}_{\min}(t)$ is the lowest-energy-level/fittest-node/vertex/entity/energy-level existing in the network at time t .

Extension of integration-limits respectively to 0 and ∞ BB claim to find critical-temperature's lower-bound:

$$T_{BE} = \frac{1}{b_{BE}} > \frac{\mathbf{e}_{\max}}{[z(q+1)\Gamma(q+2)]^{1/(q+1)}} \equiv \mathbf{e}_{\max} [z(q+1)\Gamma(q+2)]^{-1/(q+1)}$$

BB's numerical-simulation SoC-tactics reveals a chemical-potential \mathbf{m} indicating a sharp-transition from positive $\mathbf{m} > 0$ to negative $\mathbf{m} < 0$ corresponding to “their” predicted *phase-transition critical-phenomenon* between “FGR” (so called) “phase” to *Bose-Einstein CONDENSATION* (so called) “phase”, i. e. between *most-connected* node's/vertex's/entity's/energy-level's relative occupation-number as a function of temperature. BB claim to find time-independence of ratio

$$\left[\frac{k_{\max}(t)}{mt} \right]_{\in \text{BOSE-EINSTEIN CONDENSATION}} = \frac{k_{\max}}{mt} \quad \text{indicating that largest-node/vertex/entity/energy-level maintains a finite-fraction of}$$

total-links/particles-number even as network continues to evolve/expand temporally, a signature of *Bose-Einstein CONDENSATION*!

Versus for $T < T_{BE} = \frac{1}{b_{BE}} > \frac{e_{\max}}{[z(q+1)\Gamma(q+2)]^{1/(q+1)}} \equiv e_{\max} [z(q+1)\Gamma(q+2)]^{-1/(q+1)}$ the most-connected

node/vertex/entity/energy-level gradually loses its share of links, $\left[\frac{k_{\max}(t)}{mt} \right] \sim t^?$.

Since real-networks exhibit temperature T-independent fitness-distribution $\mathbf{r}(\mathbf{h})$, thus real-networks' occupancy of either BB's "FGR (so called) "phase" or/versus BB's ***Bose-Einstein CONDENSATION*** (so called) "phase" is similarly temperature T-independent.

BB give as example, choosing $\mathbf{r}(\mathbf{h}) = (\mathbf{l} + 1)(1 - \mathbf{h})^{\mathbf{l}}$ and $\mathbf{l} > \mathbf{l}_{BOSE-EINSTEIN\ CONDENSATION} = 1$, BB find network ***Bose-Einstein CONDENSATION*** with temperature T vanishing from all topologically-relevant quantities.

[in Siegel S.P.D. "**FUZZYICS**", this would mean that:

[*topological-connectivity dimensionality lower-bound increase*:

$$\begin{aligned} \Delta d_T^C &\neq \Delta d_T^C(T) \equiv (2 \cdot \Delta genus + 1) \neq (2 \cdot \Delta genus(T) + 1) \equiv (2 \cdot \Delta g + 1) \neq (2 \cdot \Delta g(T) + 1) \\ &\leq D_{FRAC TAL} \leq d^{st} \equiv (d^s + d^t) = (d^s + 1) \end{aligned}$$

of form:

$$\begin{aligned} \Delta d_T^C(t) &\neq \Delta d_T^C(t; T) \equiv (2 \cdot \Delta genus \sim t^{1/2} + 1) \neq (2 \cdot \Delta genus(T) \sim t^{1/2} + 1) \equiv (2 \cdot \Delta g \sim t^{1/2} + 1) \neq (2 \cdot \Delta g(T) \sim t^{1/2} + 1) \\ &\leq D_{FRAC TAL} \leq d^{st} \equiv (d^s + d^t) = (d^s + 1) \end{aligned},$$

i. e.

$$\Delta d_T^C(t) \neq \Delta d_T^C(t; T) \equiv (2 \cdot \Delta genus \sim t^{1/2} + 1) \neq (2 \cdot \Delta genus(T) \sim t^{1/2} + 1) \equiv (2 \cdot \Delta g \sim t^{1/2} + 1) \neq (2 \cdot \Delta g(T) \sim t^{1/2} + 1) \sim t^{1/2}$$

].

Thus BB argue that temperature T is only a simple control-parameter in their SoC-tactics model, (rooted in their technically-simpler choice of defining $g(\mathbf{e}) \neq g(\mathbf{e}, T)$, but in their Fig. 2b inset, changing \mathbf{q} iso-T still does this, so T is *not* necessary), but whose "tuning" performs their *phase-transition critical-phenomenon*

[Siegel S.P.D. "AUTMATHCAT" CROSSOVER, but root-cause ultimate-origin (a la [Menger's, Dimensiontheorie, Teubner (1929)] dimension-theory) **0. Dimensionality/ Degrees-of-Freedom Logic-Level 0**, is *decidedly not* "just a simple control-parameter", but ***the root-cause ultimate-origin!!!!***].

BB close cryptically by referring to [Krapivsky-Redner-Leyvraz Phys. Rev. Lett. 85, 4629 (2000); P. Krapivsky and S. Redner, cond.-mat/0011094] prediction of a gelation-phenomenon for "nonlinear preferential attachment" $\Pi(k) \sim k^{m>1}$. In comparing this "gelation" vs. ***Bose-Einstein CONDENSATION*** in single-node/vertex/entity/energy-level success of links/particles-capture, BB conclude cryptically that ***Bose-Einstein CONDENSATION*** can exist only if fitness exists!(!?)

"**EUREKA**" and "**SHAZAM**" For Artificial Neural-Networks'

via A-NN ***BRILLOUIN-IZATION / FOURIER-IZATION (BoANN) / (FoANN)***:

BOSE-EINSTEIN CONDENSATION of "***BOSE-EINSTEIN MACHINE***" to

Optimize Optimization-Problems Optimally (OPO) "***NIT-PICKING***" CONTROL For the *Right-Reasons* via "**FUZZYICS**" S.P.D.

"**INEVITABILITY -WEB**" AUTOMATICALLY with ***OPTIMALITY Efficiency VIA QUANTUM-STATISTICS DICHOTOMY PARSIMONY-*** of-DICHOTOMY (PoD)-**STRATEGY** versus *Hobbling* Sigmoidal Switching-Function *Crutch* "Boltzmann-Machine" "Simulated-Annealing" *INEfficiency Useless Slow/Costly/Memory-Hogging Brute-Force Flailing-Away* "Specificity-of-Complexity" (SoC)-Tactics: Brillouin-ization (BoANN/ Fourier-ization(FoANN) /Bose-Einstein-ization (Condensation) (B-E-CoANN) of Artificial-Neural-Networks

Artificial neural-networks' (A-NN's) Achilles'-heel, the **wrong** sigmoidal switching-function, via "EUREKA" + "SHAZAM" softwares, without any radial-basis -functions, can be made to undergo "noise-induced/driven phase-transitions (NITs) which permit *control* via "NIT-picking" to effect forced quantum-tunneling to global-minimum (if such exists) via " Bose-Einstein **CONDENSATION**" to **automatically** optimize optimization-problems optimally (OOPO) with **optimality** via "FUZZYICS" Synergetics Paradigm & Dichotomy (S.P.D.) "INEVITABILITY_-WEB" list-format analysis!

Fuzzy-logic/physics "FUZZYICS" "fuzzycity" Optimizing Optimization-Problems Optimally (OOPO) of neural-networks (A-N-Ns) Via *quantum-statistics* crossover equivalence to switching-function sigmoidal→**Anti**-sigmoidal crossover equivalence to (so called) "noise" power-spectrum crossover "Noise-'Induced'/ 'Driven'-Phase-Transitions" (NIT's) **vast-acceleration control** via "NIT-Picking": "Eureka" and "Shazam" A-N-N *Bose-Einstein Condensation AUTOMATIC OPTIMALITY!*

Siegel[Symp. on Fractals, Scaling..., MRS Fall Mtg., Boston (1989)-5-papers !; I. B. M.(a.k.a. "Reich-III") Conf. On Computers and Mathematics, Stanford (1986); J. Noncryst. Sol. 40, 453 (1980); Aristotle Birthday Symposium on Mechanics and Physics, Thessaloniki (1990); Bull. A. P. S. March Mtgs.: Anaheim (1990); Indianapolis (1992);...] S.P.D. "FUZZYICS" **automatically** with **optimality** is, in list-format:

SYNERGETICS PARADIGM & DICHOTOMY(SPD) "COMMON-FUNCTIONING-PRINCIPLE"
PARSIMONY-of-DICHOTOMY (POD)-STRATEGY DIMENSIONALITY-DOMINATION (DD)-
INEVITABILITY

ROOT-CAUSE
ULTIMATE-ORIGIN
 (0.)
DIMENSIONALITY/
DEGREES-of-FREEDOM
LEVEL-0. LOGIC:

d-o-f = d st = <u>ODD</u> -INTEGER	AUTMATHCAT <------DIM-CAT-----> CROSSOVER via INTERMEDIATE CONTINUOUS INTERPOLATING FRACTIONAL FRACTAL-DIMENSIONALITY UNCERTAINTY FLUCTUATIONS d st = <u>ODD</u> -Z < D st < <u>EVEN</u> -Z = d st	<u>EVEN</u> -INTEGER = d st =d-o-f
--	--	--

cau β ses

cau β ses

cau β ses

(I.)
EXTENT/SCALE/RADIUS
LEVEL-I LOGIC:

(relative)	AUTMATHCAT <------DIM-CAT-----> CROSSOVER	(relative)
[BOUNDARYFUL]=[LOCALITY]		(...GLOBALITY...)= (...BOUNDARY <u>LESS</u> ...)
{ Kallen-Lehmann &/ representation-equivalence }		&/

(II.)
POWER-SPECTRUM

LEVEL-II LOGIC:

[“1”/ω⁰-WHITE/
FLAT/FUNCTIONLESS]

AUTMATHCAT
<-----DIM-CAT----->
CROSSOVER

(...”1”/ω^{1.000...} HYPERBOLICITY...) whose
frequency-*integral* defines at least *necessary*-
condition for so-called “complexity” as
Noether’s-theorem SCALE-4-current 4-
CONvergence /CONSERVATION:
(d/dω) [[∂_μJ^μSCALE = 0] (ω)] = 1/ω=(for
arbitrary base)= “1”/ω

&/||

&/||

(III.)
CRITICAL-EXPONENT
LEVEL-III LOGIC:

n = 0

AUTMATHCAT
<-----DIM-CAT----->
CROSSOVER

n = 1.000...

↑↑
↓↓

↑↑
↓↓

↑↑
↓↓

DIMENSIONALITY
DEGREES-of-FREEDOM -
INDEPENDENT
ALSO
ROOT-CAUSE
ULTIMATE-ORIGIN
(IV.)

NOETHER'S - THEOREM:
CONTINUOUS-LIE-GROUP
SCALE-INVARIANCE
SYMMETRY
LEVEL-IV. LOGIC:

SCALE - INVARIANCE
SYMMETRY - RESTORING

<-----CROSSOVER----->

SCALE - INVARIANCE
SYMMETRY - BREAKING

↑↑
causes
↓↓

↑↑
causes
↓↓

↑↑
causes
↓↓

∂_μJ^μSCALE = 0
SCALE-4-CURRENT
4-[CONVERGENCE]
4-[CONSERVATION]

whose frequency-*derivative* defines
at least *necessary*-condition for so-
called “complexity” as Noether’s-
theorem SCALE-4-current 4-
CONvergence/ CONSERVATION:
(d/dω) [[∂_μJ^μSCALE = 0] (ω)] = 1/ω
=(for arbitrary base)= “1”/ω

<-----CROSSOVER----->

0¹ ∂_μJ^μSCALE
SCALE-4-CURRENT
4-(... DIVERGENCE...)
4-(...NON-CONSERVATION...)

&

&

&

DIMENSIONALITY
DEGREES-of-FREEDOM -
INDEPENDENT
ALSO
ROOT-CAUSE
ULTIMATE-ORIGIN
(V.)
STAR-{SET}
OF
OTHER-POSSIBLE

NOETHER'S - THEOREM:
CONTINUOUS-LIE-GROUP
SYMMETRIES-SET
LEVEL-IV. LOGIC(S) : _____

_____ - INVARIANCES
 SYMMETRY - **RESTORINGS**
-SET

↑↑
 causes
 ↓↓

$\{\partial_\mu J^\mu \dots = 0\}$ -**SET**
 $\{ \dots\text{-}4\text{-CURRENTS}\}$ -**SET**
 $\{4\text{-[CONVERGENCES]}\}$ -**SET**
 $\{4\text{-[CONSERVATIONS]}\}$ -**SET**

<-----CROSSEOVERS----->

↑↑
 causes
 ↓↓

<-----CROSSEOVERS----->

_____ - INVARIANCES
 SYMMETRY - **BREAKINGS**
-SET

↑↑
 causes
 ↓↓

$\{0 \neq \partial_\mu J^\mu \dots\}$ -**SET**
 $\{ \dots\text{-}4\text{-CURRENTS}\}$ -**SET**
 $\{4\text{-[DIVERGENCES]}\dots\}$ -**SET**
 $\{4\text{-[NON-CONSERVATIONS]}\dots\}$ -**SET**

[fluctuation-dissipation theorem-equivalent] noise \equiv generalized-susceptibility $[\chi(\omega) = d(\text{OUTPUT})/d(\text{INPUT}) = d(\text{EFFECT or RESULT})/d(\text{CAUSE})]$ power-spectrum qualitative-type functional-form and quantitative critical-exponent "automatic-mathematical-catastrophe" (AUTMATHCAT) "dimensionality-catastrophe" (DIM-CAT) crossover second-order phase-transition critical-phenomenon.

[the Kallen-Lehmann representation-equivalence, reviewed succinctly by Bjorken & Drell, are that extant measures of asymptotic-limit antipodes of the PARSIMONY-of-Dichotomy (relative) [LOCALITY] = [BOUNDARYFUL] versus (relative) (...BOUNDARYLESS...) = (...GLOBALITY...); propagators \equiv Green's-functions \equiv diffusivity \equiv ... are equivalent to extant measures of asymptotic-limit antipodes of the PARSIMONY-of-Dichotomy (relative) ["1"/ ω^0 -WHITE/FLAT/FUNCTIONLESS] versus (relative) (... "1"/ $\omega^{\text{1,000} \dots}$...-FLICKER **HYPERBOLICITY**...): {fluctuation-dissipation theorem-equivalent} noise \equiv generalized-susceptibility power-spectrum as complex-functions of complex-variable $\omega = \omega' + i \omega''$ in first even-integer critical-dimensionality complex-plane C in their pure-mathematics analyticity].

QUANTUM-STATISTICS DICHOTOMY

Siegel[Schrodinger Centenary Symposium, Imperial College, London (1987); The Copenhagen Interpretation Fifty Years After The Como Lecture, Joensuu (1987); Bull. A. P. S. March Mtgs.: Anaheim (1990); Indianapolis (1992);...] manifestly-demonstrated, for quantum-statistics/NWB-law Dichotomy, generic: Takagi[Prog. Theo. Phys. Suppl. 88, 1 (1986)]-Oguri[Phys. Rev. (1985)]-Brout[Colloquium, U. C. Berkeley (1986)]-Susskind[Colloquium, U. C. Berkeley (1986)]- ...

$1 / [e^{\hbar \omega / k_B T} - (-1)^{(d^{\text{st}} + 2 \cdot \text{spin})}] = 1 / [e^{\hbar \omega / k_B T} - (-1)^{D(\in \mathbb{Z})}]$ dimensionality-dependent/dominated (DD)-**INEVITABILITY**, in SPD "CFP" PoD-**STRATEGY** (DD)-**INEVITABILITY** list-format:

QUANTUM-STATISTICS DICHOTOMY

[D. Lichtenstein and M. Rubenstein, J. Math. Phys. (~1966)]

Takagi-Oguri-Brout-Susskind-...

$$1 / [e^{\hbar \mathbf{w} / k_B T} - (-1)^{(d^{\text{st}} + 2\text{spin})}] =$$

$$1 / [e^{\hbar \mathbf{w} / k_B T} - (-1)^{D(\notin \mathbb{Z})}]$$

GENERIC
DIMENSIONALITY-
DEPENDENT/DOMINATED
QUANTUM-STATISTICS
DD-INEVITABILITY

vs.
AUTMATHCAT
<-----DIM-CAT----->
CROSSOVER

BOSE-EINSTEIN
(BOSONS):

FERMI-DIRAC
(FERMIONS):

$$1 / [e^{\hbar \mathbf{w} / k_B T} - (-1)^{D=\text{ODD-Z}}] \cong$$

$$\downarrow$$

$$1 / [e^{\hbar \mathbf{w} / k_B T} + 1]$$

\downarrow
via

$e^{\hbar \mathbf{w} / k_B T}$ Taylor/power-series
expansion
in infra-red- $(\hbar \mathbf{w} \ll k_B T)$ -limit

$$\downarrow$$

$$1 / [1 + [1 + (\hbar \mathbf{w} / k_B T) + \dots]] \cong$$

$$\downarrow$$

$$1 / [1 + [1 + (\hbar \mathbf{w} / k_B T) + \dots]] \cong$$

$$\downarrow$$

$$1 / [2 + (\hbar \mathbf{w} / k_B T) + \dots] \cong 1/2 \cong$$

$$\downarrow$$

$$["1" / \mathbf{w}^0 - \text{WHITE} / \text{FLAT}]$$

POWER-SPECTRUM

with
 $n = 0$
CRITICAL-EXPONENT

GEOMETRICALLY
RECTANGLE
HOMOTOPY
to
ELLIPSE

via

$$1 / [e^{\hbar \mathbf{w} / k_B T} - (-1)^{D(\notin \mathbb{Z})}] \cong$$

$$\downarrow$$

\downarrow
via

Euler-formula
 $e^{i\mathbf{p}} = -1$

$$\downarrow$$

$$1 / [e^{\hbar \mathbf{w} / k_B T} - e^{i\mathbf{p}D}] \cong$$

\downarrow
via

deMoivre-formula:
 $e^{i\mathbf{q}} = \cos \mathbf{q} + i \sin \mathbf{q}$

$$\downarrow$$

$$1 / [e^{\hbar \mathbf{w} / k_B T} - (\cos(\mathbf{p}D) + i \sin(\mathbf{p}D))] \cong$$

\downarrow
via
 $e^{\hbar \mathbf{w} / k_B T}$ Taylor/power-series
expansion
in infra-red- $(\hbar \mathbf{w} \ll k_B T)$ -limit

$$\downarrow$$

$$1 / [1 + (\hbar \mathbf{w} / k_B T) + \dots + (\cos(\mathbf{p}D) + i \sin(\mathbf{p}D))] \cong$$

$1 / [[1 + (\hbar \mathbf{w} / k_B T) + \dots + \cos(\mathbf{p}D)] +$
 $+ i \sin(\mathbf{p}D)] \cong$
COMPLEX
QUANTUM-STATISTICS

$$1 / [e^{\hbar \mathbf{w} / k_B T} - (-1)^{D=\text{EVEN-Z}}] \cong$$

$$\downarrow$$

$$1 / [e^{\hbar \mathbf{w} / k_B T} - 1]$$

\downarrow
via

$e^{\hbar \mathbf{w} / k_B T}$ Taylor/power-series
expansion in
infra-red- $(\hbar \mathbf{w} \ll k_B T)$ -limit

$$\downarrow$$

$$1 / [-1 + [1 + (\hbar \mathbf{w} / k_B T) + \dots]] \cong$$

$$\downarrow$$

$$1 / (\hbar \mathbf{w} / k_B T) = (k_B T / \hbar) \cdot 1 / \mathbf{w} \cong$$

$$\downarrow$$

$$\downarrow$$

$$\downarrow$$

$$(\dots "1" / \mathbf{w}^{1000} - \text{HYPERBOLICITY} \dots)$$

POWER-SPECTRUM

with
 $n = \underline{1.000\dots}$
CRITICAL-EXPONENT

GEOMETRICALLY
HYPERBOLA
obeying equation:

obeying equation:

$$\left(\frac{x}{a}\right)^2 + \left(\frac{y}{b}\right)^2 = 1$$

↑

same (+) sign

↓

$$\left[e^{\hbar w / k_B T} + 1 \right]^{-1}$$

“No-ons” = “Nothing-ons” =
 “ENC-ons”
 in
*Intermediate Interpolating
 Continuous Fractional
 Fractal-Dimensionality
 UNcertainty*
FLUCTUATIONS
except
 at
HALF-Integer
 “ANY-ons” = “Semi-ons”

$$\left(\frac{x}{a}\right)^2 - \left(\frac{y}{b}\right)^2 = 1$$

↑

same (-) sign

↓

$$\left[e^{\hbar w / k_B T} - 1 \right]^{-1}$$

C O N I C

S E C T I O N S

of **C O N E**

ELLIPSE:

$$\left(\frac{x}{a}\right)^2 + \left(\frac{y}{b}\right)^2 = 1$$

FERMIONS = ELLIPSE

PARABOLA:

$$<-- x^2 + 2xy = 1 -->$$

AUTMATHCAT
 <-----DIM-CAT----->
 CROSSOVER
 “ANYONS”= PARABOLA

HYPERBOLA:

$$\left(\frac{x}{a}\right)^2 - \left(\frac{y}{b}\right)^2 = 1$$

HYPERBOLA = BOSONS

GEOMETRICALLY

“ANALOGOUS”

to

SPECIAL-RELATIVITY

LIGHT-CONE

SECTIONS:

NULL

<---CROSSED-LINES --->

v = c

AUTMATHCAT

<-----DIM-CAT----->

CROSSOVER

SPACELIKE

ELLIPSE

v “>” c

TIMELIKE

HYPERBOLA

v < c

demonstrating that quantum-statistics Dichotomy follows exactly SPD “CFP” (PoD)-STRATEGY (DD)-INEVITABILITY! manifestly-

ARTIFICIAL-NEURAL-NETWORKS (A-NN's):
OPTIMIZING OPTIMIZATION-PROBLEMS OPTIMALLY (OPO)

“Engineering” by-rote brute-force on-node *hobbling* sigmoidal switching-function *crutch* implementation leads to “Boltzmann-machine” “simulated-annealing” inefficiency useless unimplementable-hardware slow/costly/memory-hogging flailing-away software “specificity-of-(so-called) ‘complexity’” (SoC)-tactics with little/no *all-important understanding of meaning* !!!

All-important understanding of meaning starts with:

- (1) realization that an A-NN is a *statistics*:

Lippmann[Lincoln Labs. Repts. (~1978- ~1982)] ab initio first review of artificial neural-networks (A-NN's) defined a neural-network as a “statistics” (hence amenable to Newcombe(1881)-Weyl(1916)-Benford(1938)-Kac(1955) inter-digit *statistical (on-average)* correlations

$$P(d) = \log_{10} \left(1 + \frac{1}{d} \right) \text{ analysis, but this is not our subject here yet).}$$

- (2) realization that an A-NN with “engineering” by-rote brute-force on-node *hobbling* sigmoidal switching-function *crutch* is a *quantum-statistics*.

Many Rogers [IEEE J. Neural Networks (~1990s)-Hsu [A.-I. N.-N. Assn. Mtgs. (~1980s); SPIE Mtgs. (~1980s)] have called for “1”/f-‘noise’” acceleration of A-NN’s functioning to converge to the global-minimum optimum-solution, iff one exists.

Demuth-Beale [Matlab “Neural-Network Tool Box”, The Math Works (~1990s)] have come closest, via artificial “radial-basis functions”, but with lack of any understanding, for the wrong reasons!

They use an on-(A-NN)-node radial-basis -functions to concoct a *Gaussian* switching-function

$$f(E, T) = 2^{-x^2} \approx \left(b^{-x^2} \approx e^{-x^2} \approx 10^{-x^2} \right) \text{ (to other possible bases } b \text{ or } e \text{ or } 10 \text{ or...) to replace standard by-rote sigmoidal}$$

$$\text{switching-function (to other possible bases } b \text{ or } 2 \text{ or } 10 \text{ or ...): } f(E, T) = \frac{1}{1 + e^{\frac{-E}{T}}} \approx \left(\frac{1}{1 + b^{\frac{-E}{T}}} \approx \frac{1}{1 + 2^{\frac{-E}{T}}} \approx \frac{1}{1 + 10^{\frac{-E}{T}}} \right) \text{ in terms}$$

of “energy” E and “temperature” T and claim some five thousand (three orders-of-magnitude) less-memory/faster-convergence to some global-minimum optimization.

But *without* any real **understanding** of the **meaning** of what they have done!

So-called “simulated-annealing” is often touted as a *mindless* was to seek a global-minimum optimal-solution, if one exists, from A-NN trapping in local-minima non-optimal non-solutions.

But again *without* any real **understanding** of the **meaning** of what is being done, and **why**, except for its internal “specificity-of-complexity” (SoC)-tactics: computer-simulation number-crunchings!

Just *what* standard by-rote sigmoidal switching-function (to other possible bases b or 2 or 10 or ...):

$$f(E, T) = \frac{1}{1 + e^{\frac{-E}{T}}} \approx \left(\frac{1}{1 + b^{\frac{-E}{T}}} \approx \frac{1}{1 + 2^{\frac{-E}{T}}} \approx \frac{1}{1 + 10^{\frac{-E}{T}}} \right) \text{ is, and ultimately } \textit{detrimentally means}$$

requires **understanding** via *identification* of it as *equivalent to* quantum-theory Fermi-Dirac quantum-statistics:

$$f_{\text{on-node switching-function}}^{N.N./\text{sigmoidal}}(E, T) = \frac{1}{1 + e^{\frac{-E}{T}}} \approx \left(\frac{1}{1 + b^{\frac{-E}{T}}} \approx \frac{1}{1 + 2^{\frac{-E}{T}}} \approx \frac{1}{1 + 10^{\frac{-E}{T}}} \right)$$

understanding of the fact that :

$$f_{\text{on-node switching-function}}^{NN/\text{sigmoidal}}(E, T) = \frac{1}{1 + e^{\frac{-E}{T}}} \approx \left(\frac{1}{1 + b^{\frac{-E}{T}}} \approx \frac{1}{1 + 2^{\frac{-E}{T}}} \approx \frac{1}{1 + 10^{\frac{-E}{T}}} \right) =$$

$$f_{\text{on-node switching-function}}^{NN/\text{sigmoidal}}(E, T) = \frac{1}{1 + e^{\frac{-E}{T}}} \approx \left(\frac{1}{1 + b^{\frac{-E}{T}}} \approx \frac{1}{1 + 2^{\frac{-E}{T}}} \approx \frac{1}{1 + 10^{\frac{-E}{T}}} \right) =$$

$$f_{\text{Quantum-Statistics}}^{\text{Fermi-Dirac}}(E, T) \equiv f^{F.-D.}(E, T) = \frac{1}{e^{\frac{E}{k_B T}} + 1} \approx \left(\frac{1}{b^{\frac{E}{k_B T}} + 1} \approx \frac{1}{2^{\frac{E}{k_B T}} + 1} \approx \frac{1}{10^{\frac{E}{k_B T}} + 1} \right) \equiv$$

$$f_{\text{Quantum-Statistics}}^{\text{Fermi-Dirac}}(\mathbf{w}, T) \equiv f^{F.-D.}(\mathbf{w}, T) = \frac{1}{e^{\frac{\mathbf{h}\mathbf{w}}{k_B T}} + 1} \approx \left(\frac{1}{b^{\frac{\mathbf{h}\mathbf{w}}{k_B T}} + 1} \approx \frac{1}{2^{\frac{\mathbf{h}\mathbf{w}}{k_B T}} + 1} \approx \frac{1}{10^{\frac{\mathbf{h}\mathbf{w}}{k_B T}} + 1} \right)$$

Understanding of the **meaning** of this is from “ the chemical-elements”, in which “fermions” Fermi-Dirac quantum-statistics

$$f_{\text{Quantum-Statistics}}^{\text{Fermi-Dirac}}(\mathbf{w}, T) \equiv f^{F.-D.}(\mathbf{w}, T) = \frac{1}{e^{\frac{\mathbf{h}\mathbf{w}}{k_B T}} + 1} \approx \left(\frac{1}{b^{\frac{\mathbf{h}\mathbf{w}}{k_B T}} + 1} \approx \frac{1}{2^{\frac{\mathbf{h}\mathbf{w}}{k_B T}} + 1} \approx \frac{1}{10^{\frac{\mathbf{h}\mathbf{w}}{k_B T}} + 1} \right) \text{ electrons } \textit{automatically traps the}$$

system in any/every local-minima, called “the chemical-elements”!

Exact-opposite/diametrically-opposed “bosons” Bose-Einstein quantum-statistics

$$f_{\text{Quantum-Statistics}}^{\text{Bose-Einstein}}(\mathbf{w}, T) \equiv f^{B.-E.}(\mathbf{w}, T) = \frac{1}{e^{\frac{\hbar \mathbf{w}}{k_B T}} - 1} \approx \left(\frac{1}{b^{\frac{\hbar \mathbf{w}}{k_B T}} - 1} \approx \frac{1}{2^{\frac{\hbar \mathbf{w}}{k_B T}} - 1} \approx \frac{1}{10^{\frac{\hbar \mathbf{w}}{k_B T}} - 1} \right) \quad \text{suffer from **no** such}$$

automatically trapping the system in any local-minima.

- (3) “EUREKA” (“Bosonization”) involves this above quantum-statistics Dichotomy *understanding* of the *meaning*: that the “fermions” Fermi-Dirac quantum-statistics

$$f_{\text{Quantum-Statistics}}^{\text{Fermi-Dirac}}(\mathbf{w}, T) \equiv f^{F.-D.}(\mathbf{w}, T) = \frac{1}{e^{\frac{\hbar \mathbf{w}}{k_B T}} + 1} \approx \left(\frac{1}{b^{\frac{\hbar \mathbf{w}}{k_B T}} + 1} \approx \frac{1}{2^{\frac{\hbar \mathbf{w}}{k_B T}} + 1} \approx \frac{1}{10^{\frac{\hbar \mathbf{w}}{k_B T}} + 1} \right) \quad \text{automatically traps the system in}$$

any/every local-minima,

versus

exact-opposite/diametrically-opposed “bosons” Bose-Einstein quantum-statistics

$$f_{\text{Quantum-Statistics}}^{\text{Bose-Einstein}}(\mathbf{w}, T) \equiv f^{B.-E.}(\mathbf{w}, T) = \frac{1}{e^{\frac{\hbar \mathbf{w}}{k_B T}} - 1} \approx \left(\frac{1}{b^{\frac{\hbar \mathbf{w}}{k_B T}} - 1} \approx \frac{1}{2^{\frac{\hbar \mathbf{w}}{k_B T}} - 1} \approx \frac{1}{10^{\frac{\hbar \mathbf{w}}{k_B T}} - 1} \right)$$

suffer from **no** such *automatically trapping the system in any local-minima.*

Hence “**EUREKA**” (“bosonization”) *quantum-statistics* qualitative-type **CROSSOVER**, from Fermi-Dirac (“fermions”) to Bose-Einstein (“boson”), is **absolutely mandatory!!!**

<u>ARTIFICIAL</u>	<u>NEURAL-NETWORKS</u>	<u>OPTIMALITY</u>
<u>ANALYSIS</u>		
:		
via		
(Siegel)		
<u>“FUZZYICS” S.P.D. I.-W.</u>		

<u>(A. N.-N.):</u>	<u>(A. N.-N.):</u>	<u>(A. N.-N.):</u>
$f_{\text{Quantum-Statistics}}^{\text{Fermi-Dirac}}(\mathbf{w}, T; "1"=\#) \equiv$	“EUREKA”:	$f_{\text{Quantum-Statistics}}^{\text{Bose-Einstein}}(\mathbf{w}, T; "1"=\#) \equiv$
$\equiv f^{F.-D.}(\mathbf{w}, T; "1"=\#) =$	vs.	$\equiv f^{B.-E.}(\mathbf{w}, T; "1"=\#) =$
$= \frac{"1"=\#}{e^{\frac{\hbar \mathbf{w}}{k_B T}} + 1} \approx$	AUTMATHCAT	$= \frac{"1"=\#}{e^{\frac{\hbar \mathbf{w}}{k_B T}} - 1} \approx$
	<-----DIM-CAT----->	
	CROSSOVER	
	via	
$\left(\begin{array}{l} "1"=\# \\ \approx \frac{\hbar \mathbf{w}}{b^{k_B T} + 1} \approx \\ "1"=\# \\ \approx \frac{\hbar \mathbf{w}}{2^{k_B T} + 1} \approx \\ "1"=\# \\ \approx \frac{\hbar \mathbf{w}}{10^{k_B T} + 1} \end{array} \right)$	<-----“BOZONIZATION”----->	$\left(\begin{array}{l} "1"=\# \\ \approx \frac{\hbar \mathbf{w}}{b^{k_B T} - 1} \approx \\ "1"=\# \\ \approx \frac{\hbar \mathbf{w}}{2^{k_B T} - 1} \approx \\ "1"=\# \\ \approx \frac{\hbar \mathbf{w}}{10^{k_B T} - 1} \end{array} \right)$
	CROSSOVER	

$\&$
 $+$
(A. N.-N.)
“SHAZAM”:

$$\begin{aligned}
 & \left[\begin{aligned}
 & f_{\text{Quantum-Statistics}}^{\text{Bose-Einstein}}(\mathbf{w}, T; \mathbf{I}' = \#) \equiv \\
 & \equiv f^{\text{B.-E.}}(\mathbf{w}, T; \mathbf{I}' = \#) = \\
 & = \frac{\mathbf{I}' = \#}{\frac{\hbar \mathbf{w}}{e^{k_B T} - 1}} \approx \\
 & \lim_{\# \rightarrow \infty} \left(\begin{aligned}
 & \approx \frac{\mathbf{I}' = \#}{\frac{\hbar \mathbf{w}}{b^{k_B T} - 1}} \approx \\
 & \approx \frac{\mathbf{I}' = \#}{\frac{\hbar \mathbf{w}}{2^{k_B T} - 1}} \approx \\
 & \approx \frac{\mathbf{I}' = \#}{\frac{\hbar \mathbf{w}}{10^{k_B T} - 1}}
 \end{aligned} \right) \Bigg] = \\
 & = \lim_{\# \rightarrow \infty} \left[\frac{\mathbf{I}' = \#}{\frac{\hbar \mathbf{w}}{e^{k_B T} - 1}} \right] = \left[\frac{\mathbf{d}(\mathbf{w} - 0)}{\frac{\hbar \mathbf{w}}{e^{k_B T} - 1}} \right] \approx \\
 & \approx \lim_{\# \rightarrow \infty} \left[\frac{\mathbf{I}' = \#}{\frac{\hbar \mathbf{w}}{b^{k_B T} - 1}} \right] = \left[\frac{\mathbf{d}(\mathbf{w} - 0)}{\frac{\hbar \mathbf{w}}{b^{k_B T} - 1}} \right] \approx \\
 & \approx \lim_{\# \rightarrow \infty} \left[\frac{\mathbf{I}' = \#}{\frac{\hbar \mathbf{w}}{2^{k_B T} - 1}} \right] = \left[\frac{\mathbf{d}(\mathbf{w} - 0)}{\frac{\hbar \mathbf{w}}{2^{k_B T} - 1}} \right] \approx \\
 & \approx \lim_{\# \rightarrow \infty} \left[\frac{\mathbf{I}' = \#}{\frac{\hbar \mathbf{w}}{10^{k_B T} - 1}} \right] = \left[\frac{\mathbf{d}(\mathbf{w} - 0)}{\frac{\hbar \mathbf{w}}{10^{k_B T} - 1}} \right] = \\
 & = \mathbf{d}(\mathbf{w} - 0)
 \end{aligned}$$

CONCLUSION

Artificial (by rote) sequential: (so called) “simulated-annealing” + (so called) “Boltzmann-machine” is replaced and superseded by the herein manifestly-demonstrated “***Bose-Einstein Condensation*** ‘machine’”!

Artificial neural-networks’ (A-NN’s) Achilles’-heel, the **wrong** sigmoidal switching-function, via “EUREKA” + “SHAZAM” softwares, without any radial-basis-functions, can be made to undergo “noise-induced/driven phase-transitions (NITs) which permit *control* via “NIT-**picking**” to effect forced quantum-tunneling to global-minimum (if such exists) via “Bose-Einstein

CONDENSATION” to ***automatically*** optimize optimization-problems optimally (OOPO) with ***optimality*** via “**FUZZYICS**” Synergetics Paradigm & Dichotomy (S.P.D.) “INEVITABILITY_-WEB” list-format analysis!

Fuzzy-logic/physics “**FUZZYICS**” “fuzzycity” Optimizing Optimization-Problems Optimally (OOPO) of neural-networks (A-N-Ns) Via *quantum-statistics* crossover equivalence to switching-function sigmoidal→***Anti***-sigmoidal crossover equivalence to (so called) “noise” power-spectrum crossover “Noise-‘Induced’/ ‘Driven’-Phase-Transitions” (NIT’s) ***vast-acceleration control*** via “NIT-Picking”: “Eureka” and “Shazam” A-N-N *Bose-Einstein* **Condensation** ***AUTOMATIC OPTIMALITY!***