McGraw-Hill
Illustrative Mathematics™

The highest-rated curriculum. A partner you know and trust.
“Students learn mathematics as a result of solving problems. Mathematical ideas are the outcomes of the problem-solving experience . . . ”

Creating a World Where Learners Know, Use, and Enjoy Mathematics

Decades of research shows that if students are given a chance to notice and wonder while trying to solve a problem by themselves, they retain procedural skills, develop problem-solving skills, build conceptual understanding, and form a mental framework for how ideas fit together. It allows students to develop strategies for tackling non-routine problems while engaging in productive struggle.

_Illustrative Mathematics_ is a problem-based curriculum designed to address content and practice standards to foster learning for all. Students are encouraged to take an active role to see what they can figure out before having things explained to them or being told what to do.

The Highest Rated Curriculum. A Partner You Know and Trust.

**McGraw-Hill**
- Personalized service and support from a local McGraw-Hill sales representative
- A team of curriculum specialists to support your implementation
- On-demand customer service to get help when you need it
- Spend less time printing and more time teaching with reliable delivery of print resources

**Exclusive Features**
- Interactive reports to drive instruction
- Student activities available digitally
- Autoscored practice problems for immediate feedback
- Engaging color print resources
- Improved layout of teacher materials support instruction more efficiently
- *Options to bundle with ALEKS* personalized learning

*ALEKS is not IM certified.

**Supporting the Illustrative Mathematics Mission**
As an IM Certified™ Partner, McGraw-Hill is committed to providing the support needed to successfully implement *Illustrative Mathematics*. A portion of every purchase is earmarked toward supporting the continued development of high-quality math curriculum.

Perfect Scores from EdReports

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<tr>
<th>Grade 6</th>
<th>Grade 7</th>
<th>Grade 8</th>
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*ALEKS is not IM certified.*
Developing coherent learning progressions and connections among areas of study requires crafting lessons to tell a mathematical story. Lessons must coherently build across units and grade levels and attend to many things: the mathematics, representations, activity structures, and learning trajectories, to name a few. Each of these considerations impacts how students access mathematics and influences the belief that mathematics is a connected set of ideas that makes sense.

The story of each grade is told in nine units. Each unit has a narrative that describes the mathematical work that will unfold in that unit. Each lesson in the unit also has a narrative.

Mathematics is not a spectator sport

Decades of research shows that when students are given a chance to notice and wonder while trying to solve a problem by themselves, they retain procedural skills, develop problem-solving skills, build conceptual understanding, and form a mental framework for how ideas fit together. In order to learn mathematics, students need to spend class time doing mathematics.
“An excellent mathematics program includes a curriculum that develops important mathematics along coherent learning progressions and develops connections among areas of mathematical study and between mathematics and the real world.”

Principles to Action by National Council of Teachers of Mathematics

**Lesson Narratives explain:**
- The mathematical content of the lesson and its place in the learning sequence.
- The meaning of any new terms introduced in the lesson.
- How the mathematical practices come into play, as appropriate.

**Activities within lessons also have narratives, which explain:**
- The mathematical purpose of the activity and its place in the learning sequence.
- What students are doing during the activity.
- What the teacher needs to look for while students are working on an activity to orchestrate an effective synthesis.
- Connections to the mathematical practices, when appropriate.
The Illustrative Mathematics Lesson

**Warm-Up**
Help students get ready for the day’s lesson or give students an opportunity to strengthen their number sense or procedural fluency.

**Instructional Activities**
For each activity, the teacher helps students understand the problem, students work on the problem, and then the teacher makes sure that students synthesize what they have learned.

**Lesson Synthesis**
Each lesson includes a lesson synthesis section that assists the teacher as they help students incorporate new insights into their big-picture understanding.

**Cool-Down**
A brief formative assessment to determine whether students understood the lesson.

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Digital Student and Teacher Editions

McGraw-Hill Illustrative Mathematics offers flexible implementations with both print and digital options that fit a variety of classrooms.

Online resources offer:

- Customizable content.
- The ability to add resources.
- Auto-scoring of student practice work.
- Ongoing student assessments.
- Classroom performance reporting.

Launch Presentations

Digital versions of lessons to present content.

Reports

Review the performance of individual students, classrooms, and grade levels.

Access Resources

Point-of-use access to resources such as assessments, eBooks, and course guides.
Strengthen Skills With Instructional Routines

Instructional routines allow students and teachers to pay less attention to what they are supposed to do and more attention to the mathematics to be learned. Routines provide a structure that helps strengthen students’ skills in listening and communicating their mathematical ideas.

There are 17 routines used in *Illustrative Mathematics*, including:

**Notice and Wonder**

In this routine, students are shown a mathematical representation and are asked, “What do you notice? What do you wonder?” and the teacher steers the conversation to wondering about something mathematical that the class is about to focus on. This helps make a mathematical task accessible to all students.

**Number Talk**

Number talks build computational fluency by encouraging students to think about the numbers in a computation problem and rely on what they know about structure, patterns, and properties of operations to mentally solve the problem.

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**Lesson 1-19**  
**Designing a Tent**

**Learning Goal**  
Let’s design some tents.

**Activity**  
19.1 Tent Design—Part 1

Have you ever been camping?  
You might know that sleeping bags are all about the same size, but tents come in a variety of shapes and sizes.

Your task is to design a tent to accommodate up to four people and estimate the amount of fabric needed to make your tent. Your design and estimate must be based on the information given and have mathematical justification.

First, look at these examples of tents, the average specifications of a camping tent, and standard sleeping bag measurements. Talk to a partner about:

- Similarities and differences among the tents
- Information that will be important in your designing process
- The pros and cons of the various designs

**Tent Styles**

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**Activity**  
1.2 More Orange, Green, or Blue?

Your teacher will assign you to look at Pattern A or Pattern B. In your pattern, which shape covers more of the plane: blue rhombuses, orange trapezoids, or green triangles? Explain how you know.

**Pattern A**

**Pattern B**

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**Note:**  
*Notice and Wonder* and *I Notice/I Wonder* are trademarks of NCTM and the Math Forum and are used in these materials with permission.
Which one doesn’t belong?

Students are presented with four figures, diagrams, graphs, or expressions with the prompt, “Which one doesn’t belong?” Typically, each of the four options “doesn’t belong” for a different reason, and the similarities and differences are mathematically significant. Students are prompted to explain their rationale for deciding that one option doesn’t belong and given opportunities to make their rationale more precise.

Information Gap Cards

In an information gap, one partner gets a problem card with a math question that doesn’t have enough given information, and the other partner gets a data card with information relevant to the problem card. Students ask each other questions like “What information do you need?” and are expected to explain what they will do with the information. This routine provides opportunities for high-quality mathematical conversations.
“The 5 Practices provided the structure I needed as a teacher to put all of these good teaching strategies into a cohesive teaching style that was not only student-centered but also focused on the mathematical goal of the day.”

Alicia F. Grade 6–7 mathematics, Woodbury, Minnesota
Facilitating Productive Classroom Discussions

Activities are structured using the 5 Practices for Orchestrating Mathematical Discussions².

Anticipate

Consider how students might mathematically interpret the problem, the array of strategies that they might use to tackle it, and how those strategies and interpretations might relate to the mathematical concepts, representations, procedures, and practices that you would like your students to learn.

Monitor

Pay close attention to students’ mathematical thinking and solution strategies as they work on the task. Prompt students to make their thinking visible.

Select

Select particular students to share their work with the rest of the class to get specific mathematics into the open for discussion.

Sequence

Make purposeful choices about the order in which students’ work is shared to maximize the chances of achieving the mathematical goals for the discussion.

Connect

Help students draw connections between their solutions and other students’ solutions as well as the key mathematical ideas in the lesson.

²(Smith & Stein, 2011), also described in Principles to Actions: Ensuring Mathematical Success for All (NCTM, 2014), and Intentional Talk: How to Structure and Lead Productive Mathematical Discussions (Kazemi & Hintz, 2014).
Assessing Student Progress

*Illustrative Mathematics* contains formative and summative assessments in each unit to help gauge classroom and student progress.

**Pre-Unit Assessments**

Each unit begins with a pre-unit diagnostic assessment titled Check Your Readiness. This assessment reviews prerequisite concepts and skills for the unit. Each assessment item identifies which lesson the skill or concept is needed for and provides guidance on what to do if students struggle or do well on the item. Teachers can use this knowledge to pace or tune instruction or move more quickly through a topic to optimize instructional time.

**Mid-Unit Assessments**

In longer units, a mid-unit assessment is also available. This assessment has the same form and structure as an end-of-unit assessment.

**Summative Assessments**

All summative assessment problems include a complete solution and standard alignment. Multiple-choice and multiple response problems often include a reason for each potential error a student might make. Restricted constructed response and extended response items include a rubric. Unlike formative assessments, problems on summative assessments generally do not prescribe a method of solution.

**End-of-Unit Assessments**

End-of-unit assessments gauge students’ understanding of the key concepts of the unit while also preparing students for new-generation standardized exams. Problem types include:

- Multiple-choice
- Multiple response
- Short answer
- Restricted constructed response
- Extended response

Problems vary in difficulty and depth of knowledge. In longer units, the end-of-unit assessment will include the breadth of all content for the full unit, with emphasis on the content from the second half of the unit.

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**Activity 3.3 Off the Grid**

Find the area of the shaded region(s) of each figure. Explain or show your reasoning.

<table>
<thead>
<tr>
<th>Figure A</th>
<th>Figure B</th>
<th>Figure C</th>
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</thead>
<tbody>
<tr>
<td>3 cm</td>
<td>5 cm</td>
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<tr>
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<tr>
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**Summary**

Reasoning to Find Area

There are different strategies we can use to find the area of a region. We can:

1. Decompose it into shapes whose areas you know how to calculate; find the area of each of those shapes, and then add the areas.
Consistent Lesson Structure

Each lesson has a warm-up activity, a synthesis, and a cool-down. By keeping the components in a similar form, the flow of work becomes predictable. This reduces cognitive demand, which enables students to focus on the mathematics rather than the lesson’s mechanics.

Logical Development of Concepts

Mathematical concepts are introduced simply, concretely, and repeatedly, with complexity and abstraction developing over time.

Participation Progression

Students are allowed time to think through a situation or question independently before engaging with others. This allows them to carry the weight of learning, with just-in-time supports from a community of learners.

Real-World Contexts

Opportunities to apply the mathematics they learn clarifies and deepens students’ understanding of core math concepts and skills. Mathematical modeling is a powerful activity for all students, but especially students with disabilities.
A Personalized Pathway to Math Proficiency

*ALEKS® is an online personalized learning solution for grades 6–12. ALEKS can be bundled with Illustrative Mathematics to provide targeted, supplemental assessment and instruction. It uses artificial intelligence to identify and provide instruction on the topics each student is most ready to learn. A continuous cycle of assessment, learning, and reinforcement adapts instruction to the individual needs of each student and customizes a unique learning pathway to help accelerate students to standard mastery. The program’s three-phase cycle keeps students engaged by challenging them with concepts they are ready to learn, thus eliminating boredom and frustration.

*ALEKS is not IM certified.

Features:

- An algorithm that generates a unique problem set for every student, every time.
- Detailed explanations for every problem—including dictionary and video resources.
- Learning Mode open-response problems and intuitive input tools provide an authentic measure of conceptual understanding.
- Pie reports provide in-depth analysis of student progress in multiple topics.
- Insights reports that identify students who may need intervention.
- Content in English and Spanish.
- Progress monitoring on student mastery of mathematical standards.
- Dynamic data at the student, class, school, and district level.

*2019 CODiE Award Winner
- Best Summative Assessment Solution
- Best College and Career-Readiness Solution

*The only peer-recognized competition in education and business technology.
IM Certified™ Professional Learning

McGraw-Hill is an IM Certified™ professional learning partner. Our facilitators are specially trained to deliver high-quality professional learning to teachers, coaches, and district leaders. McGraw-Hill partners with teachers and educational leaders to provide long-term, sustainable support for developing, refining, and reflecting on professional learning practices.
Partnering with McGraw-Hill

• Engaging color print resources for students and teachers
• Enhanced teacher materials support instruction more efficiently
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Learn more about McGraw-Hill Illustrative Mathematics
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