

2019

## Session 686

### Activities and Applets for Intuitive Understanding of SRS, Stratified, and Cluster Random Sampling

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### Outline

- Introductions
- About the Activity
- Notice/Wonder
  - As you view the different simulations
    - What do you notice?
    - What do you wonder?
- TURN AND TALK
  - After each exploration, we will ask you to turn and talk with a neighbor about what you noticed and anything you are wondering about.
- Questions

### About the Activity

- Educated citizens need to understand how random sampling enables us to make conclusions about a population (with a measure of uncertainty)
- AP Statistics Exam often asks students about advantages and disadvantages to different sampling methods in specific contexts
- We wanted a way for them to easily **explore** the implications of different sampling methods
- **Simulation** often gives students a more concrete visualization of the theoretical results
  - Tactile, Computer

### Turn and Talk

Introduce yourself to your neighbors

- Where you are from
- Grade level you teach
- In what course do you teach about selecting samples from a population?
  - What do you most want students to understand?

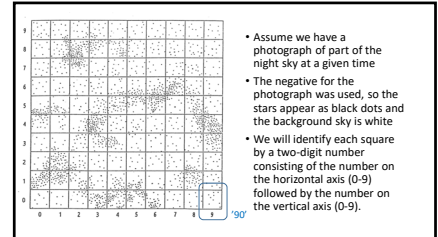
### SAMPLING STARS IN THE SKY



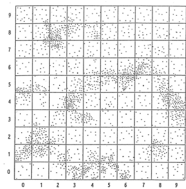
• *Exploration 2.2.1 – Introduction to Statistical Investigations AP Version*

• Adapted from Petocz (2005), *Sampling Space: Practical Experiments for Teaching Sampling*

Have you ever looked up into the night sky on a clear night and wondered how many stars there are in the sky?  
How could you go about estimating the number of stars?

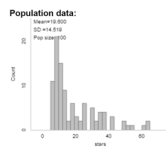


Goal: Estimate the number of stars in this section of the night sky.



- Why not just count them?
- Alternative? Random sample?
- Sampling frame = 100 squares
- Randomly selecting 10 squares, count the stars in those 10 squares
- **Statistic** = Average number of stars per square
- Then multiply by 100 to estimate total number of stars
- Will this "work"?

### Sampling Stars



Mean number of stars per square = 19.60 stars  
Std Dev = 14.519 squares

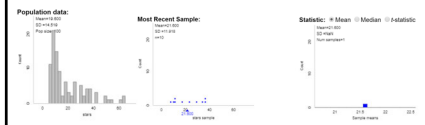
**Parameter** = Average number of stars per square in this grid

Does random sampling work?  
Does the sample mean tend to be close to the population mean?

Explore this method by taking lots of samples from the same population

### Some things to pay attention to in the Simulation

#### Three Different Graphs



### Method #1: Simple Random Samples

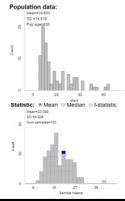
Rossman/Chance One Mean Applet

#### Notice/Wonder

As you view the different simulations

- What do you notice?
- What do you wonder?
- Does the method seem to work?

**TURN AND TALK**



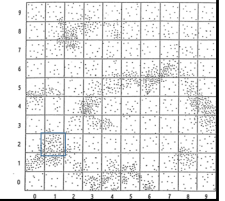
### Other Sampling Methods

- Would another method be more convenient?
- Would another method be more accurate?

### Method #2: Stratified Random Sample Variable = "density"

If you were going to divide the star map into two strata, high density and low density, approximately how many squares would you classify as high density and how many as low density?

**Just do a quick visual inspection, no need to actually count the number of stars in each square.**

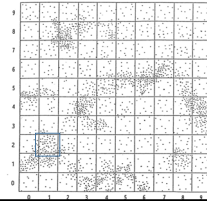


### Method #2: Stratified Random Sample Variable = "density"

If you were going to divide the star map into two strata, high density and low density, approximately how many squares would you classify as high density and how many as low density?

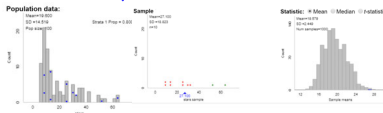
**How does this suggest changing the sampling method? Why?**

**TURN AND TALK**



### Method #2: Stratified Random Sample Variable = "density"

Rossman/Chance One Mean Applet



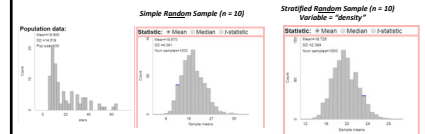
#### Notice/Wonder

As you view the different simulations

- What do you notice?
- What do you wonder?
- Does the method seem to work?

**TURN AND TALK**

### Comparison of Simple Random Sample (SRS) and Stratifying by Density



Compare your results when stratifying by density and when taking simple random samples. Is one sampling method preferable over the other? Explain how so/not.

[Hint: Which changed the most, the center, shape, or variability? What are the implications of this change?]

**TURN AND TALK**

### Method #3

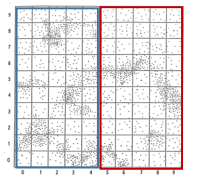
#### Stratified Random Sample: Variable = "side" (left/right)

Rossman/Chance One Mean Applet

Let's look at another variable to help understand how to choose a 'good' variable to stratify on.

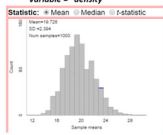
Suppose instead of choosing density as our variable on which to stratify, we instead decided to split the star map vertically into two equal halves, where stars in the left 50 squares of the map (columns 0-4) would be in the left stratum and stars in the right 50 squares of the map (columns 5-9) would be in the right stratum.

Why might using which side the stars are in (left/right) as the variable to stratify on be more feasible than knowing the density of the squares in advance?

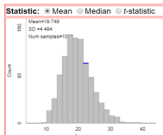


Does the choice of one variable provide a statistical advantage over the other as your choice of variable to stratify on? Explain.

#### Stratified Random Sample (n = 10) Variable = "density"



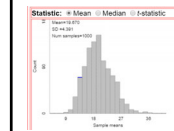
#### Stratified Random Sample (n = 10) Variable = "side"



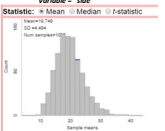
**TURN AND TALK**

Compare your results when stratifying by side and when taking a simple random sample. Is one sampling method preferable over the other? Explain how so/not.

#### Simple Random Sample (n = 10)



#### Stratified Random Sample (n = 10) Variable = "side"



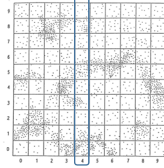
If the population does not have obvious strata (subgroups that behave differently from each other on the variable(s) of interest), then a simple random sample ensures a high degree of representativeness and is simpler and less time consuming than obtaining a stratified random sample.

#### Method #4 Cluster Random Sample: Variable = "column"

Describe a method you could use to select a cluster random sample of 10 squares from the star map to estimate the mean number of stars in each square, using column as the cluster variable.

How does this suggest changing the sampling method? Why?

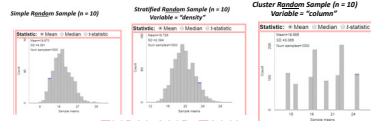
**TURN AND TALK**



#### Method #4 Cluster Random Sample: Variable = "column"

Compare your results when selecting a cluster sample using the column as the cluster variable with stratifying by density and with taking a simple random sample.

Is one sampling method preferable over the other? Explain.

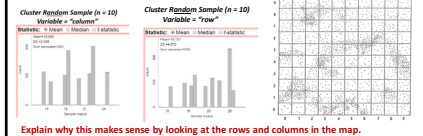


**TURN AND TALK**

#### Method #5 Cluster Random Sample: Variable = "row"

Compare your results for the two different variables that you used to obtain a cluster random sample (column and row).

Does the choice of one variable provide a statistical advantage over the other as your choice of cluster variable?



Explain why this makes sense by looking at the rows and columns in the map.

**TURN AND TALK**

#### Comparing stratified sampling to cluster sampling

|  | Strata   | Clusters  |
|--|--|---|
| Is a listing of the whole population required? | Yes  | No  |
| Number of groups                               | Comparatively few strata   | Typically a large number of clusters                                      |
| Sizes of groups                                | Often large  | Smaller   |
| Measure units from                             | Every stratum  | Only a simple random sample of clusters                                   |
| Reason(s) for using                            | To ensure small strata are represented and to reduce the standard deviation of estimates | To get a random sample without having to list all units in the population |

**Thank You!  
Questions?**

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