

Interpret and Communicate Math Ideas with Increasing Precision through the *Decide and Defend* Instructional Routine

GraceKelemanik@gmail.com

AmyLucenta@gmail.com

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@GraceKelemanik

@AmyLucenta

#DeciDefend #FosteringMPs #NCTMSD2019

Goal



Learn how the specific designs for interaction in the *Decide and Defend* instructional routine support students as they work to read, write, speak, and listen to mathematical ideas and reasoning with increasing precision.

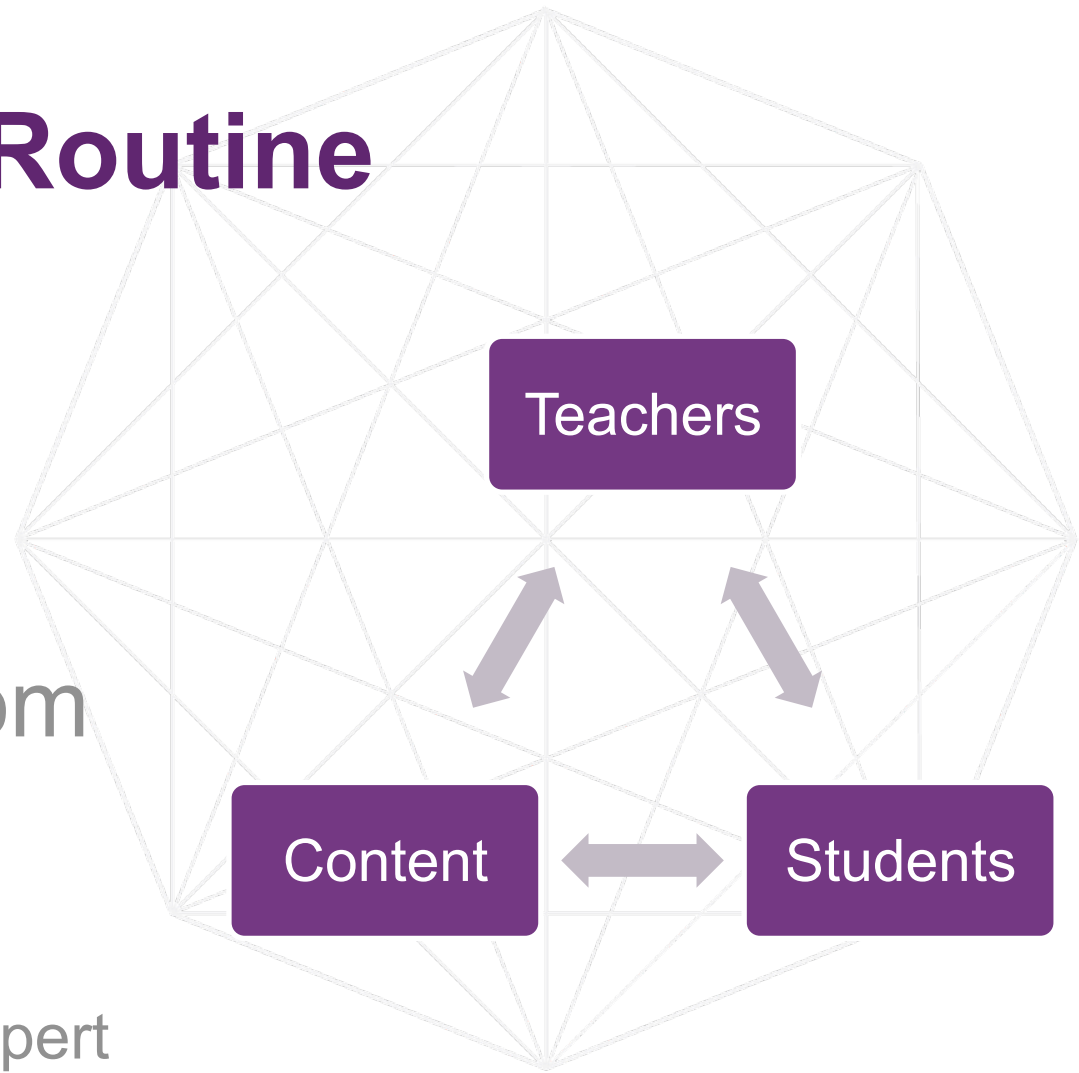
Agenda

1. Framing
2. Experience the *Decide and Defend* Instructional Routine
3. Unpack communication designs in *Decide and Defend*
4. Plan for language support and development

Instructional Routine

“Designs for interaction that organize classroom activities”

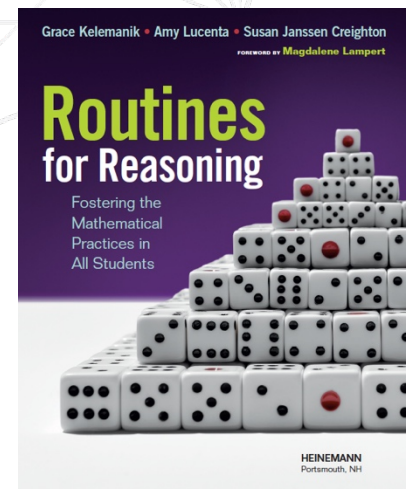
- Magdalene Lampert
NCSM 2015



Instructional Routines that Develop Mathematical Practices

- Capturing Quantities (MP2)
- Connecting Representations (MP7)
- Recognizing Repetition (MP8)
- Three Reads (MP1)
- Contemplate then Calculate (MP7)
- Decide and Defend (MP3)

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Critique the Reasoning of Others and Construct Viable Arguments (MP3)

Mathematically proficient students...

- distinguish correct logic or reasoning from that which is flawed, and if there is a flaw in an argument—explain what it is.
- justify their conclusions, communicate them to others, and respond to the arguments of others.
- can listen or read the arguments of others, decide whether they make sense, and ask useful questions to clarify or improve the arguments.

Decide and Defend





Decide & Defend

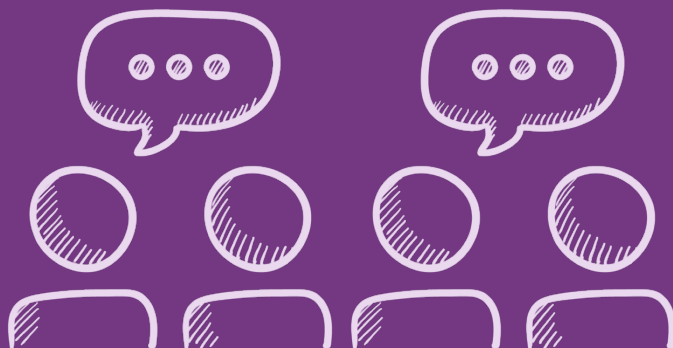
WHAT: Interpret math work, decide if you agree or disagree, draft, and defend your decision.

WHY: To build the mathematical habits of interpreting, deciding and defending (i.e., to think and work like mathematicians)

Decide & Defend



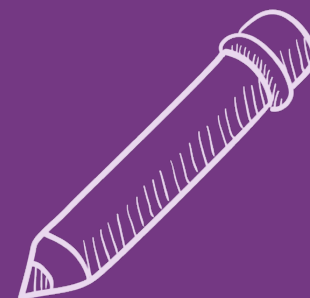
Interpret
the
Work



Decide



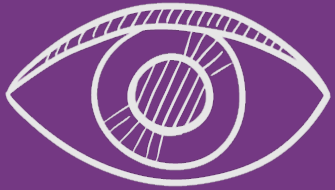
Defend



Reflect
on
Learning

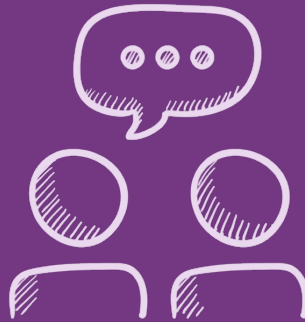


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Interpret the Work

Think — Pair - Share



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What is the question they are answering?

What did they do?

What did they find?

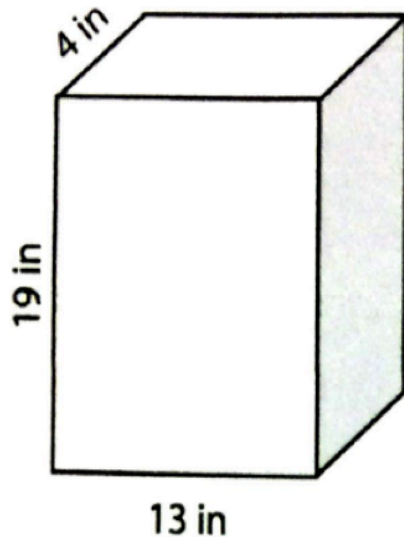


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What is the question they are answering?

Find the surface area.



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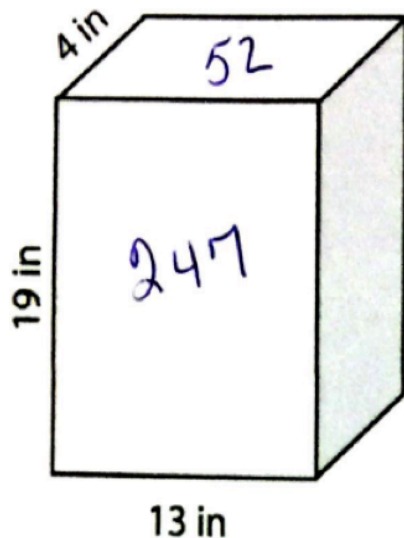


What is the question they are answering?

What did they do?

What did they find?

Find the surface area.



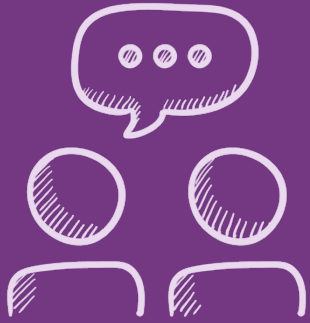
$$247 \times 4 + 52 \times 2$$

$$988 + 104$$

$$1092 \text{ sq units}$$



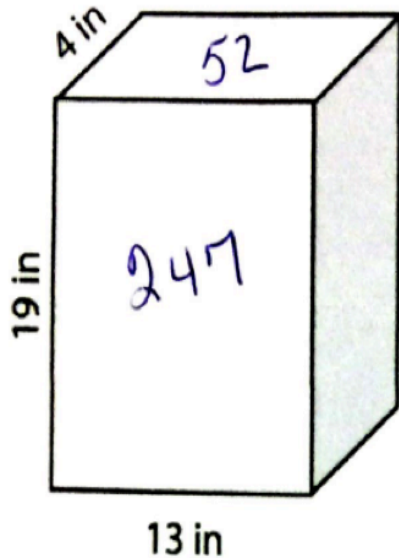
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I think they ...

What do you think they did?

Find the surface area.



$$247 \times 4 + 52 \times 2$$

$$988 + 104$$

$$1092 \text{ sq units}$$



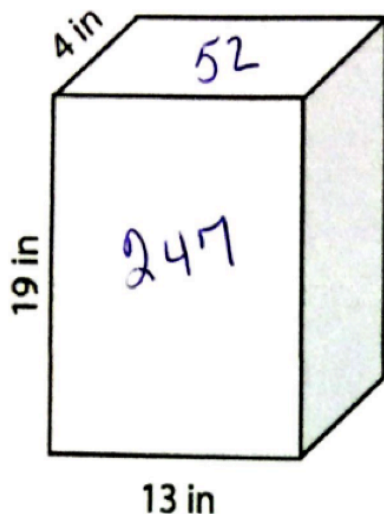
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First they...
next... then...

They found...
by...

Find the surface area.



$$247 \times 4 + 52 \times 2$$

$$988 + 104$$

$$1092 \text{ sq units}$$

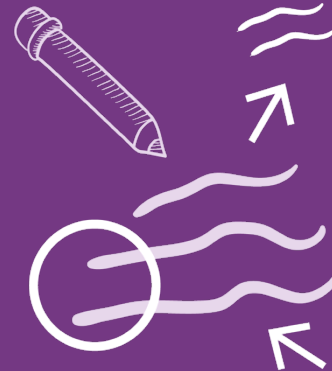
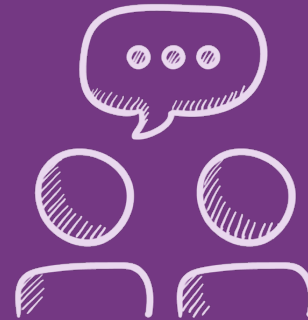


Decide if the Work is Correct

Think



Pair



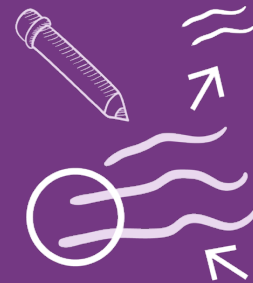
Annotate



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Decide if the Work is Correct



Ask yourself...

Does the *answer* make sense?

Does the *process* make sense?

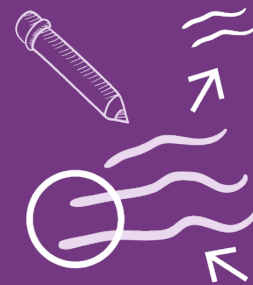
Are the *calculations* correct?



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Decide if the Work is Correct



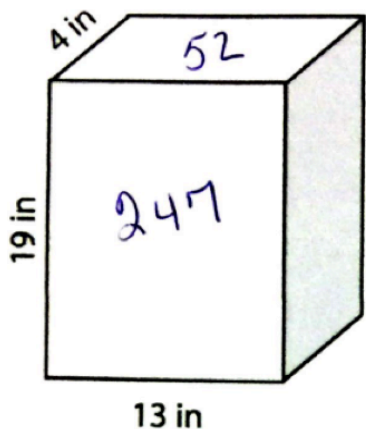
Ask yourself...

Does the
answer
make sense?

Does the *process*
make sense?

Are the
calculations
correct?

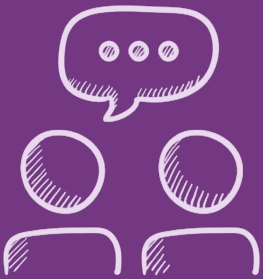
Find the surface area.



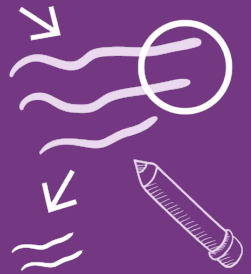
$$\begin{aligned} 247 \times 4 &+ 52 \times 2 \\ 988 &+ 104 \\ 1092 \text{ sq units} \end{aligned}$$



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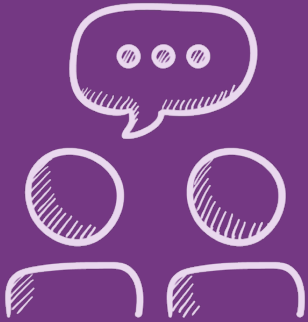
Decide if the Work is Correct



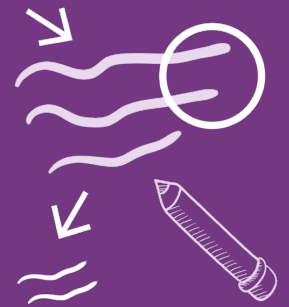
I think the work is
correct/incorrect
because...

I'm not sure if the work
is correct because...





Draft your Defense



- Prepare what you'll show
- Prepare what you'll say



Defend your Decision



Defender

We decided the work is correct/incorrect because...

We're still not sure about....

Skeptic

I agree/disagree with your defense because...

A question I have is...



Defend your Decision



Defender

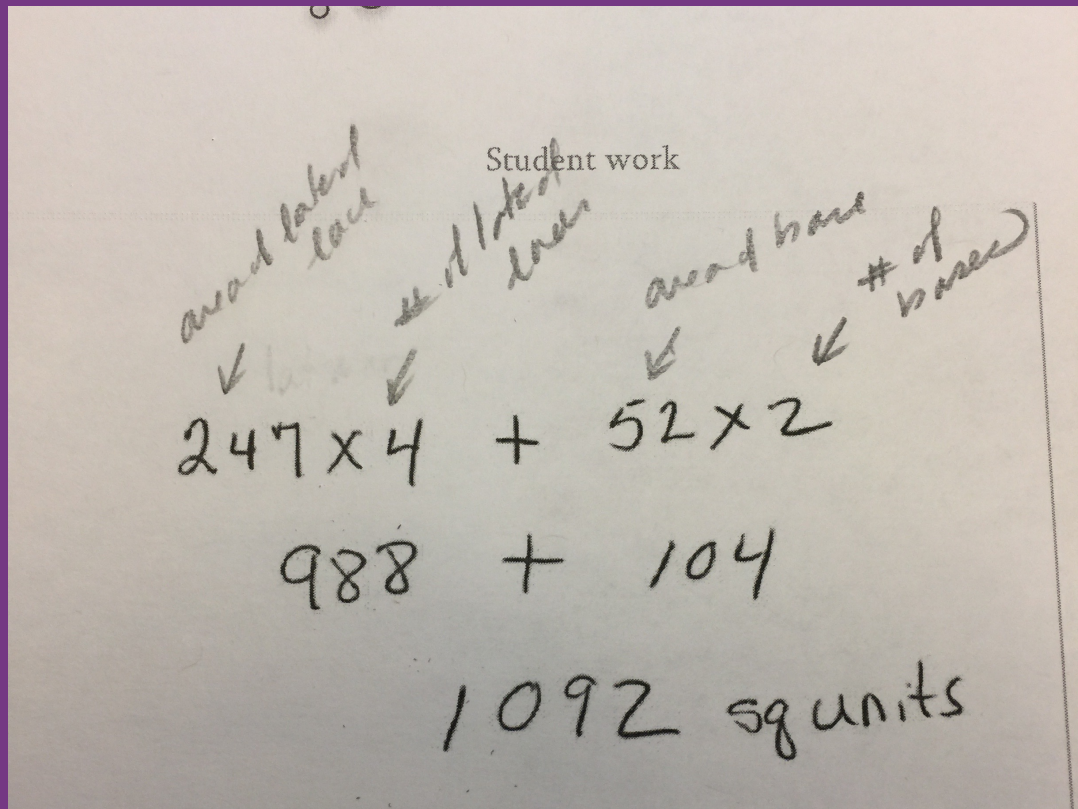
We decided the work is
correct/incorrect because...
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Skeptic

I agree/disagree with your
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A question I have is...



Defend your Decision



Defender

We decided the work is
correct/incorrect because...
We're still not sure about....

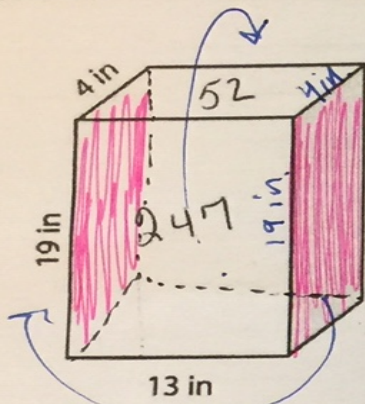
Skeptic

I agree/disagree with your
defense because...
A question I have is...



Defend your Decision



Original Problem	Student work
<p>Find the surface area.</p> 	$\begin{array}{l} \text{X2} \\ 247 \times 4 + 52 \times 2 + \overbrace{19 \times 4}^{\text{shaded}} \times 2 \\ \hline 988 + 104 + \text{---} \\ 1092 \text{ sq units} \end{array}$

Defender

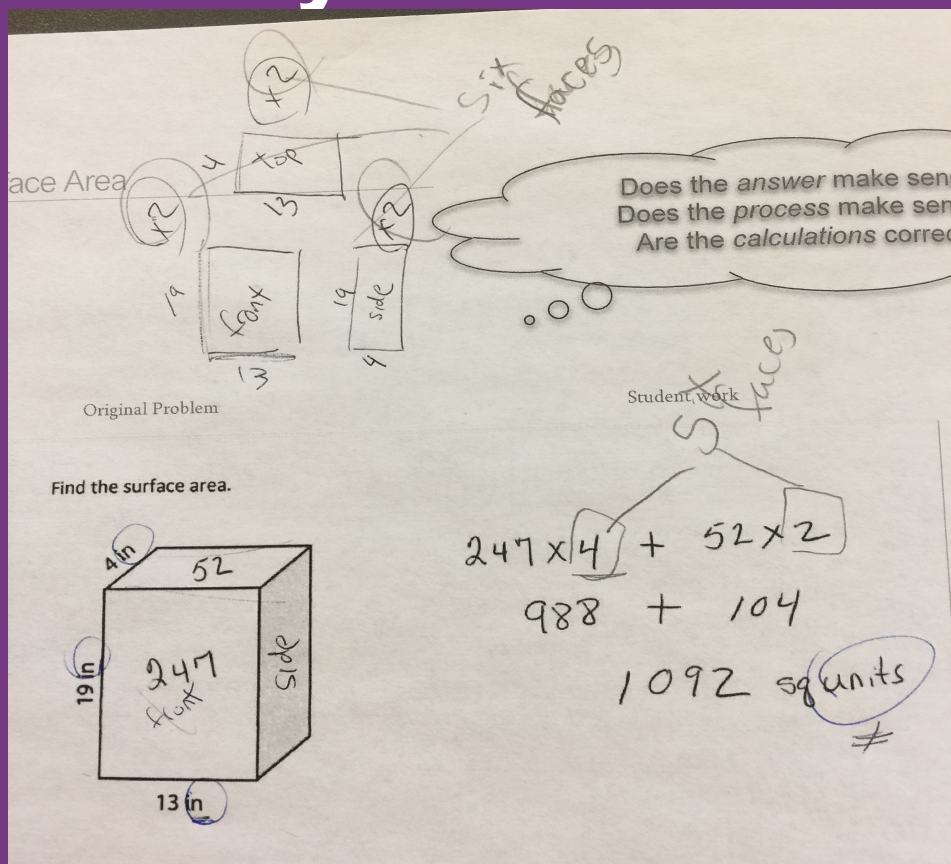
We decided the work is correct/incorrect because...
We're still not sure about....

Skeptic

I agree/disagree with your defense because...
A question I have is...



Defend your Decision



Defender

We decided the work is correct/incorrect because...
We're still not sure about....

Skeptic

I agree/disagree with your defense because...
A question I have is...

Reflect on learning



- Next time I interpret someone else's work, I will pay attention to...
- Next time I interpret someone else's work, I will ask myself...
- When convincing a skeptic, I learned to
- A new math idea I learned is...



Decide and Defend

- When/how were you communicating mathematically?
- What design features/teacher moves supported increased precision in math language and understanding?

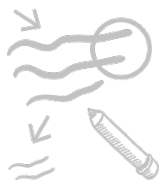


4 Essential Instructional Strategies

Keeping the focus on the mathematical thinking while providing access for a wide range of learners



Ask-yourself questions



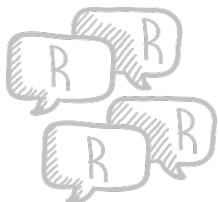
Annotation

I noticed...so I knew...

I saw...so I looked for...

... Connects to ... because

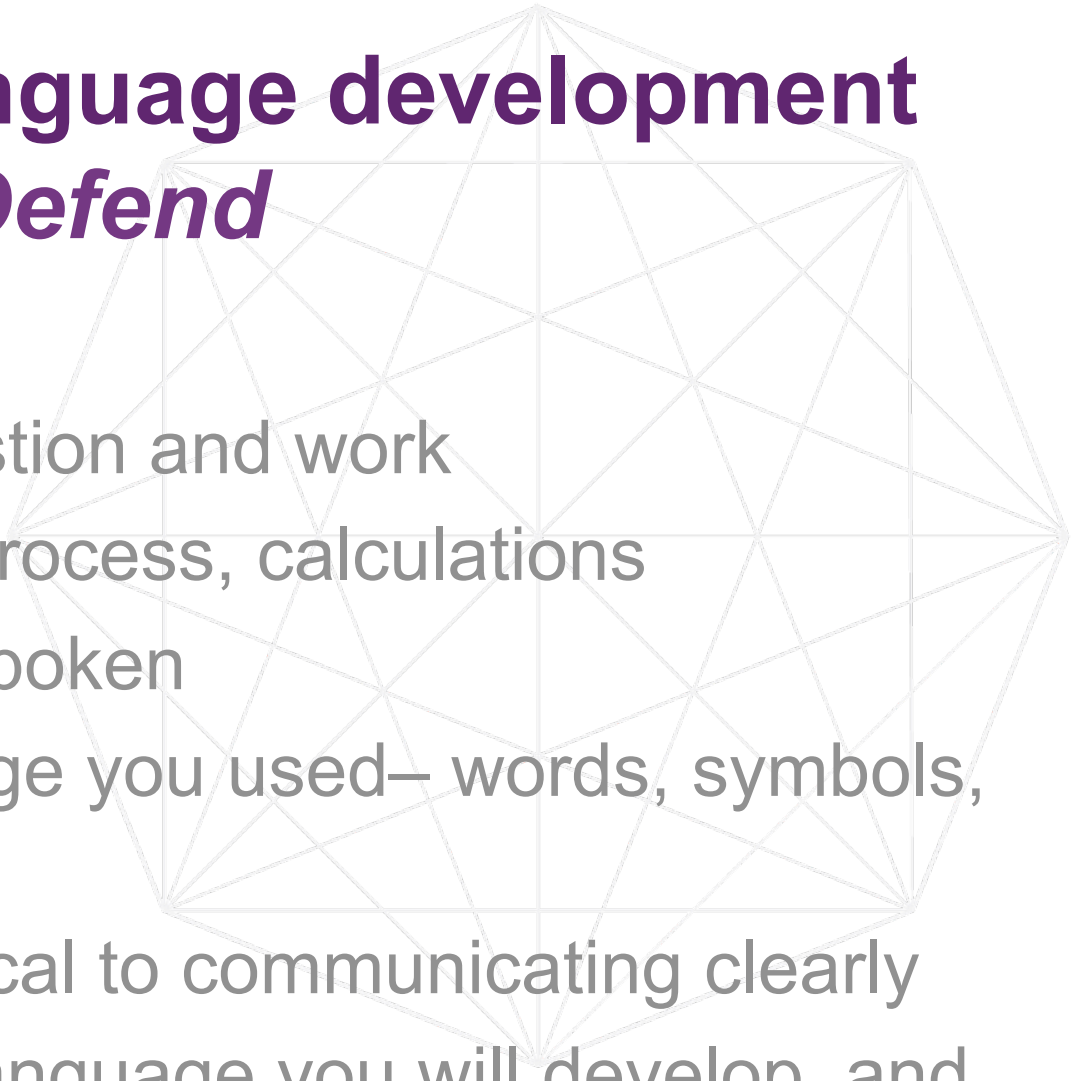
Sentence frames and starters



The Four Rs – repeat, rephrase,
reword, record

Planning for language development in *Decide and Defend*

- Do the math
 - Make sense – question and work
 - Decide – answer, process, calculations
 - Defend – written, spoken
- Reflect on the language you used– words, symbols, visuals
- Identify language critical to communicating clearly
- Identify what critical language you will develop, and
- Identify when in the routine you will develop that language

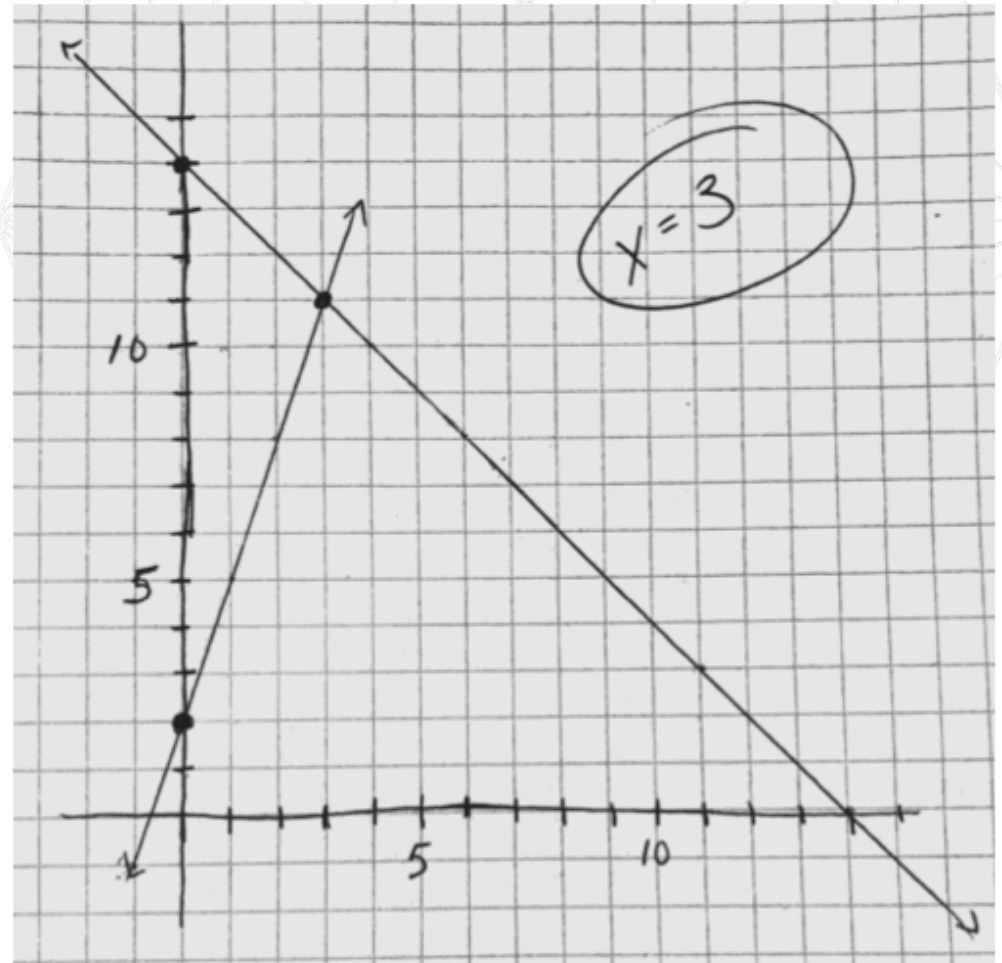


Planning for Language

- Do the Math.
- What language did you use?
- What was language was critical?
- What language would you develop?
- When in the routine?

Solve for X

$$3X + 2 = 14 - X$$



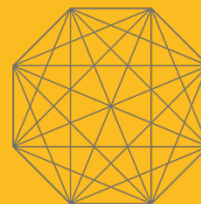
For More on *Decide and Defend* and Other Instructional Routines

Reach Out

AmyLucenta@gmail.com
GraceKelemanik@gmail.com

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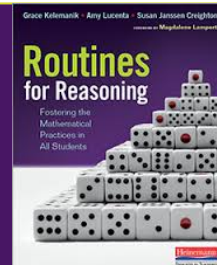
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Get the Book

www.heinemann.com



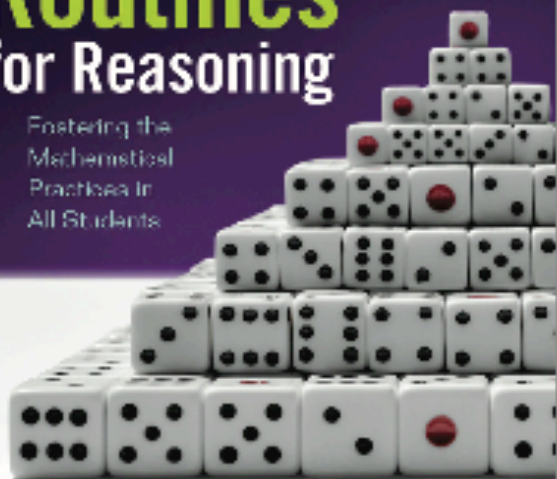


FOSTERING **MATH** PRACTICES

Grace Kellemanik • Amy Lucenta • Susan Janssen Creighton
with an introduction by Magdalena Lampert

Routines for Reasoning

Fostering the
Mathematical
Practices in
All Students



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June 24 - 27, 2019 • 8:30 AM to 3:00 PM

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Register at:

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\$299 before May 1st • \$349 after May 1st

Register at:

<https://edco.rocks/strategies>

When selecting worked examples for *Decide and Defend*, ask yourself...

- Does the worked example highlight a common error students make?
- Does the worked example draw attention to a classic misconception students hold?
- Does the worked example contain a representation that will serve to deepen students' conceptual understanding?
- Does the worked example present a unique solution strategy that sparks consideration of underlying math concepts?



Three Composing/Decomposing Problems (Jose) 2.NBT.A

Amy Lucenta, Decide and Defend, 0

0 likes

[Read more](#)

$$\frac{2}{3} \quad ? \quad \frac{2}{5}$$

Fraction Comparisons with Pictures 3.NF.A.3d

Amy Lucenta, Decide and Defend, 0

0 likes

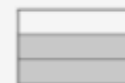
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Clark's Gummy Bears: Best Buy

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Tonya's work



There is one $\frac{3}{5}$ cup serving of rice in 1 cup, and there is $\frac{1}{5}$ cup of rice left over, so the answer should be $1\frac{1}{5}$.

Cup of Rice 6.NS.A.1, 5.NF.B.7

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$$\begin{aligned} K &= \text{katie's age} \\ C &= \text{cousin's age} \\ K - 10 &= 2C \end{aligned}$$

