



# Is this Vending Machine FUNCTIONing Correctly?

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**What are some common understandings of function that your students have?**



# What is a function?

# Teaching the Concept of Function

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**How might you introduce the concept of function to 8<sup>th</sup> graders who have never heard the term before?**

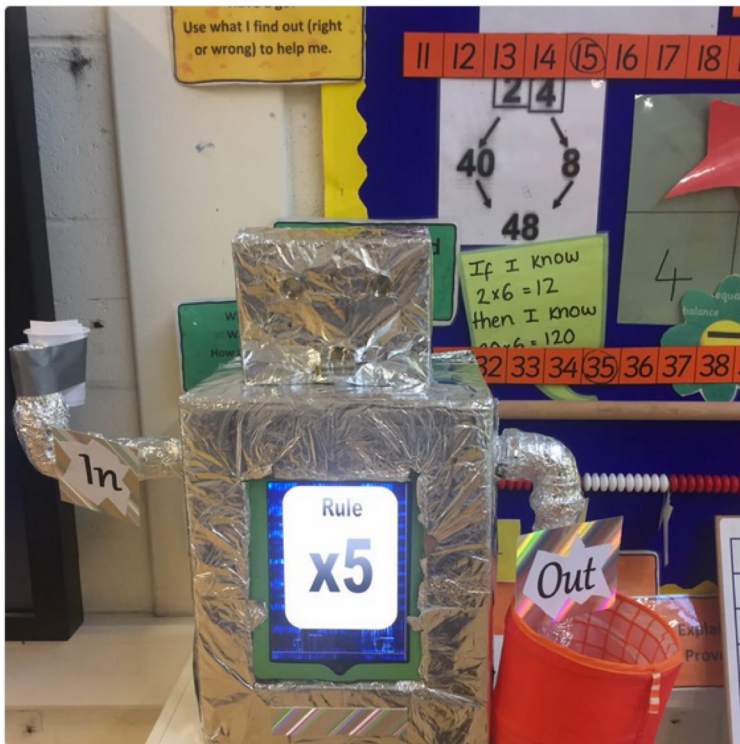




Mr Elliman  
@MrElliman

Follow

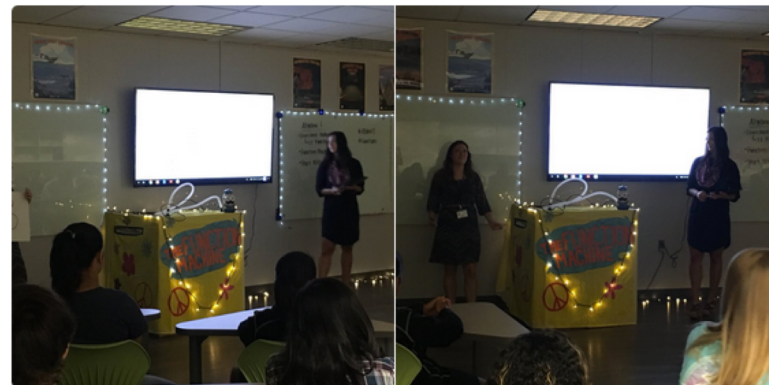
Looking forward to introducing my maths class to Funky the Function Machine today!



DSHS ELL  
@sciotoELL

Follow

Discovery learning with the Function Machine in Algebra I today! Figuring out input/output patterns and even seeing what happens when the machine breaks! [#IrishNation](#) [#theDublinDifference](#)



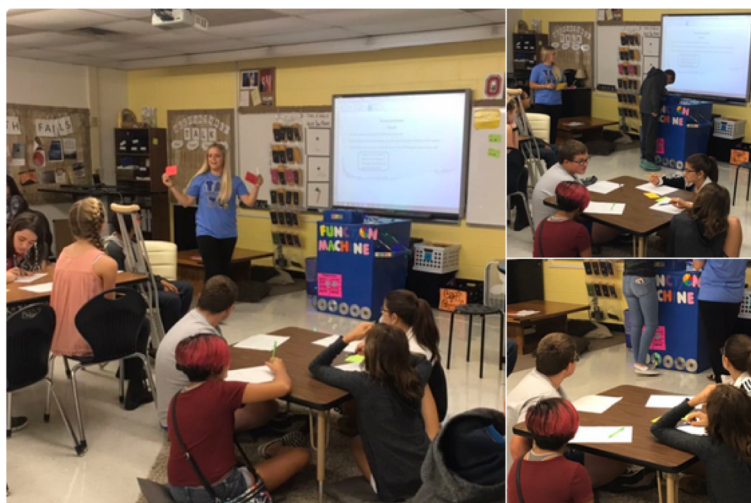
5:46 AM - 22 Aug 2018



**Steven Tartt**  
@Lions\_Admin

Follow

Miss Grossman @grossmanmath makes learning fun & highly engaging using her mystical, magical function machine to explore relationships between inputs & outputs @GahannaMSWest.



9:27 AM - 31 Aug 2018



**Tori Cox**  
@ToriTeachesMath

Follow

Ss played Number Tranformer Machine today by guessing the rule from inputs and outputs. Then I “broke” the machine w/ more than one output per input. I love this way of motivating the definition of a function #mtbos #iteachmath #teach180




2:01 PM - 24 Aug 2018

# Function Machines



The input number is 2.




Jessie

Rule:

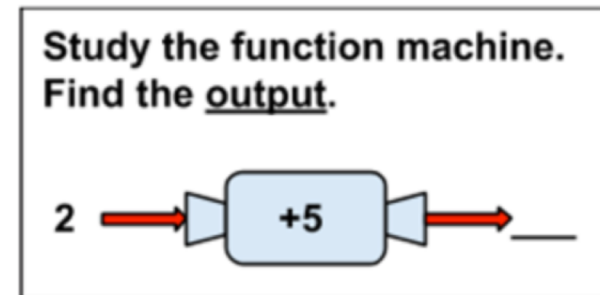
Input	Output
2	8
4	10
7	13
9	15

Then the output is 8.



Maya

Math Trailblazers



Huinker (2002) MTMS

Input

Enter

Output = Input

?  $\div$

Get New Rule

Check My Rule

Can you figure out the rule?

Input Output

Shodor

# “Guess My Rule” Function Machines

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## Pros

- A focus on inputs / outputs (independent / dependent)
- Requires one to recognize and describe a pattern
- Promotes connections between tables of values and algebraic expressions

## Cons

- Emphasizes algebraic rules (and representations)
- Does not allow for examining non-functions

# The Function Concept

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## Essential Understandings:

- 1a – Functions are single-valued mappings from one set - the domain of the function - to another-its range.
- 1b – Functions apply to a wide range of situations. They do not have to be described by any specific expression.
- 1c – The domain and range of functions do not have to be numbers.

From NCTM Developing Essential Understandings of  
Expressions, Equations, & Functions (2011)

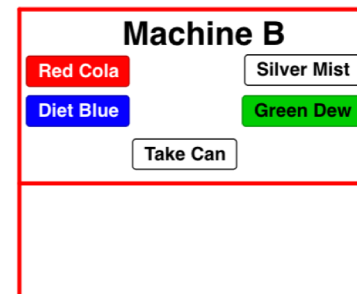
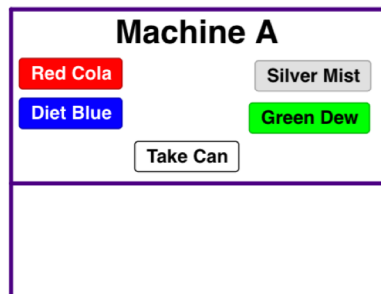
# The Vending Machine Applet



[go.uncc.edu/NCTMSD2019](http://go.uncc.edu/NCTMSD2019)

This one is a function.

This one is NOT a function.



Don't forget to click Take Can each time.





**What conceptions of function arose  
as you worked through the Vending  
Machine Applet Task?**

# Analyzing Middle School Students' Mathematical & Technological Thinking

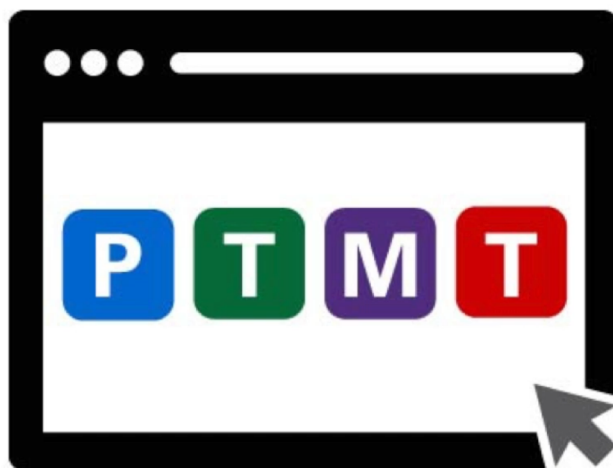
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**How do you anticipate middle school students engaging with this applet?**



# Middle School Group One



**Preparing to Teach Mathematics  
with Technology  
Examining Student Practices**

# Analyze Group 1's Thinking

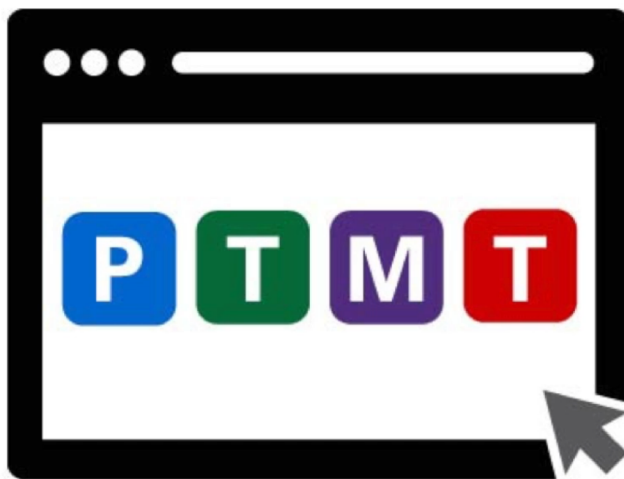
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**How did Group 1 engage with the applet to decide which machine was or was not a function?**

**Explain Group 1's understanding of function. Use examples from the screencast as evidence to show how you know what they do or do not fully understand.**

# Middle School Group Two



**Preparing to Teach Mathematics  
with Technology  
Examining Student Practices**

# Analyze Group 2's Thinking

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**How did Group 2 engage with the applet to decide which machine was or was not a function?**

**Explain Group 2's understanding of function. Use examples from the screencast as evidence to show how you know what they do or do not fully understand.**

# Compare and Contrast: Focus on Essential Understandings

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In what ways did the students' demonstrate their understanding of the essential understandings of the function concept?

In what ways might the applet have supported their development of these understandings?

## Essential Understandings:

- 1a – Functions are single-valued mappings from one set - the domain of the function - to another-its range.
- 1b – Functions apply to a wide range of situations. They do not have to be described by any specific expression.
- 1c – The domain and range of functions do not have to be numbers.



**What might you expect students would record as a definition for function after engaging with the Vending Machine Applet? Explain.**

Using the terms “input” and “output” write a definition for function based on your exploration of the machines.



Function is when the input gives you a consistent output.

Consistent input and output and single relationship that works for all factors.

Input - button pressed

output - can that came out

input can be different,  
but output is same for each input

Input → The button you press to receive a can  
Function → Input + Output = answer  
Output → The can that comes out of the vending machine.

A function is when the input produces a predictable output.

# Final Thoughts

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To develop an understanding of function that aligns with the essential understandings we believe...

- It is important that students have opportunities to consider what is and is not a function
- It is important that students have opportunities to explore non-algebraic representations of function

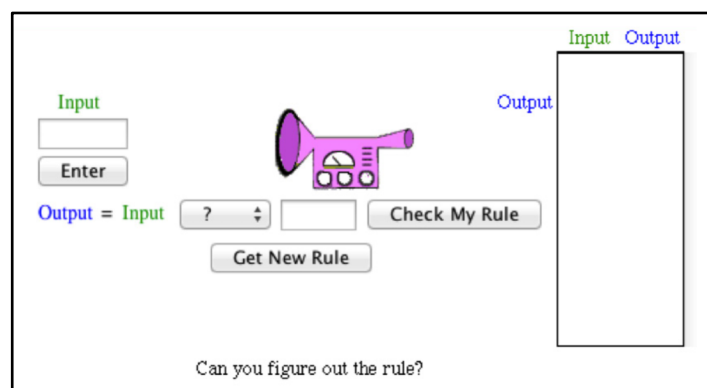
The Vending Machine Applet is a novel and engaging way to address these needs.

You are welcome to use and share the app!

FYI...There is an accompanying paper that has been accepted to MTMS that will come out eventually. 😊

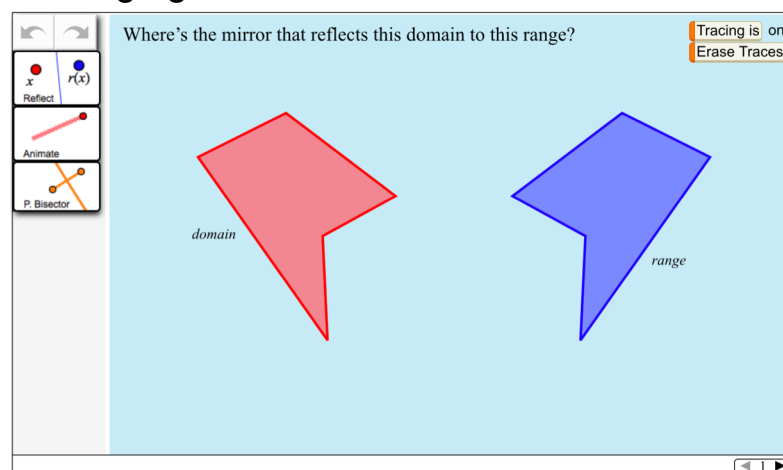


# What would come next?

A software interface for a 'Guess my rule' task. It features an input field with a green 'Input' label, an 'Enter' button, and a pink megaphone icon. Below the input field is a text area with 'Output = Input' and a dropdown menu showing '?'. To the right is an 'Output' field with a blue 'Output' label. Buttons for 'Check My Rule' and 'Get New Rule' are present. At the bottom, it asks 'Can you figure out the rule?'.

Guess my rule type tasks

Leveraging transformations to think about function



9:45 – 11:00 -- Sapphire CD

**Making Connections between Geometric Transformations and Functions  
using Technology (and Dance!)**



## Preparing to Teach Mathematics with Technology Examining Student Practices

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