

## **Agenda**

- Introduction
- Definition of arguments
  - Why is it important?
  - Current state
- Collective argumentation approach
- Task examples
  - Try an example!
- Resources
- Conclusions
- Comments and questions





### Introduction

- 9<sup>th</sup> year in education -Mathematics and French
- PhD student in mathematics and world language education
- Research interests: interpersonal discourse of content knowledge, discourse and conceptualization of mathematical proofs and arguments, and the development of learning communities



Definition of mathematical argument



## What is argumentation?

#### What is a mathematical argument?

- The act of convincing oneself and others of the truth of a mathematical statement based on agreed-upon principles in a specific community.
- · Verbal or written
- · Sophisticated or informal
- Explanation



#### What comprises a mathematical argument?

- A connected sequence of assertions for or against a mathematical claim, with the following characteristics:
  - Use statements accepted as true and available without further justification
  - · Employs reasoning
  - · Communicated with understandable expression
- · In the context of the classroom community



#### Why is it important?

- · Conceptual understanding
  - Justification is a deeper level of mathematical processing
- Mathematicians prove!
- Engaging math is not static!
- Standards
  - NCTM (1989, 2000): Mathematical Practice #3
  - Common Core State Standards for Mathematics (2010)



What is the current state?



#### What is the current state of affairs?

- Arguments and proofs solely utilized in Geometry (if that)
- MP #3: "Create viable arguments and critique the reasoning of others."



Collective Argumentation



#### What is collective argumentation?

- Communal Criteria
- · Open Tasks
- · Facilitation of Instruction
- · Role of the teacher





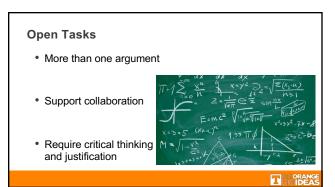


#### **Communal Criteria**

- Using facts and evidence
- Concise
- True for all cases
- Understandable
- \*If necessary, go over terminology.



# Open Tasks

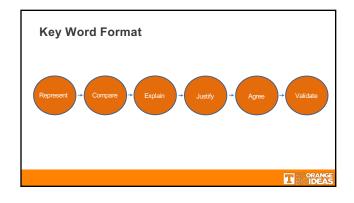


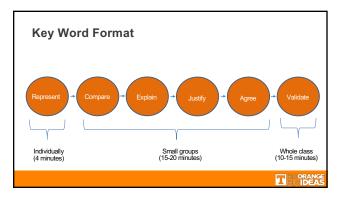
Facilitation of Instruction

#### **Facilitation of Instruction**

- · Students are presented with the task
- Students work individually (4 minutes)
- Students work in small groups of 3-5 students (15-20 minutes)
- Students validate their arguments to the whole class (10-15 minutes)







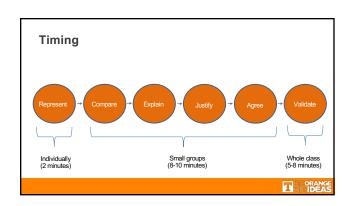
Role of the teacher

#### Role of the teacher

- During group work time: Question students push them without giving hints or clues.
- Try not to show preference for different responses.
- Validate: Encourage students to critique each other respectfully. Ask critical questions to each group regardless of the sophistication of the argument.

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Task Example



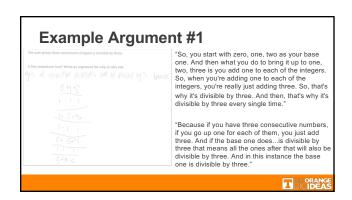
#### **Task**

- Claim: The sum of three consecutive integers is divisible by three.
- Is this conjecture true? Write an argument for why or why not.



## Volunteers Individual Small Groups Validate based on criteria

# Example Arguments



## **Example Argument #2**

"Take any three consecutive numbers. You can add one to the first number and subtract one from the last number. The sum will be equal to the original because we are essentially adding zero. The result will be three numbers that are equal. Adding three numbers that are equal creates a sum that is divisible by three."

1 + 2 + 3 +1 -1

2 + 2 + 2

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## **Example Argument #3**

"The conjecture is true because I tried several examples, and it worked out. I even tried examples of negative numbers and it worked. So, we think the conjecture is true because it worked for all of the examples we tried."

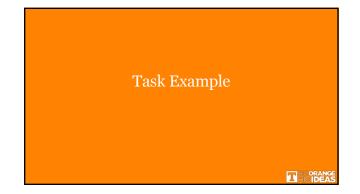
"For instance, -11 + (-10) + (-9) = -30, which is divisible by 3."



## **Example Argument #4**

"The conjecture is true. We even found that it works for any odd number of consecutive integers. Take 5 consecutive integers: 5+6+7+8+9=35, which is divisible by 5. This works for 7 and 9 too, and we think it will work for any odd number of consecutive integers."





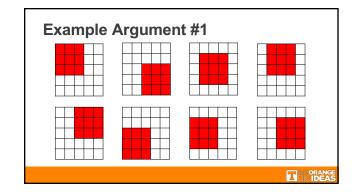
### **The Squares Problem**

Find the number of 3-by-3 squares are there in the 4-by-4 square below.



- How many different 3-by- 3 squares are there in a 5-by- 5 square?
- How many different 3-by- 3 squares are there in a 6-by- 6 square?
- How many different 3-by- 3 squares are there in a 10-by- 10 square?
- How many different 3-by- 3 squares are there in any size square?



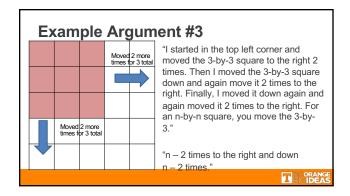


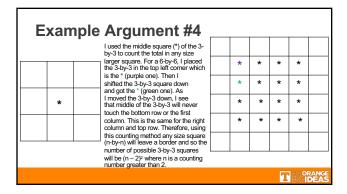
## **Example Argument #2**

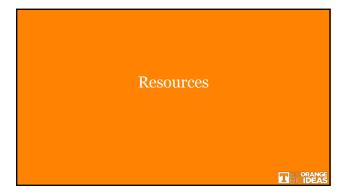
х	У
4-by-4	4
5-by-5	9
6-by-6	16
7-by-7	25
x-by-x	$(x-2)^2$

"I noticed that the y values are squares and then I realized that the squares are two less than x and I got  $(x-2)^2$ ."

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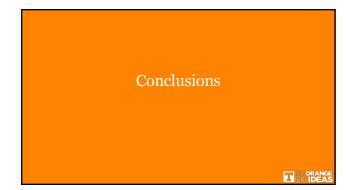




#### Resources

- <a href="https://www.illustrativemathematics.org/curriculum">https://www.illustrativemathematics.org/curriculum</a> for 6-8
- <a href="https://playwithyourmath.com">https://playwithyourmath.com</a>
- Dan Meyer's Three-Act Math Tasks
- http://map.mathshell.org
- NCTM website (problems of the week, etc.)
- · Reading academic articles





#### **Conclusions**

- · Argumentation can be done at all levels!
- Create and utilize the classroom community.
- · Use open tasks accessible to the community.
- Allow for students to represent, compare, explain, justify, agree, and validate (key word method).
- · Encourage collaboration and creativity!



# Questions? Contact me! Today's presentation & materials: http://www.monsieurking.weebly.com Email: nking5@vols.utk.edu