

# **Proportional Relationships:**

A Love Story of Linear Algebra



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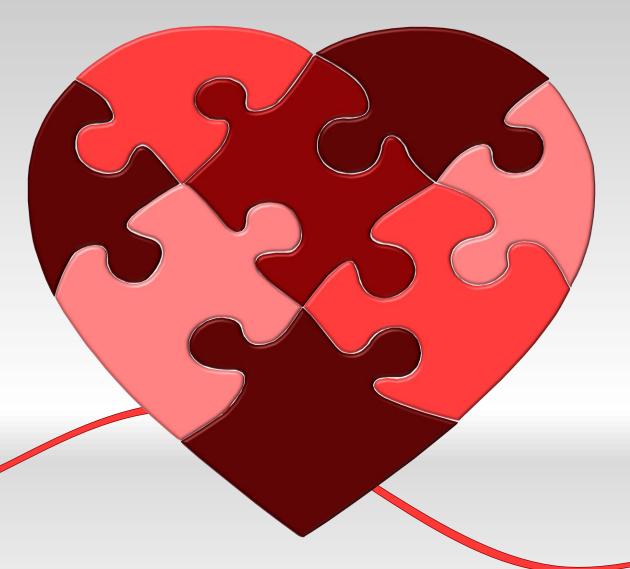
# **Interacting Today**

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 https://padlet.com/pruitte/
 wax3gi744ims

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**Equivalent Fractions** 

Measurement & Data

Algebraic Thinking

**Ratios** 

**Proportional Relationships** 

Attributes of a Line

Linear Algebra

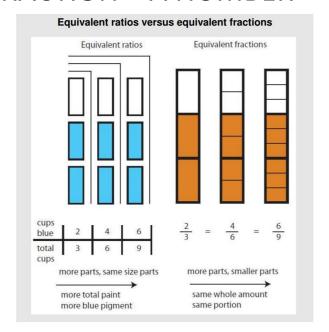
# **Proportional Relationships:**

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# **Equivalent Fractions**

- Starts in 3<sup>rd</sup> Grade
- Allows for the generation of fractions
- Important to note what happens in equivalent fractions
  - FRACTION = A NUMBER





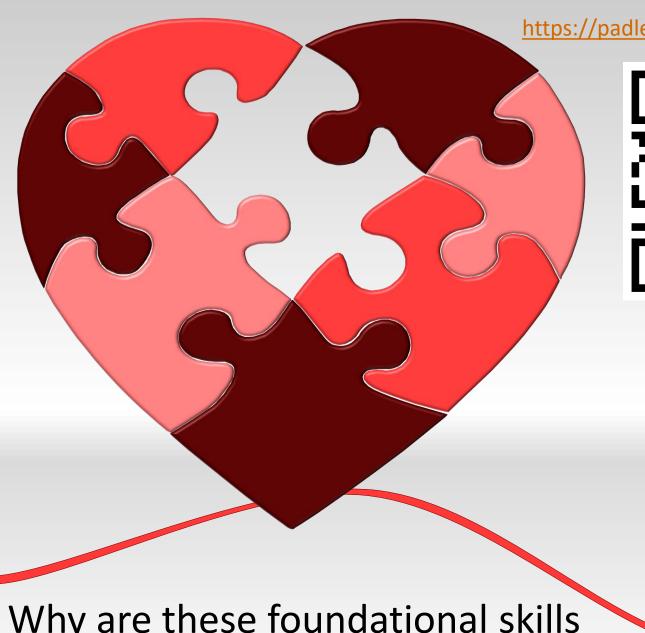


- Starts in 4<sup>th</sup> Grade
- Generate a conversion table for feet and inches listing the number pairs (1, 12), (2, 24), (3, 36),...





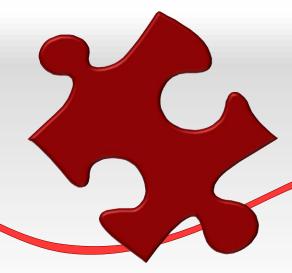
- Starts in 5<sup>th</sup> Grade
- Form ordered pairs consisting of corresponding terms from the two patterns, and graph the ordered pairs on a coordinate plane.



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Why are these foundational skills important?





# **Ratios**

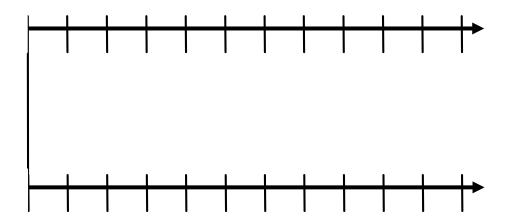
- Starts in 6<sup>th</sup> Grade
- Ratios arise in situations in which two (or more) quantities are related.
- RATIO = A RELATIONSHIP
- Important to build models with students first.
- Frayer Model is one way to do this

Starting Ratio:			Bar Mode	I/ Tape Diagra	m/ Other Model:
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# **DOUBLE NUMBER LINES 6.RP.A.I**



- Use a double number line to represent the following situation.
  - Grandma walks 2 miles in 30 minutes.

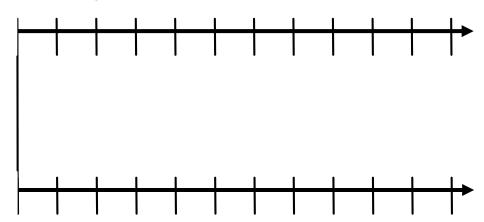


# **DOUBLE NUMBER LINES 6.RP.A.2**



- Use a double number line to represent the following situation.
  - Ms. Fraiser the librarian can read  $1\frac{1}{2}$  books in 3 days. Create a number line to model this information.
  - How many books can Ms. Fraiser read in one day?

What other questions can be asked using this information?



# PROBLEM SOLVING WITH RATIOS 6.RP.A.3

		Bar Model/ Tape Diagram/Qther Model:
Table:		
Double Number Lines:	Two batches of cookies require 7 cups of flour. Solve to find how much flour will be needed for up to 8 batches of cookie.	Coordinate Grid:



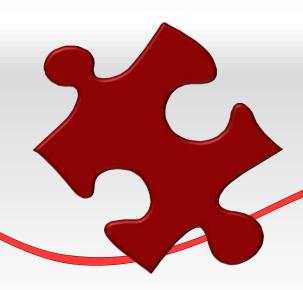
re decided to make chocolate chip cookie the math club! The recipe calls for % cuigar and the recipe makes 20 cookies club has 60 members! How much need?



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Why is it important to make connections of different representations?





# **Proportional Relationships**

## MAFS.7.RP.1.2

Recognize and represent proportional relationships between quantities.

- a. Decide whether two quantities are in a proportional relationship, e.g., by testing for equivalent ratios in a table or graphing on a coordinate plane and observing whether the graph is a straight line through the origin.
- b. Identify the constant of proportionality (unit rate) in tables, graphs, equations, diagrams, and verbal descriptions of proportional relationships.
- c. Represent proportional relationships by equations. For example, if total cost t is proportional to the number n of items purchased at a constant price p, the relationship between the total cost and the number of items can be expressed as t = pn.
- d. Explain what a point (x, y) on the graph of a proportional relationship means in terms of the situation, with special attention to the points (0,0) and (1,r) where r is the unit rate.

## Solve for Rates and Ratios in Multiple Ways

Starting Ratio:		Equation to Repres	sent Proportionality:
Table:			
Double Number Lines:	Place the prol		Coordinate Grid:

# **Buying Bananas, Assessment Version**

# **Task**

Carlos bought  $6\frac{1}{2}$  pounds of bananas for \$5.20.

- a. What is the price per pound of the bananas that Carlos bought? [\_\_\_\_]
- b. What quantity of bananas would one dollar buy? [\_\_\_\_] pounds
- c. Which of the points in the coordinate plane shown below correspond to a quantity of bananas that cost the same price per pound as the bananas Carlos bought? (Select all that apply.)



# **Linear Algebra**



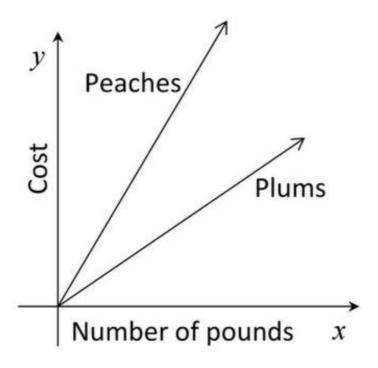
# MAFS.8.EE.2.5

Graph proportional relationships, interpreting the unit rate as the slope of the graph. Compare two different proportional relationships represented in different ways. For example, compare a distance-time graph to a distance-time equation to determine which of two moving objects has greater speed.

# **MAFS.8.EE.2.6**

Use similar triangles to explain why the slope m is the same between any two distinct points on a non-vertical line in the coordinate plane; derive the equation y = mx for a line through the origin and the equation y = mx + b for a line intercepting the vertical axis at b.

The graphs below show the cost y of buying x pounds of fruit. One graph shows the cost of buying x pounds of peaches, and the other shows the cost of buying x pounds of plums.



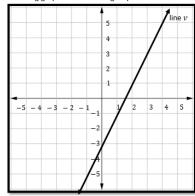
- a. Which kind of fruit costs more per pound? Explain.
- b. Bananas cost less per pound than peaches or plums. Draw a line alongside the other graphs that might represent the cost y of buying x pounds of bananas.

Name: Period:

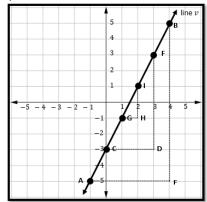
#### Item 1

#### Use the following information to complete the task.

Mrs. Thomas assigned the following graph of line v to a group of students on a big poster.



Joy, Gaby, and Dave are working on the poster together to compute the slope of line v. Joy finds the slope between the points (0, -3) and (3,3). Gaby finds the slope between the points (-1, -5) and (4,5). Dave finds the slope between the points (1, -1) and (2,1). They have each drawn a triangle to help with their calculations (shown below).



#### Part A:

Which student has drawn which triangle? Match the name of the student with the triangle they drew.



#### Part B:

Determine the slope that each student calculated.

Joy:	Gaby:	Dave:
Joy:	Gaby:	Dave:

#### Part C:

Which of the following statements are true? Select all that apply.

- A. The slope of  $\overline{CF}$  is equal to the slope of  $\overline{GI}$ .
- B. The slope of  $\overline{CF}$  is equal to the slope of  $\overline{AB}$ .
- C. The slope of  $\overline{CF}$  is equal to the slope of  $\overline{CD}$ .
- D. The slope of  $\overline{CF}$  is equal to the slope of line v.
- E. The slope of line v is equal to  $\frac{CD}{DF}$ .
- F. The slope of line v is equal to  $\frac{EB}{4B}$
- G. The slope of line v is equal to  $\frac{GI}{HI}$

#### Part D:

Which of the following statements best describes the way that the triangles drawn by the students illustrate the concept of slope calculation?

- A. For each pair of right triangles, we can find the proportion that compares each horizontal leg. This quotient is the slope of the line.
- B. For each pair of right triangles, we can find the proportion that compares each vertical leg. This quotient is the slope of the line.
- C. For each right triangle, we can divide the length of the vertical leg by the length of the horizontal leg. This quotient is the slope of the line.
- D. For each right triangle, we can divide the length of the horizontal leg by the length of the vertical leg. This quotient is the slope of the line.

#### Part E:

Complete the equation of line v in the spaces provided below.

$$y = \left(\begin{array}{c} \\ \\ \end{array}\right) x + \left(\begin{array}{c} \\ \end{array}\right)$$

Starting Ratio:		Bar Model/ Tape Diagram/ Other Model:
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Starting Ratio:			Bar Model/	Tape Diagram/Other Model:
Table:				
Double Number Lines:	Two batches of require 7 cups of Solve to find how flour will be need to 8 batches of	f flour. w much ded for up		Coordinate Grid:

Starting Ratio:		Equation to Represent Proportionality:
<u>Table:</u>		
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# Solve for Rates and Ratios in Multiple Ways

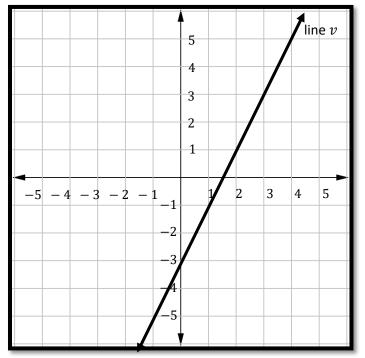
Starting Ratio:		Equation to Represent Proportionality:
<u>Table:</u>		
Double Number Lines:	Carlos bought 6 1/2 pounds of bananas for \$5.20.	s <u>Coordinate Grid:</u>
<u> </u>		
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Name: Period:

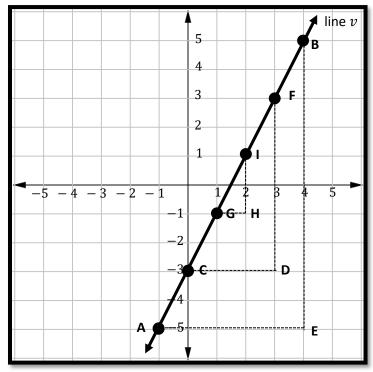
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Calculator Yes Page 1 of 5

#### Part A:

Which student has drawn which triangle? Match the name of the student with the triangle they drew.

Joy Gaby Dave  $\triangle GHI$   $\triangle CDF$   $\triangle AEB$ 

#### Part B:

Determine the slope that each student calculated.

Joy:

Gaby:

Dave:

#### Part C:

Which of the following statements are true? Select all that apply.

- A. The slope of  $\overline{CF}$  is equal to the slope of  $\overline{GI}$ .
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- D. For each right triangle, we can divide the length of the horizontal leg by the length of the vertical leg. This quotient is the slope of the line.

#### Part E:

Complete the equation of line v in the spaces provided below.

$$y = \left(\begin{array}{c} \\ \\ \end{array}\right) x + \left(\begin{array}{c} \\ \end{array}\right)$$

Standard: MAFS.8.EE.2.6 Student Copy

## Item 2

## PART A:

Complete the table to show four points on the same line.

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3	5
	-2

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A line is drawn through the four points. Write the equation of the line in slope-intercept form.

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l		

#### PART C:

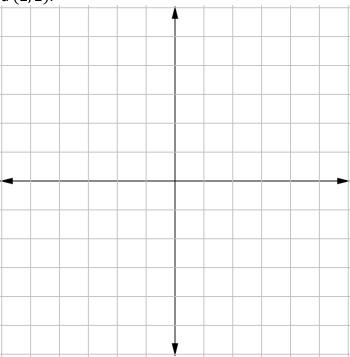
What is another point that falls on this line?

- 1		
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# Item 3

Plot the following points on the given graph in order to answer the questions below:

(-4,-1), (-2,0), (0,1) and (2,2).



### Part A:

Draw a line that connects the four points, then draw two similar right triangles and label them.

#### Part B:

Find the slope of the hypotenuse of the two similar triangles you created in Part A.

Triangle 1:	Triangle 2:

#### Part C:

Compare the slopes of the two triangles. What do you notice?

#### Part D:

Write the equation of the line in the form y = mx + b.

Standard: MAFS.8.EE.2.6 Student Copy

## **Extension:**

Select all points listed below that fall on this same line.

- A. (1,0)
- B. (3,-1)
- C. (4,3)
- D. (-6, -2)
- E. (-9, -17)
- F. (10,6)

Using any of the coordinates above, explain how the points are on the same line.

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