



#### **Brian Bushart**

Elementary Mathematics Curriculum Coordinator

#### **AGENDA**

- Prologue
- Margie's Story
- Anna and Loretta's Story
- Putting It All Together
- Taking It Back to the Classroom

https://bit.ly/NCTM2018NWP











# Notice anything similar?

Jana bought 1 hat and 2 skirts. The hat cost \$28.53, and the skirts cost \$15.88 each. What is the total cost in dollars and cents of the items Jana bought?

4th Grade, Texas STAAR, 2016

6<sup>th</sup> most difficult item out of 48 items

#### Item difficulty

Jana bought 1 hat and 2 skirts. The hat cost \$28.53, and the skirts cost \$15.88 each. What is the total cost in dollars and cents of the items Jana bought?

4th Grade, Texas STAAR, 2016

51% - correct or reasonably close

**33**% - 1 hat and 1 skirt ≈ **1,200 children** 





# Culture of Answer Getting

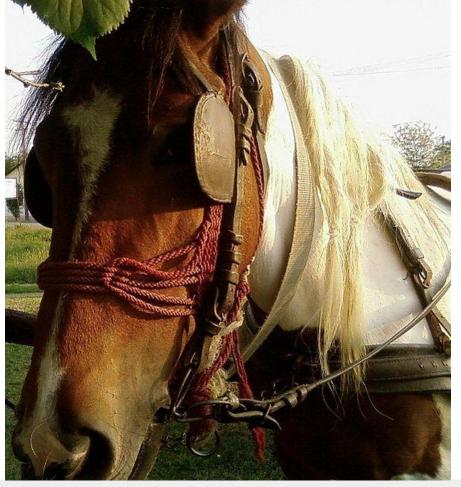
- Blinders on
- Crowding out
- Gaps in understanding



# Culture of Answer Getting

- Blinders on
- Crowding out
- Gaps in understanding







#### Blinders on

Jana bought 1 hat and 2 skirts. The hat cost \$28.53, and the skirts cost \$15.88 each. What is the total cost in dollars and cents of the items Jana bought?



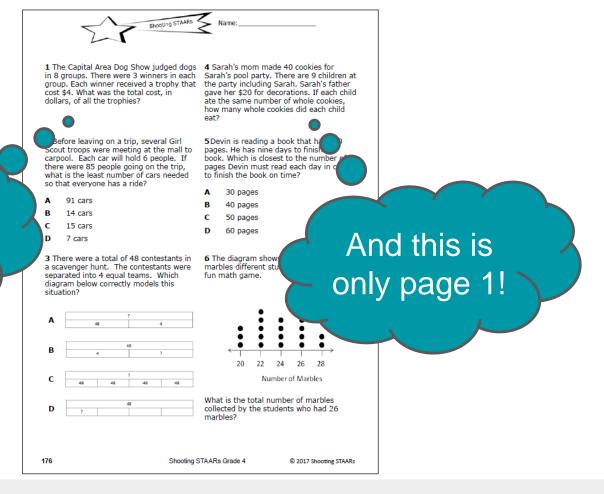
# What's going on?

- Blinders on
- Crowding out
- Gaps in understanding

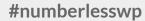


#### Crowding out

Can my thinking go here?

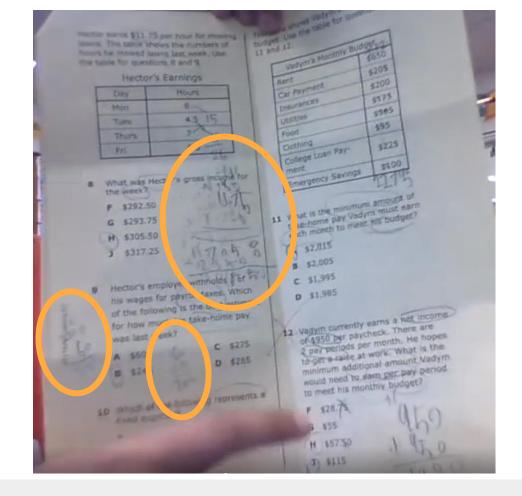








#### **Crowding out**





# What's going on?

- Blinders on
- Crowding out
- Gaps in understanding



# Gaps in understanding

Jana bought 1 hat and 2 skirts. The hat cost \$28.53, and the skirts cost \$15.88 each. What is the total cost in dollars and cents of the items Jana bought?

4th Grade, Texas STAAR, 2016



# Gaps in understanding

Jana bought 1 hat and 2 skirts.



The hat cost \$28.53, and the skirts cost \$15.88 each.

#### Gaps in understanding





Jana bought 1 hat and 2 skirts. The hat cost \$28.53, and the skirts cost \$15.88 each. What is the total cost in dollars and cents of the items Jana bought?

#### Culture of Answer Getting

- Blinders on
- Crowding out
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Answers matter, but we want <u>more</u> than just correct answers.

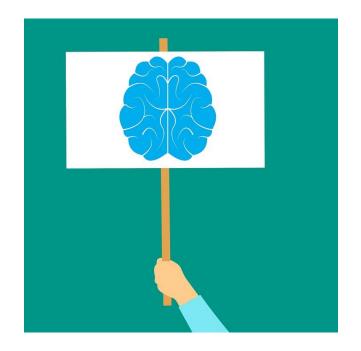






#### Culture of Sense Making

- Take the blinders off
- Provide space and time to think
- Bridge gaps in understanding



# Culture of Sense Making

- Take the blinders off
- Provide space and time to think
- Bridge gaps in understanding

Numberless Word
Problems





- She had some in-class assignments in the first bag.
- She had some homework assignments in the second bag.

- She had 37 in-class assignments in the first bag.
- She had 56 homework assignments in the second bag.

- She had 37 in-class assignments in the first bag.
- She had 56 homework assignments in the second bag.
- She graded some of the in-class assignments on the plane to D.C.

- She had 37 in-class assignments in the first bag.
- She had 56 homework assignments in the second bag.
- She graded 28 of the in-class assignments on the plane to D.C.
- How many in-class assignments does she have left to grade?
- How many assignments does she have left to grade?
- How many more homework than in-class assignments does she have left to grade?

- She had 37 in-class assignments in the first bag.
- She had 56 homework assignments in the second bag.
- She graded 28 of the in-class assignments on the plane to D.C.

Write a number sentence that can be used to find how many assignments Margie has left to grade in the two bags.

Rita had two boxes of ribbons.

- She had 37 large ribbons in the first box.
- She had 56 small ribbons in the second box.
- She gave 28 of the large ribbons to her sister.

Which number sentence can be used to find the number of ribbons Rita had left in the two boxes?



3rd Grade, Texas STAAR, 2016

#### **Features of Numberless Word Problems**

- Reveal information over time
- Situation first, question last
- Reason about relationships and quantities along the way





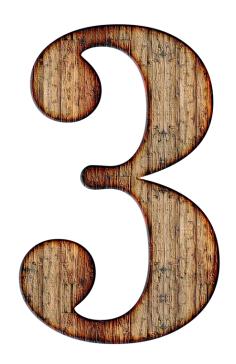
# Setting the Scene





#### Setting the Scene

 Students have struggled with word problems, especially choosing the correct operation.



#### Setting the Scene

- Students were lowest performing on EOY math assessment
- Students were second to lowest on EOY reading assessment



# Creating a Community of Sense Making

- Coaching cycle focusing on Numberless Word
   Problems (Jan – Apr)
- Start by collecting preassessment data

Na	me:
Jan	is collected cans three times last year.
•	<ul> <li>In February she collected 382 cans.</li> <li>In April she collected 475 cans.</li> <li>In June she collect 629 cans.</li> </ul>
	w many more cans did Janis collect in February and April combined than collected in June?
lund	e Union Hill cafeteria sold 273 lunches on Monday. They sold 442 ches on Friday. What is the difference between the number of meals the eteria sold on the two days?



#### **Features of Numberless Word Problems**

- Reveal information over time
- Situation first, question last
- Reason about relationships and quantities along the way

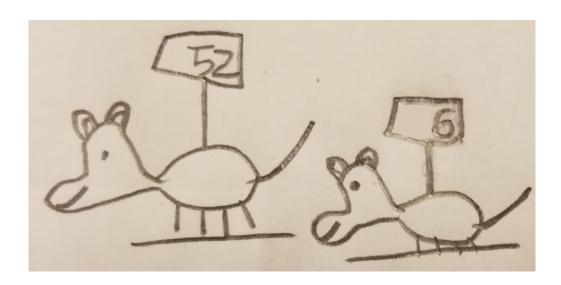
A Chihuahua weighs some number of pounds. A collie weighs some number of pounds.



A Chihuahua weighs 6 of pounds. A collie weighs some number of pounds.



# A Chihuahua weighs 6 of pounds. A collie weighs 52 pounds.



A Chihuahua weighs 6 of pounds. A collie weighs 52 pounds.

How many Chihuahuas will it take to equal the weight of the collie?



A Chihuahua weighs 6 of pounds. A collie weighs 52 pounds. How much heavier is the collie than the Chihuahua?

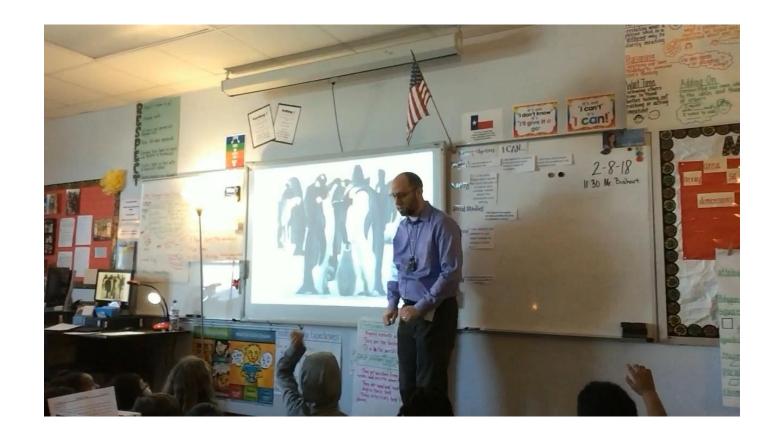






Scientists recently unearthed the fossil of an ancient penguin that was as tall as an adult man!







Scientists recently unearthed the fossil of an ancient penguin that was as tall as an adult man! The largest penguin alive today is the emperor penguin. It is only as tall as a 5-year-old boy and weighs 88 pounds. This is 132 pounds less than the ancient penguin. How much did the ancient penguin weigh?

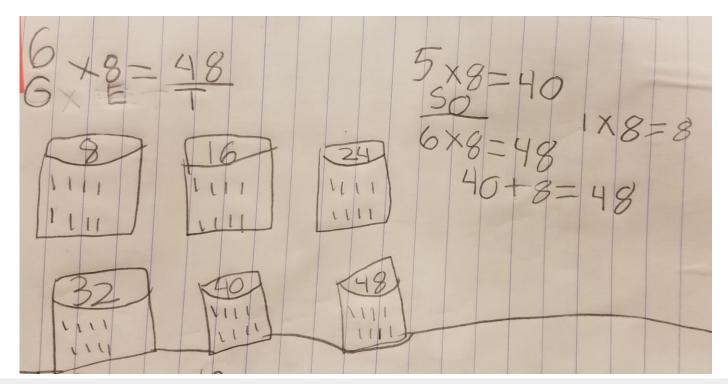






Max and his dad were creating a giant sand castle. They filled up 6 buckets of sand to use. Each bucket held 8 pounds of sand. How many pounds of sand did they use?











Joseph loves Minecraft. He is working on building a larger wheat farm. One section of his wheat farm has 4 equal rows of 6 plants. Another section has 68 plants.





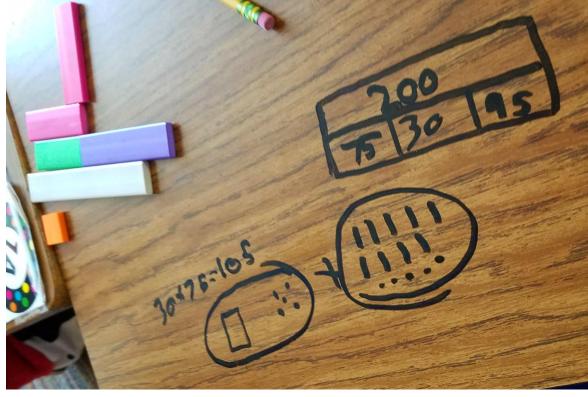




Estrella's goal is to practice her piano for 200 minutes this week.

- On Monday she practiced for 30 minutes.
- On Wednesday she practiced for 75 minutes.









STAAR Ready Assessment Mathematics

> GRADE 3 Spring 2018



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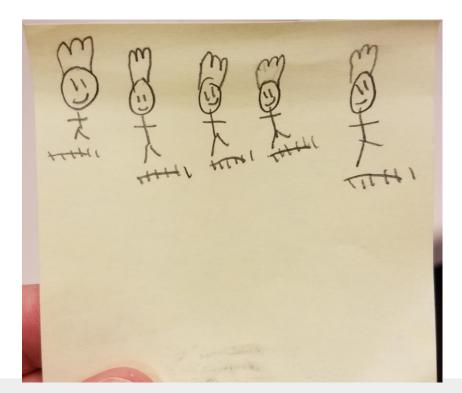
 Analyzed assessment data to provide focused support

@bstockus





Five bakers each made 6 pies. Each pie had 5 slices. Which equation shows one way to find the total number of slices?



# Using Numberless Word Problems

- Respond to students' needs
- Intentional planning over time
- Value sense making, not just answer getting

#### Anna's Feedback

Numberless word problems have been a success in my classroom. The students are making more sense of problems and are able to discuss their thinking WAY more than in the beginning.

They love to notice and wonder, and I feel like NWP have made them slow down, think about, and process operations more than before.

-- Anna Trolinger



#### Anna's Advice

- Highlight just a few noticings and wonderings to save time
- Ask, "What would a mathematician notice or wonder?"
- Avoid "fluff" images on the story slides
- Have students sketch their visualizations on sticky notes (Great formative assessment!)

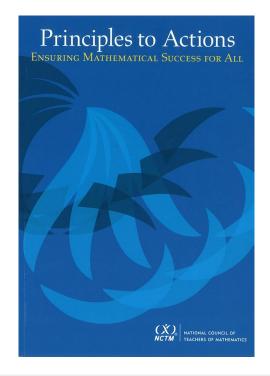




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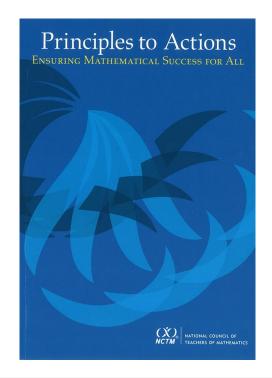
# **Effective Mathematics Teaching Practices**

- Facilitate meaningful mathematical discourse
- Pose purposeful questions



# **Effective Mathematics Teaching Practices**

- Implement tasks that promote reasoning and problem solving
- Use and connect mathematical representations



# Students Who Struggle

"Simple word problems give meaning to mathematical operations such as subtraction or multiplication. When students are taught the underlying structure of a word problem, they not only have greater success in problem solving but can also gain insight into the deeper mathematical ideas in word problems."

--IES Practice Guide "Assisting Students Struggling with Mathematics: Response to Intervention (RtI) for Elementary and Middle Schools"



#### **Students With Disabilities**

"The reliance on key words and procedures often leads to a dependency on adults for help, the learned helplessness that can become a habit for students with learning disabilities...They do not develop a sense of personal agency or confidence that they can learn."

--Judy Storeygard, <u>Count Me In! Including Learners with Special Needs in</u>
<u>Mathematics Classrooms</u>, page 98



# **Emergent Bilingual Students**

"Strategies that promote student discourse offer teachers one way to support their students' sense-making processes. Further, when embedded into teachers' daily mathematics instruction, strategies that promote mathematics discourse allow teachers to monitor the ways in which students are making sense of information."

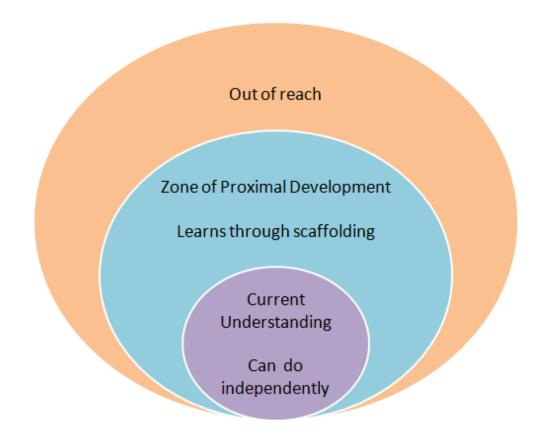
--Lara Dick, et al, "Supporting Sense Making with Mathematical Bet Lines", Teaching Children's Mathematics, May 2016

# Supporting Each and Every Learner

"What if we turn math into literacy?...Here are characteristics of strong readers. It doesn't take much to change this into characteristics of strong mathematicians...Stop cracking the math code already! Make sense making a focus of every single thing you do in your math classroom."

--<u>Annie Fetter, "Sense Making: It Isn't Just for Literacy Anymore", 2015</u> NCTM Annual Conference

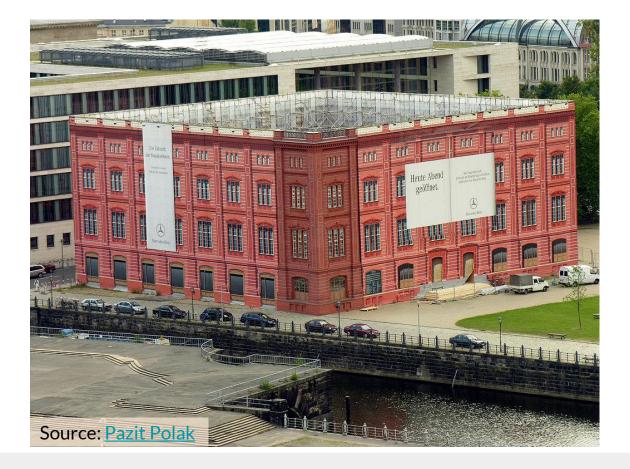


















# Spectrum of Support

- Numberless Word Problems
- 3 Reads
- Removing the Question
- Notice and Wonder

#### https://bit.ly/3ReadsSite









### Start Here - <a href="https://bit.ly/NumberlessWP">https://bit.ly/NumberlessWP</a>

### Teaching to the Beat of a Different Drummer

My place to write about teaching, and math, and teaching math.

HOME ABOUT CONFERENCES & WORKSHOPS PROFESSIONAL DEVELOPMENT #SHADOWCON16

NUMBERLESS WORD PROBLEMS FRACTION RESOURCES TALKING MATH WITH KIDS #ELEMMATHCHAT



Numberless Word Problems

Search

Have you ever said or thought any of the following?



### Anna's Numberless Word Problems

### https://bit.ly/AnnaNWP

<u>The Collie and Chihuahua Problem</u> – This is a comparison problem where the difference is unknown.

<u>The Ancient Penguin Problem</u> – This is another comparison problem. This time the larger quantity is unknown.

The Sand Castle Problem - This is an equal groups problem with an unknown product.

<u>The Minecraft Problem</u> – This is a multi-step problem involving multiplication and addition.

The Piano Practice Problem – This is a multi-step problem involving addition and subtraction.

The Pie Problem – This is a multi-step problem involving multiplication.



### Focus on Sense Making

"Take it in short chunks.

Don't get too bogged down in worrying about the 'answer'. Get excited about watching the process."

-- Christine Mauer, Special Education K-5, Texas





### Pose Purposeful Questions

"When I was first starting to use NWP, I printed out the slide presenter's notes to help me get used to the structure of the questions."

-- Jenna Laib, K-8 Math Specialist, Massachusetts





# Pose Purposeful Questions

- What are you picturing in your mind?
- What changed? What do you know now that you didn't know before?
- What number do you think would make sense here? Why do you say that?
- What questions could we ask about this situation?



### **Student-Generated Questions**



"They can complicate it more than I ever would."

--Leilani Losli, Instructional Coach, Round Rock ISD

https://bit.ly/LosliNWP

### **Student-Generated Numbers**



"When I told them I was not giving them the information and that instead they were choosing their own numbers along with the question they wanted to answer, they were so excited!"

https://bit.ly/MathMindsNWP

-- Kristin Gray, PD Designer, Delaware

### https://bit.ly/SmallGroupNWP

altogether?

### NWP in Small Groups

Mrs. Prentice shipped pints of ice cream to stores on Monday. She shipped three flavors of ice cream.

Mrs. Prentice shipped pints of ice cream to stores on Monday.

- She shipped some pints of chocolate ice cream.
- She shipped some pints of strawberry ice cream.
- · She shipped some pints of vanilla ice cream.

Mrs. Prentice shipped pints of ice cream to stores on Monday.

- She shipped 375 pints of chocolate ice cream.
- She shipped some pints of strawberry ice cream.
- She shipped some pints of vanilla ice cream.

Mrs. Prentice shipped pints of ice cream to stores on Monday.

- She shipped 375 pints of chocolate ice cream.
- She shipped 143 pints of strawberry ice cream.
- . She shipped some pints of vanilla ice cream.

Mrs. Prentice shipped pints of ice cream to stores on Monday.

- She shipped 375 pints of chocolate ice cream.
- She shipped 143 pints of strawberry ice cream.
- She shipped 137 pints of vanilla ice cream.

Jennifer Houghton, Elementary Math Specialist, Texas So what question could I ask you about this situation?

How many pints of ice cream did she ship

How many fewer pints of vanilla ice cream did she ship than chocolate?

How many more pints of chocolate ice cream did she ship than pints of strawberry and vanilla combined?

Next Monday she ships 30 less pints of chocolate ice cream. How many pints of chocolate ice cream does she ship next Monday?

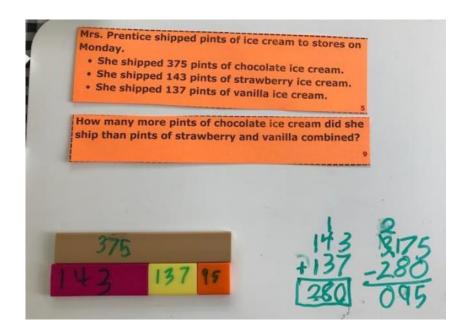


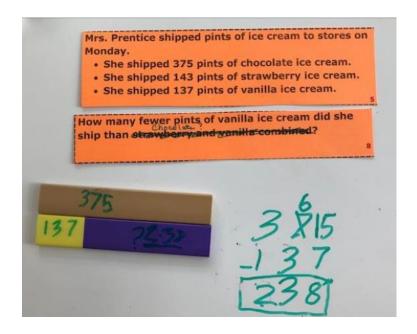






### Bar Models









### **Fun Facts:**

• An anteater's tongue is long and skinny, like a piece of spaghetti.

• An anteater's tongue is about 2 feet long.

Jana Byrd, Alabama Math Science and Technology Initiative



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# bixapañ







### Math In The News

@MathInTheNews

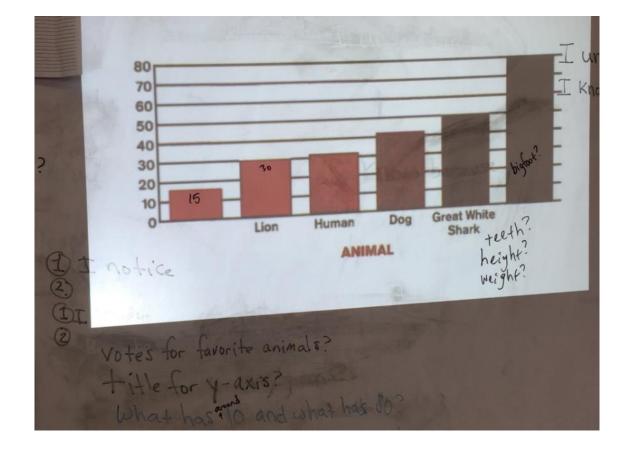
A new math question related to current events every school day.

Joined August 2012



Heidi Fessenden, Teacher, Massachusetts

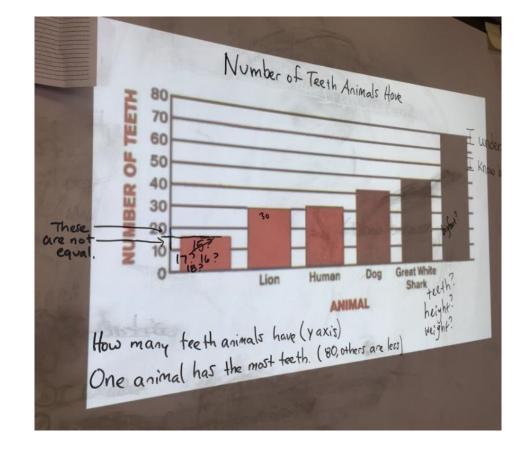
Kassia Wedekind, Math Coach, Virginia





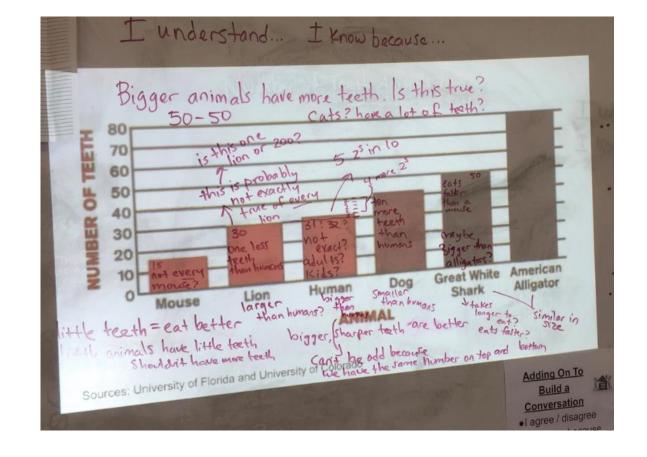
Heidi Fessenden, Teacher, Massachusetts

Kassia Wedekind, Math Coach, Virginia



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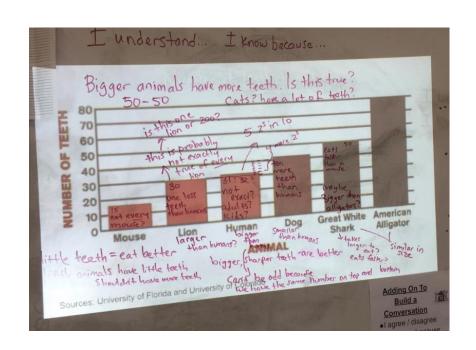
Kassia Wedekind, Math Coach, Virginia





"Is this graph about ONE lion, ONE shark, or MANY lions, MANY sharks? Also, does a human have 31 or 32 teeth? How do we know?"

-- Heidi Fessenden, Teacher, Massachusetts





# "Just try it! It might not go exactly as planned, but it's worth the risk."

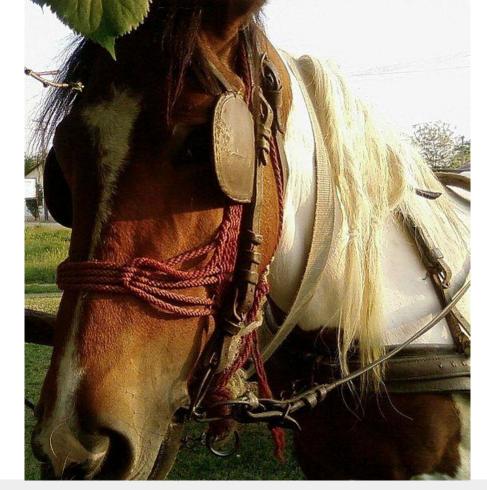
-- Julie Bourke, Michigan, 2<sup>nd</sup> grade teacher







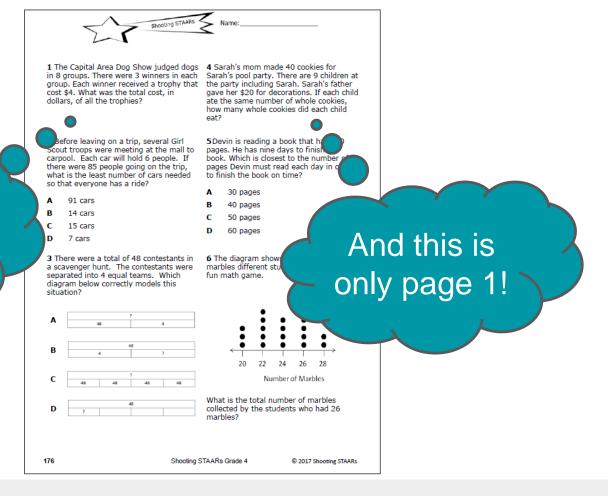
### Blinders On





### **Crowding Out**

Can my thinking go here?





### Gaps in Understanding





Jana bought 1 hat and 2 skirts. The hat cost \$28.53, and the skirts cost \$15.88 each. What is the total cost in dollars and cents of the items Jana bought?

# Culture of Sense Making

- Take the blinders off
- Provide space and time to think
- Bridge gaps in understanding

Numberless Word
Problems

### Be in touch.

brian\_bushart@roundrockisd.org





#numberlesswp

https://bit.ly/NCTM2018NWP







