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# **Ditch That Lecture**

## **Designing Activities For Abstract Topics That Foster Inquiry**

**Session #482  
Friday, 3pm**

**Jim Pardun  
@JimPa23**



***“How do you incorporate this strategy into topics such as polynomial multiplication?  
PLEASE ANSWER THIS ONE!”***



**Dan Meyer**

@ddmeyer

Following



Problem solving workshop Q: "How do you incorporate this strategy into topics such as polynomial multiplication? PLEASE ANSWER THIS ONE!"

1:42 PM - 12 Apr 2013

2 Likes



9



2



Tweet your reply



**Jonathan**

@rawrdimus

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I've seen it in our Algebra II textbook as well. My first year I think I put something like this on an assignment when I was going to have a sub. Naturally, no one figured it out or found it amazing. The whole point is to attach some meaning to the pixelated graph of a polynomial and teach something about maximums. Coincidentally, I saw this a few weeks ago:

Problem solving workshop Q: "How do you incorporate this strategy into topics such as polynomial multiplication? PLEASE ANSWER THIS ONE!"

— Dan Meyer (@ddmeyer) April 12, 2013

I don't know and did not pursue more context to this, but I assume the thought was how do you jazz up something bland and skill based like polynomial multiplication. I remembered that in





**Kerri Sustich**

@MsSustich

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**Zach Cresswell**  
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activities to intro  
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**Nora Greene**

@GreeneMathTeach

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Could use thatRT [@rachelrosales](#): Looking for  
a good real-world application of radical  
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1



**Katrina Newell**  
@MrsNewellsMath

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need

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4



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main  
er

activity,  
the

***“You’re about to hear  
a lecture on how to  
not lecture.”***



# Fostering Inquiry - 5 Things To Know

1.

2.

3.

4.

5.





# Definitions

- **Inquiry** - The natural curiosity that lies within all of us.
- **Inquiry/Problem Based Learning** - A student-centered pedagogy where a specific set of problems / activities are used to trigger curiosity within students.
- **Project Based Learning** - A student-centered pedagogy where students develop a deeper knowledge by working for an extended period of time to investigate a complex question, problem, or challenge.

# Fostering Inquiry - 5 Things To Know

1.

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# Fostering Inquiry - 5 Things To Know

1.  
Group Norms

2.

3.

4.

5.



# 1. Establish Group Norms

**Everyone can  
learn math to  
the highest  
levels.**

**Mistakes are  
valuable.**

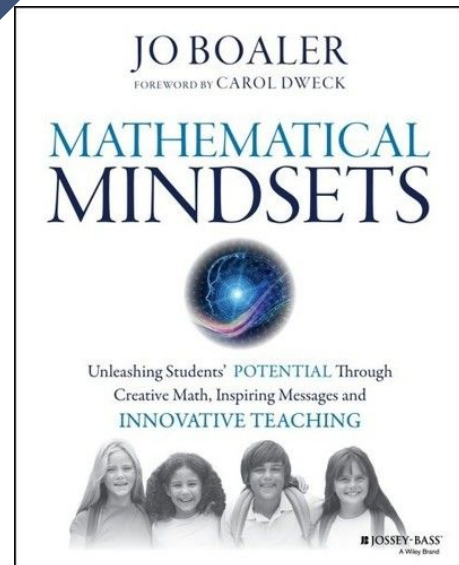
**Questions are  
really  
important.**

**Math is about  
creativity &  
making sense.**

**Math is about  
connections &  
communicating.**

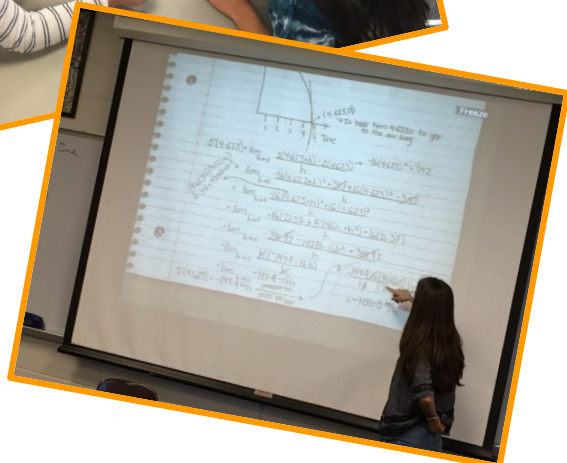
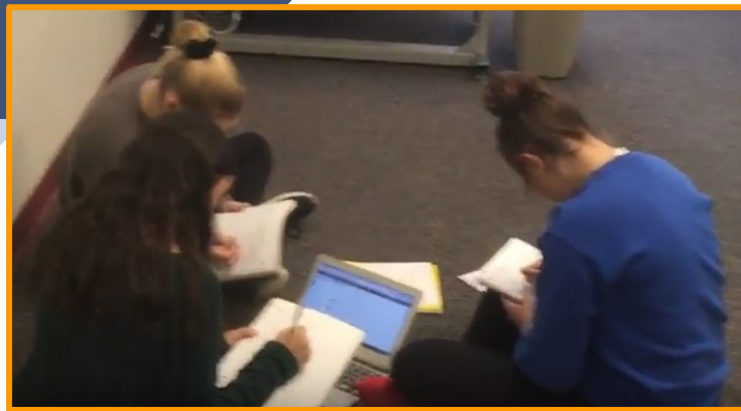
**Math class is  
about learning  
not performing.**

**Depth is more  
important than  
speed.**





# 1. Establish Group Norms



# Fostering Inquiry - 5 Things To Know

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# Fostering Inquiry - 5 Things To Know

1.  
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2.  
Goals

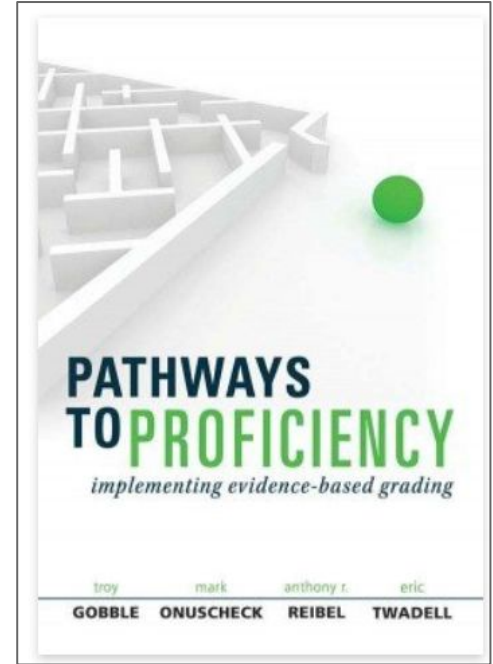
3.

4.

5.

## 2. Goals - Where Are You Going?

- Learning Targets
  - ▷ What skill am I expected to perform?
  - ▷ Why do I need to perform this skill?
  - ▷ How well do I need to perform this skill?
- How will students demonstrate their learning?
- What will assessment look like?



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## 3. Tap Into Prior Knowledge

- Preview Activities
  - ▷ Immediate engagement
  - ▷ Foreshadow upcoming ideas
  - ▷ Worked individually by the student
  - ▷ Primes the brain for what happens next



## 3. Tap Into Prior Knowledge

- [Polygraph](#) by Desmos



Your Partner: Jim Pardun

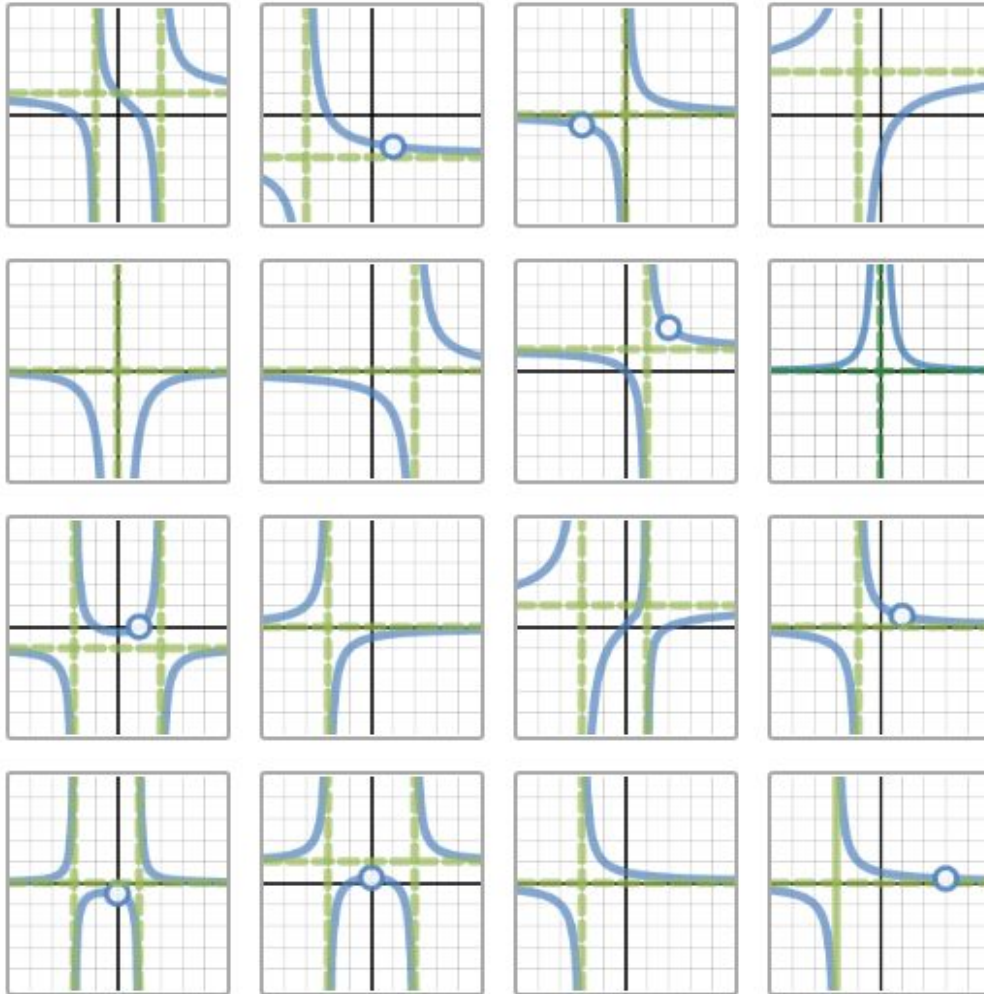
**Yes / No Questions**

**What would your first question be?**

**Your challenge:** figure out which graph your partner picked. Ask a "yes" or "no" question about the graph.




Send

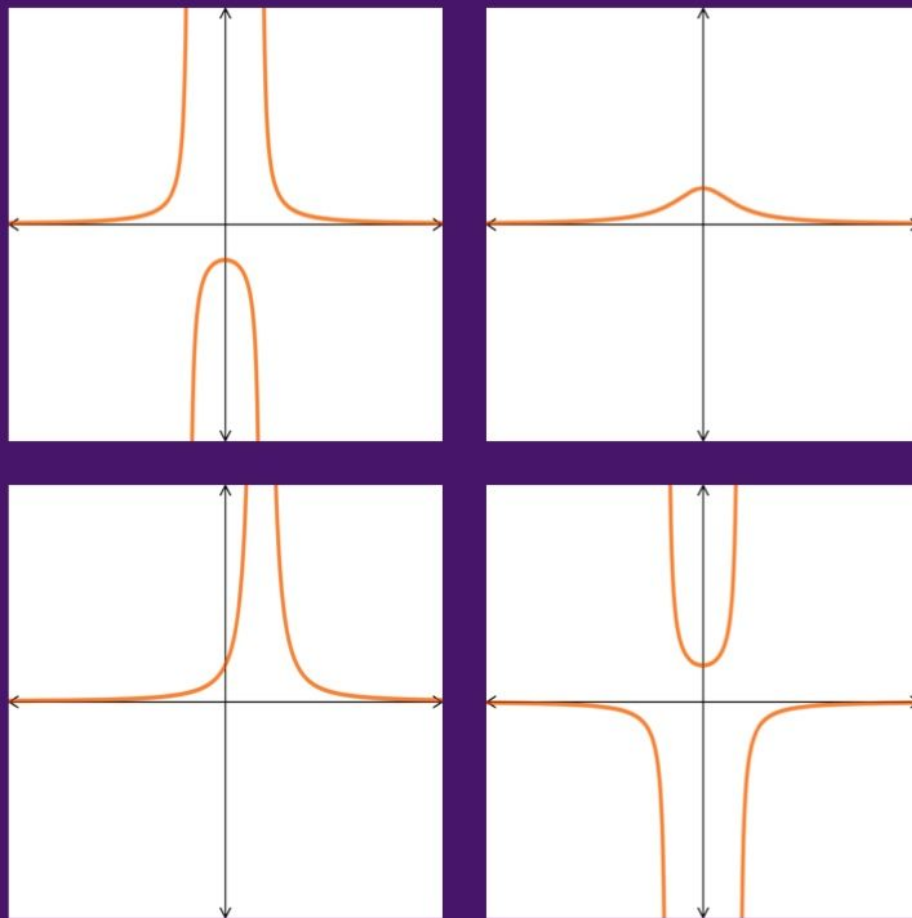




### 3. Tap Into Prior Knowledge

- [Polygraph](#) by Desmos
- [Which One Doesn't Belong](#) (WODB)

**Decide which  
one doesn't  
belong?**



**Tell the person  
sitting next to  
you.**



### 3. Tap Into Prior Knowledge

- [Polygraph](#) by Desmos
- [Which One Doesn't Belong](#) (WODB)
- [Preview Activity](#) - Product & Quotient Rules for Derivatives

## 2.3 The product and quotient rules

**Preview Activity 2.3.** Let  $u$  and  $v$  be the functions defined by  $u(t) = 2t^2$  and  $v(t) = t^3 + 4t$ .

- (a) Determine  $u'(t)$  and  $v'(t)$ .
- (b) Let  $p(t) = 2t^2(t^3 + 4t)$  and observe that  $p(t) = u(t) \cdot v(t)$ . Rewrite the formula for  $p$  by distributing the  $2t^2$  term. Then, compute  $p'(t)$  using the sum and constant multiple rules.
- (c) True or false:  $p'(t) = u'(t) \cdot v'(t)$ .
- (d) Let  $q(t) = \frac{t^3 + 4t}{2t^2}$  and observe that  $q(t) = \frac{v(t)}{u(t)}$ . Rewrite the formula for  $q$  by dividing each term in the numerator by the denominator and simplify to write  $q$  as a sum of constant multiples of powers of  $t$ . Then, compute  $q'(t)$  using the sum and constant multiple rules.
- (e) True or false:  $q'(t) = \frac{v'(t)}{u'(t)}$ .



### 3. Tap Into Prior Knowledge

- [Polygraph](#) by Desmos
- [Which One Doesn't Belong](#) (WODB)
- [Preview Activity](#) - Product & Quotient Rules for Derivatives
- [Preview Activity](#) - Polynomial Functions



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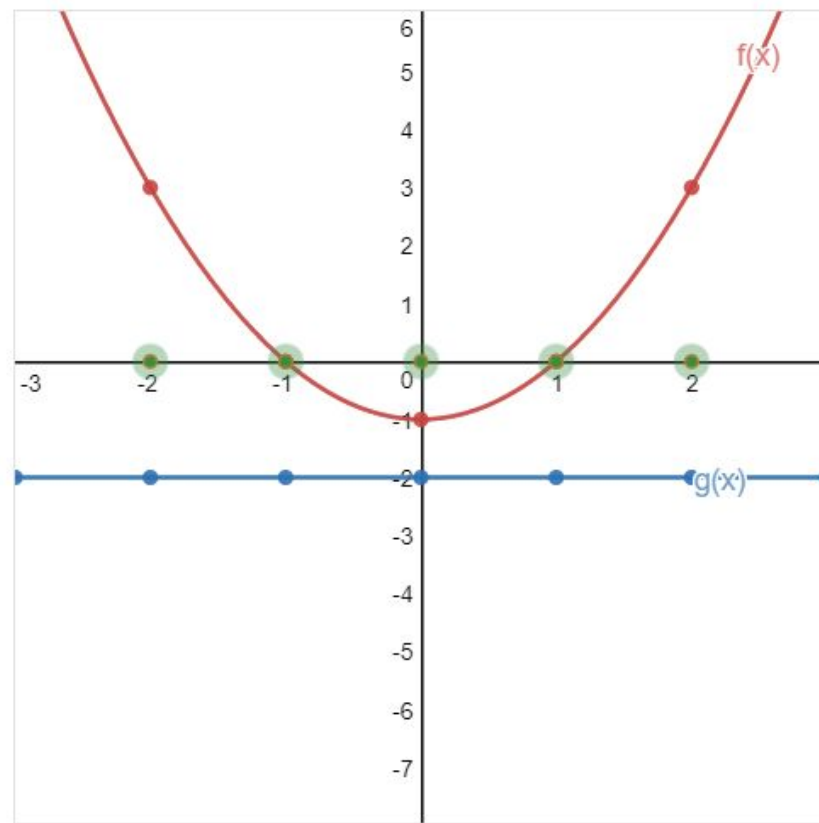
4.  
Bite Sized Tasks

5.

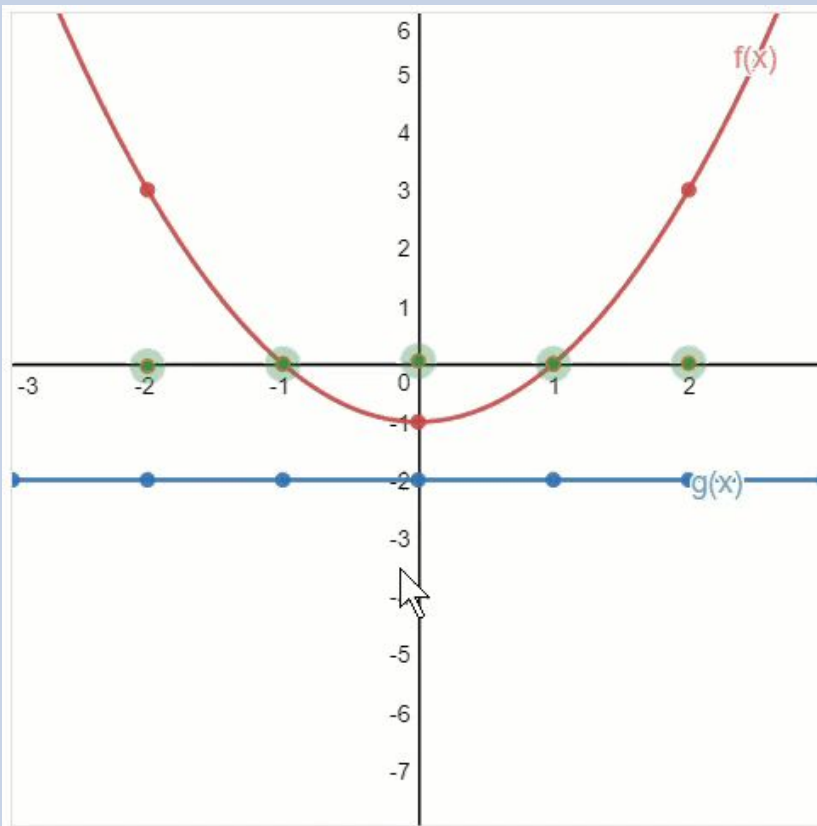


## 4. Bite-Sized Tasks

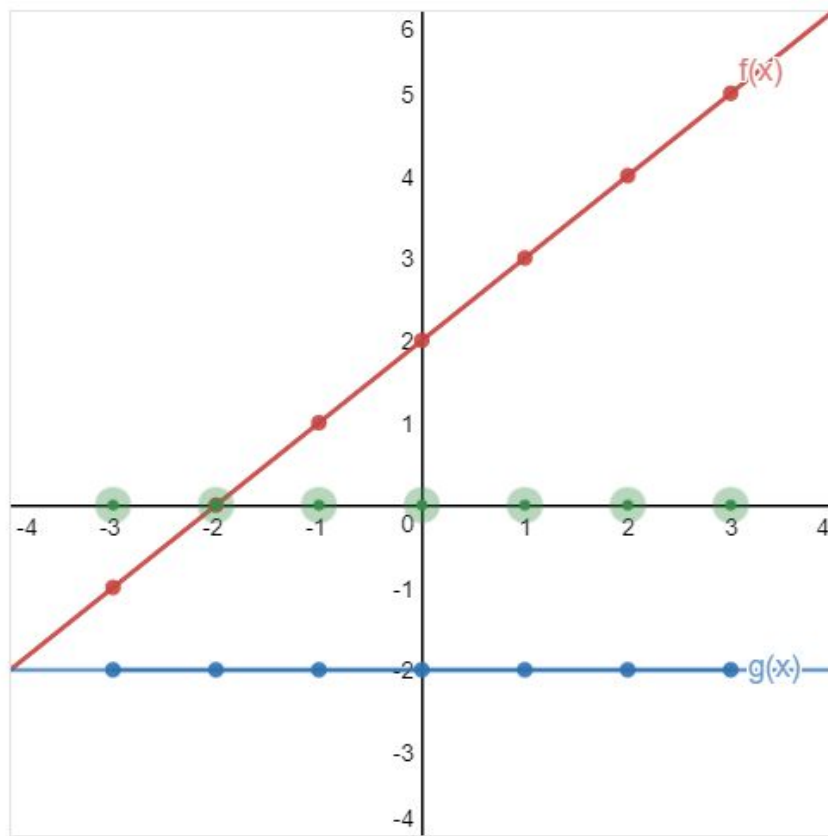
- Graphing Rational Functions - [Activity 1](#)



Drag the green dots to represent the product of  $[f(x)][g(x)]$ .

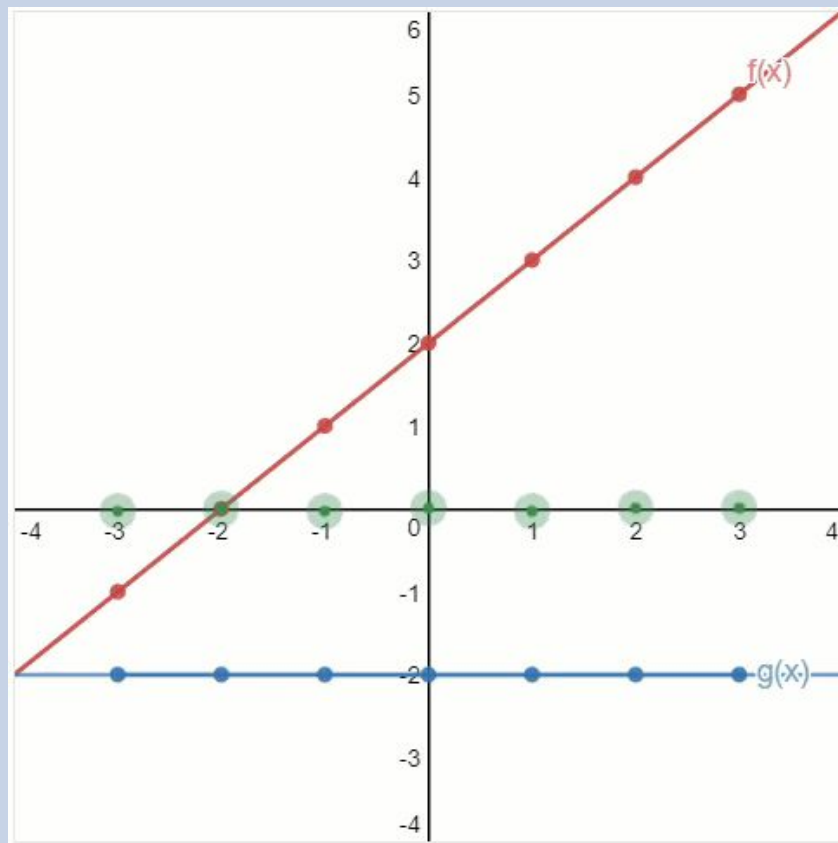


Drag the green dots to represent the product of  $[f(x)][g(x)]$ .

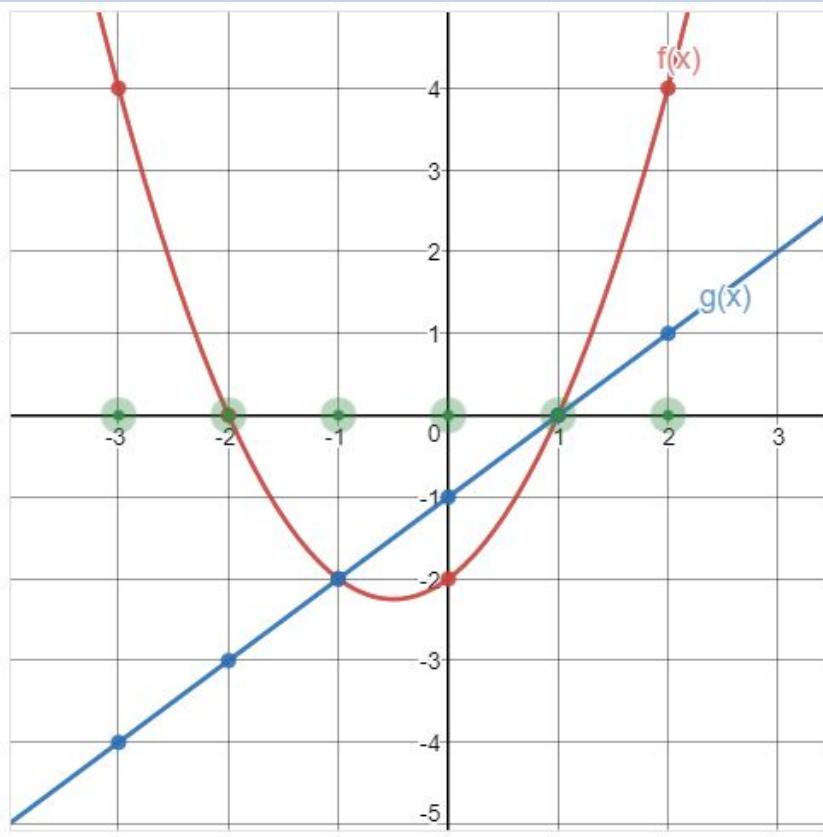


Drag the green dots to represent the quotient  $\frac{f(x)}{g(x)}$ .

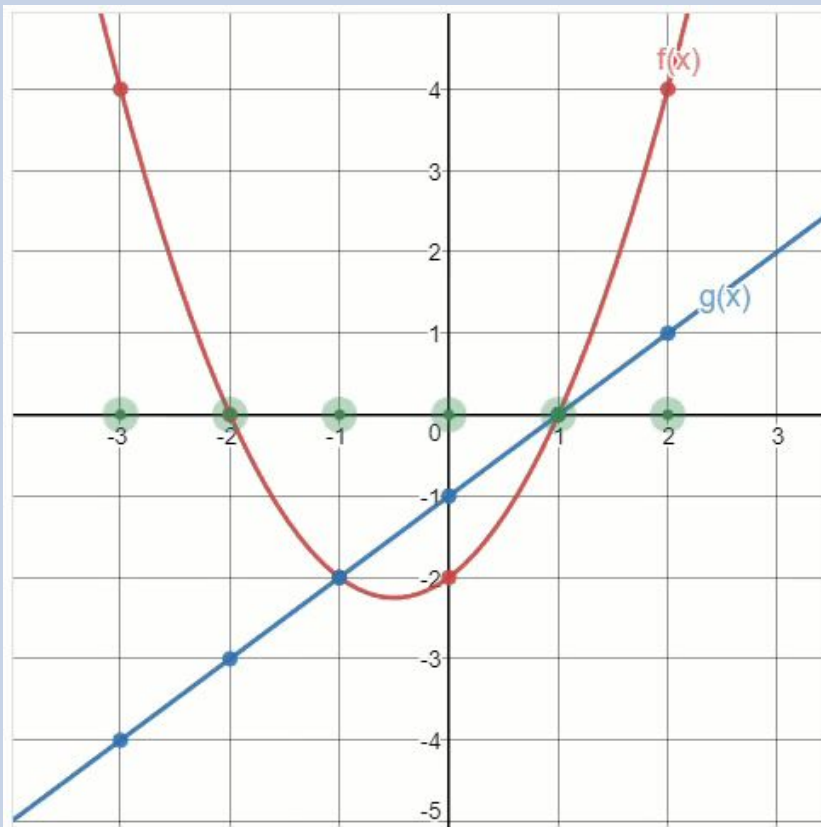




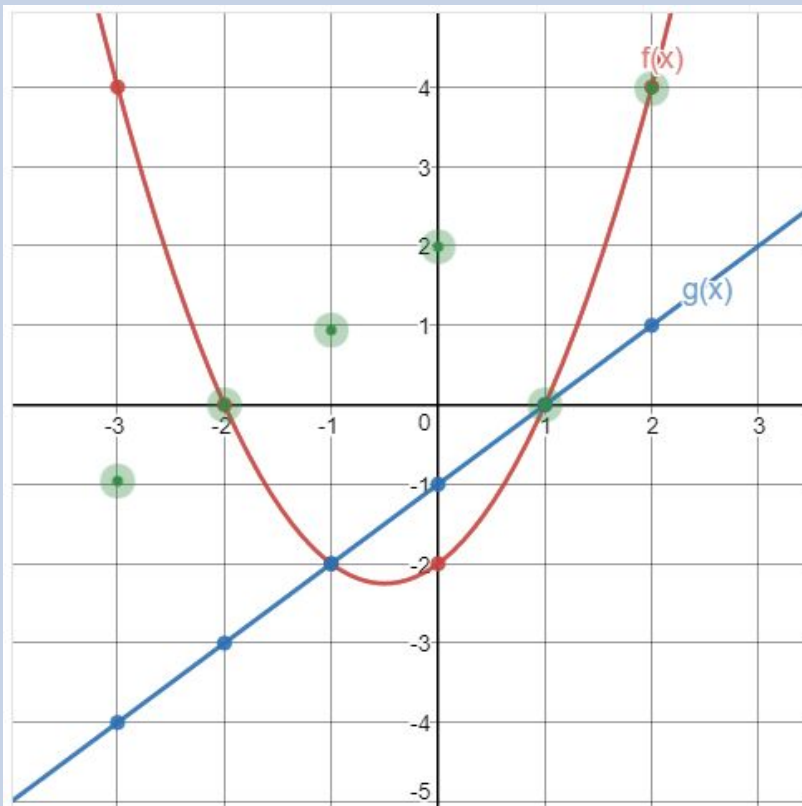
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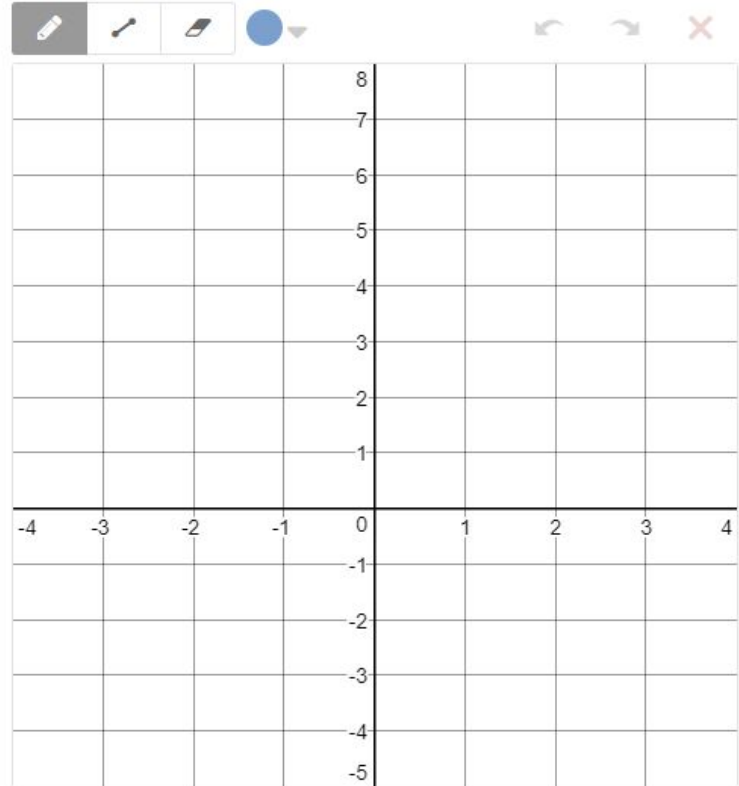
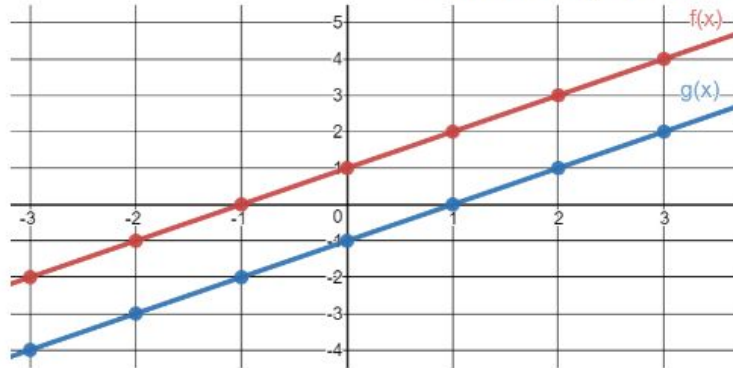
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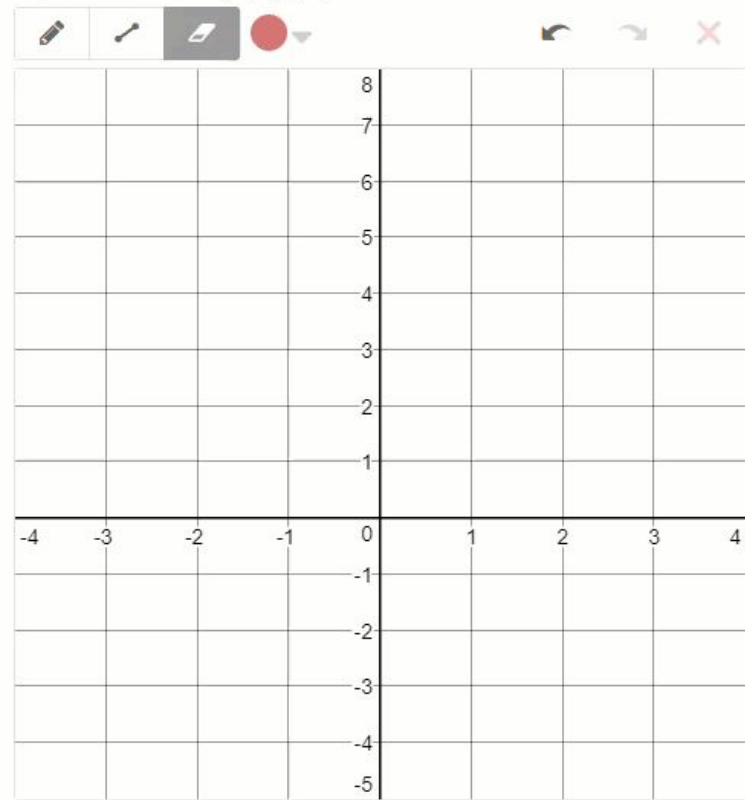
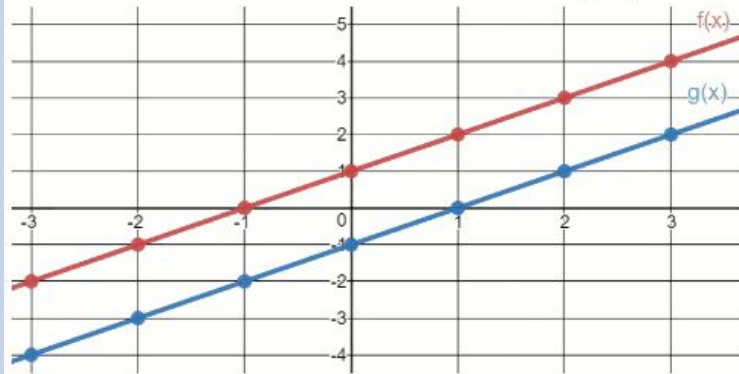
When considering the quotient  $\frac{f(x)}{g(x)}$ , one of those points may have presented a problem. What was the issue? What strategy did you use to overcome the problem?

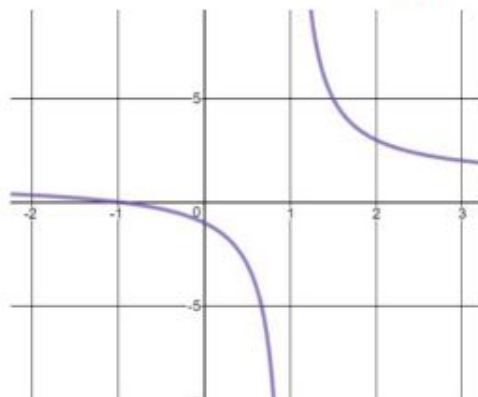
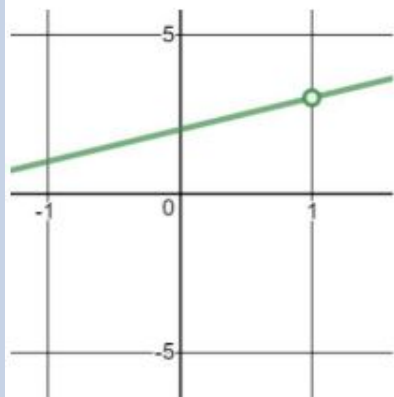
Submit to Class

Sketch a graph of the quotient of  $f(x)/g(x)$



Sketch a graph of the quotient of  $f(x)/g(x)$



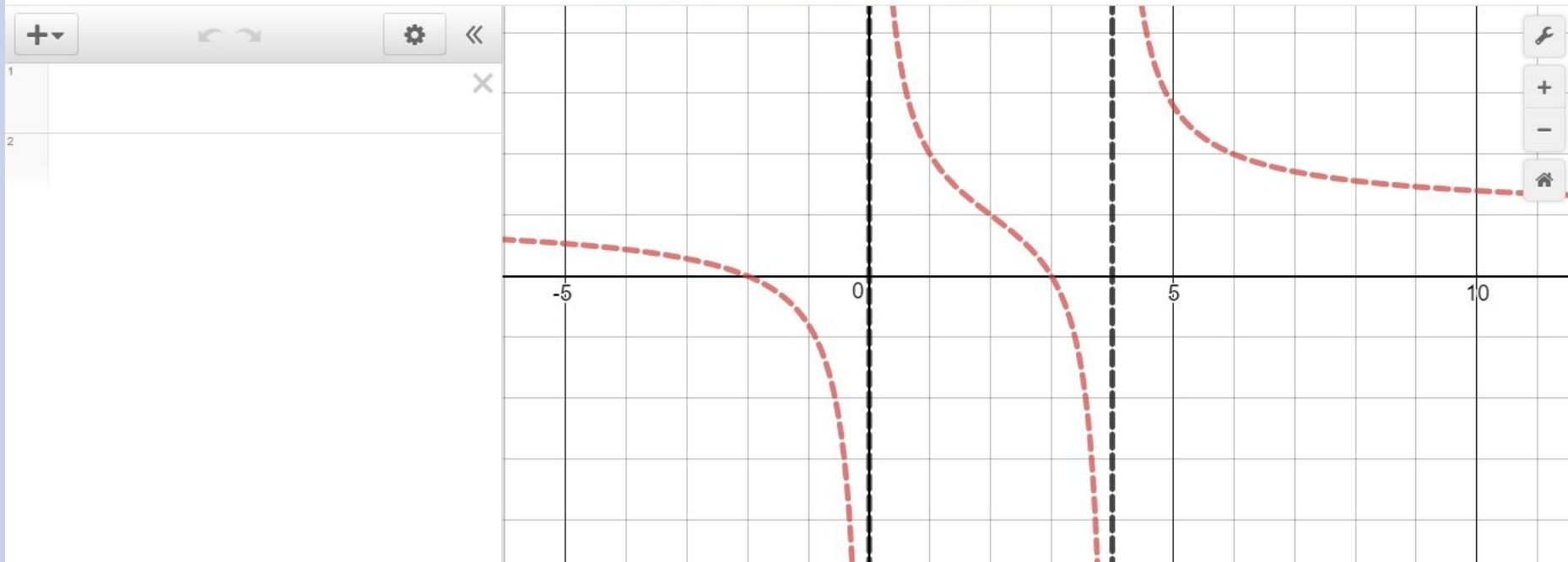


### Take Note...

When dividing functions  $\frac{f(x)}{g(x)}$ , the graph is "undefined" when the denominator has an output of zero. When  $g(x) = 0$ , the result is either a hole in the graph (green graph) or a vertical asymptote (purple graph).

To revisit this concept, go back and explore slide 5, slide 7, or slide 8.

### Challenge 1 - Recreate This Graph







## 4. Bite-Sized Tasks

- Graphing Rational Functions - [Activity 1](#)
- T makes connections & sets up next activity
- Graphing Rational Functions - [Activity 2](#)

## Learning Target 39: Analyzing Rational Functions

### Activity 39.2

Analyze the end behavior of the rational functions by exploring the limit as  $x$  approaches extremely large values and extremely small values. Answer each limit with a specific number, positive infinity  $(+\infty)$ , or negative infinity  $(-\infty)$

$$(a) \ p(x) = \frac{x^6 - 2}{x^6}$$

$$(b) \ a(x) = \frac{5x^6 - 2}{x^6 + 1}$$

$$(c) \ c(x) = \frac{5x^6 - 2}{x^8 + 1}$$

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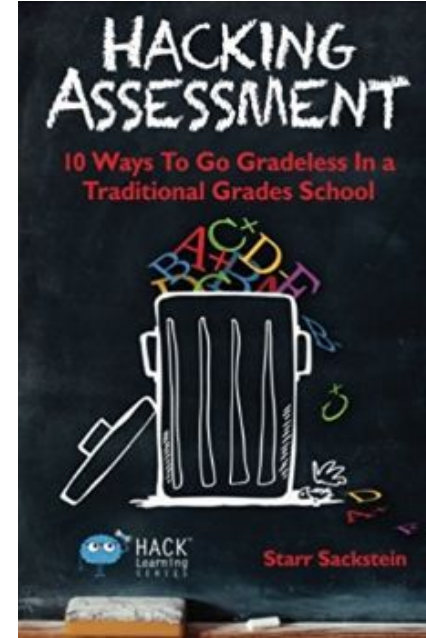
4.  
Bite Sized Tasks

5.  
Student Reflection



## 5. Classroom Discussions & Reflections

- What was your understanding of the activity/task?
- What did you do to achieve success?
- What challenges did you face? How did you respond?
- Provide a convincing description of your solution.
- If you could do it again, what would you do differently?

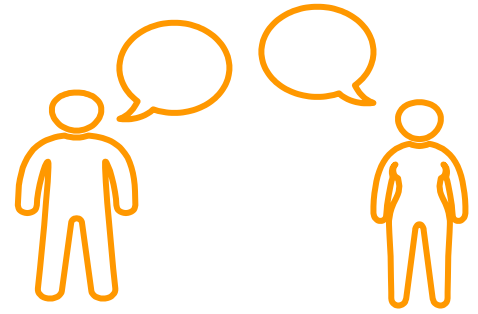


# Preview Activity

- Taps into the prior knowledge of the student
- Immediate engagement for the student
- Foreshadows upcoming concepts
- Completed by the student BEFORE the lesson is taught



# The Activities

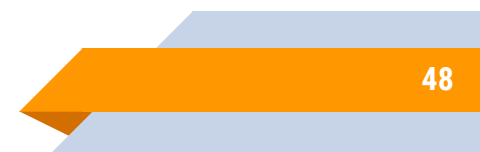


- Breaks the concept down into bite-sized chunks
- Usually 2 - 4 activities per concept
- Inquiry based group work
- Teacher backfills information, debriefs, and makes connections
- Teacher provides examples only when necessary



# The Exercises

- 3 - 4 challenging problems with multiple parts
- Connects key ideas
- Dives deeper into the concept
- Worked individually by the student
- Supplement with drill work (if needed)





# Call To Action

- Establish (and revisit) Classroom Norms
- One inquiry based lesson for an abstract topic
- Be less helpful



# Resources

## Preview Activities

- [Desmos Activity Builder](#)
- [WODB](#)
- [Active Calculus](#)
- [Illustrative Mathematics](#)

## Activities, Tasks, Exercises & Extensions

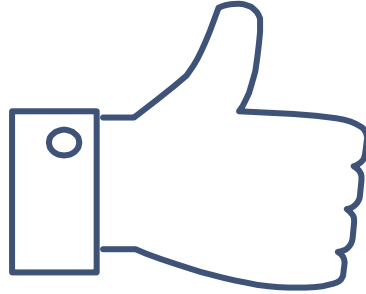
- [Phillips Exeter Academy](#) (problem based curriculum)
- [Brilliant.org](#) (source of rich problems)
- [Active Calculus](#) (inquiry based Calculus book)
- [Illustrative Mathematics](#) (problem based curriculum)
- [Underground Mathematics](#) (source of rich problems)
- [Calendar Problems](#) (MT Magazine)
- [NRICH Mathematics](#) (source of rich problems)
- [Mathematics Vision Project](#) (MVP)
- [MARS](#) (problem based curriculum)
- [Open Middle](#) (source of rich problems)



# Resources

## Books, Articles & Blogs

- [Pathways To Proficiency](#) (Book)
- [Classroom Norms](#) (resource website)
- [Mathematical Mindsets](#) (Book)
- [100 Numbers Task](#) (Sara VanDerWerf)
- [Why Inquiry Fails](#) (David Wees)
- [Engagement In Mathematics](#) (Dan Meyer)
- [Hacking Assessment](#) (Starr Sackstein)
- [Continuous Everywhere But Differentiable Nowhere](#) (Sam Shah)



# THANKS!

Any questions?

You can find me on Twitter

**@JimPa23**

**goo.gl/FTpKbX**

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