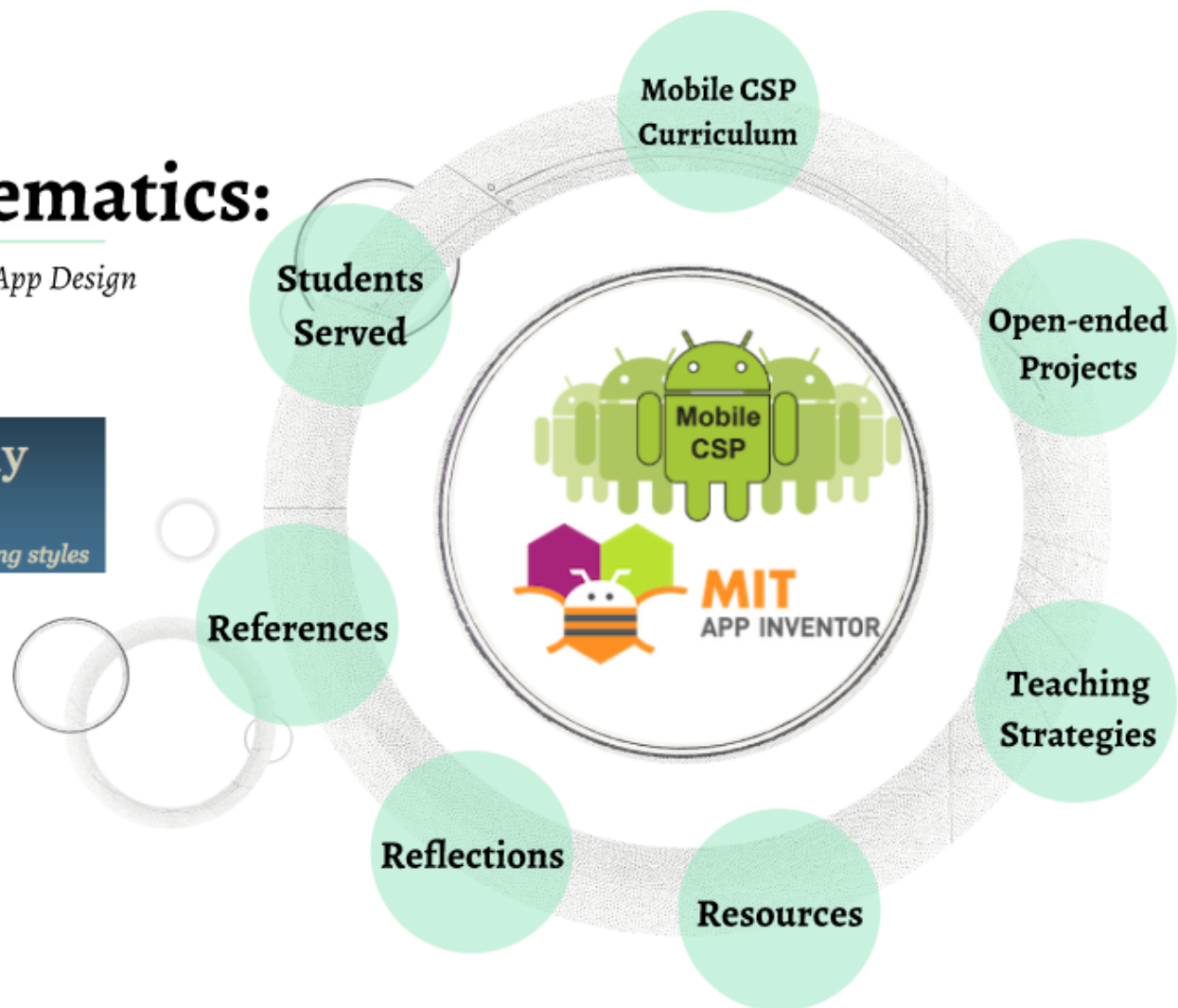


APPlied Mathematics:

The Logic, Algebra, and Geometry of App Design



Amy Bigelow
Math Department Chair
East Haddam, CT
fa-ct.org



Students Served

- Top 12th graders taking AP & College courses
- Top 7th - 10th graders in Pre-Calculus
- 12th grade remedial math students
- 4th - 8th graders with no experience

Top scholars

**Pre-Algebra
students**



Top Scholars

- AIME & USAMO Qualifiers
- Self-taught programmers
- Taking college courses through Wesleyan University & University of Connecticut
- Taken or preparing for AP exams in BC Calculus and Physics C
- Took this as easy, fun elective
- Still struggle with time management and long-term projects
- Now planning to take AP Computer Science Principles exam
 - Involves multiple choice exam, research project, and creating a program and writing a reflection and analysis

Weakest Students

- Struggle to understand the concept of variables
- Not yet comfortable finding percents of numbers
- Taking Life Skills and Common Sense math courses
- Enticed by future jobs in Cyber Security and Game Design
-
- Varied time management and self-advocacy skills
- Dropped the course after first semester
 - Now pursuing paths in Graphic Design, Video Editing, and Multimedia Applications



- One-day hackathons
- 4th - 8th graders with no prior experience
- Design an app that supports a non-profit's mission

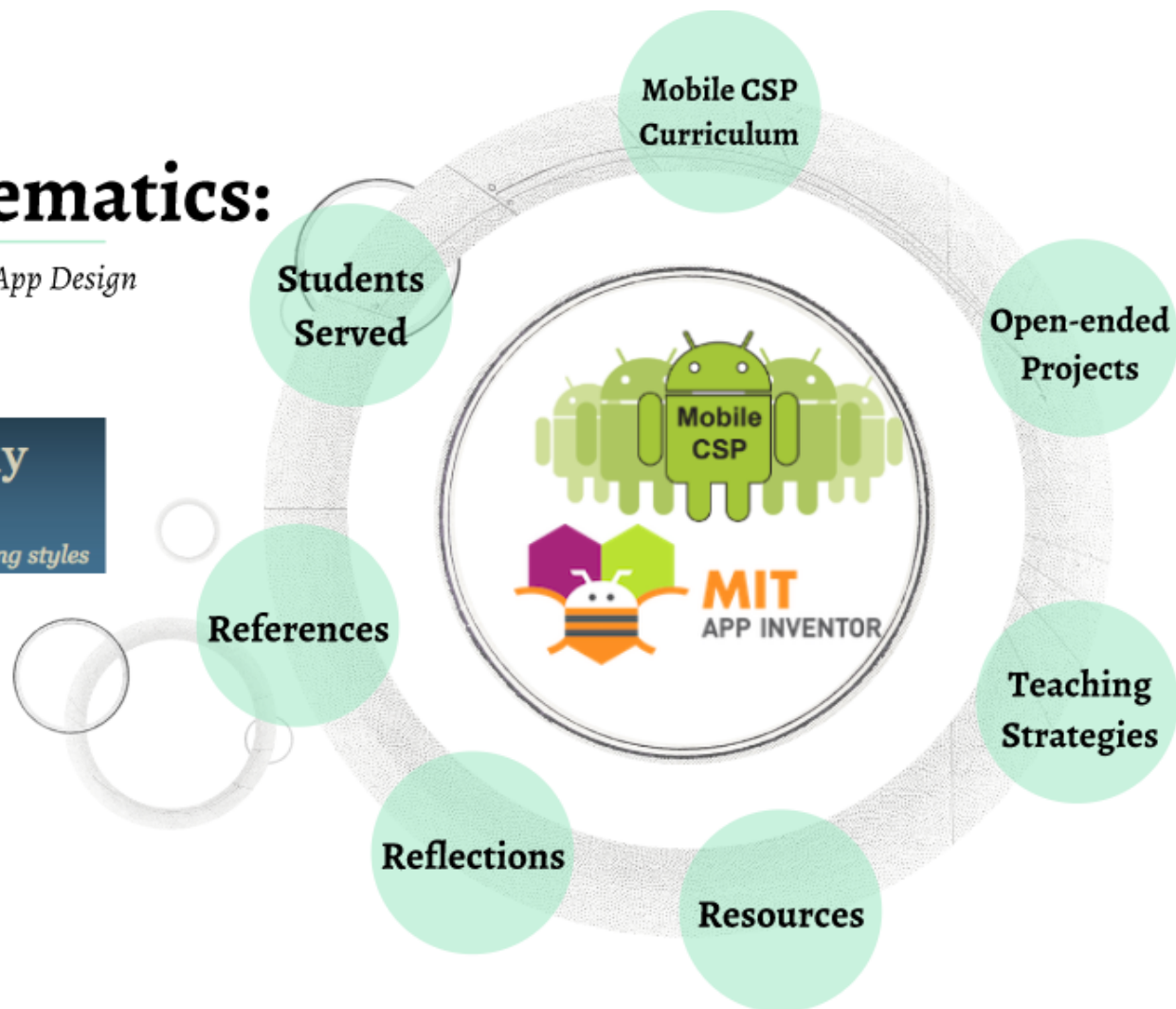


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Mobile CSP Curriculum

- Approved for AP Computer Science Principles
- Uses MIT App Inventor to design Android apps
- Structures:
 - Step-by-step app design with enhancements
 - Website for portfolio write ups
 - Multiple choice with infinite guesses
 - Short programming drills
 - Practice Explore & Create tasks for AP

Math

**Other neat
parts**

The Mathematics in Programming

Variables

Logic

**Number
Theory**

Geometry

**Common
Core
Practices**

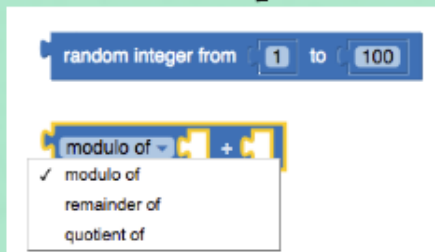
Functions

Common Core Practices

- 1.) Make sense of problems and persevere in solving them**
- 2.) Reason abstractly and quantitatively**
- 3.) Construct viable arguments and critique the reasoning of others
- 4.) Model with mathematics**
- 5.) Use appropriate tools strategically
- 6.) Attend to precision
- 7.) Look for and make use of structure**
- 8.) Look for an express regularity in repeated reasoning**

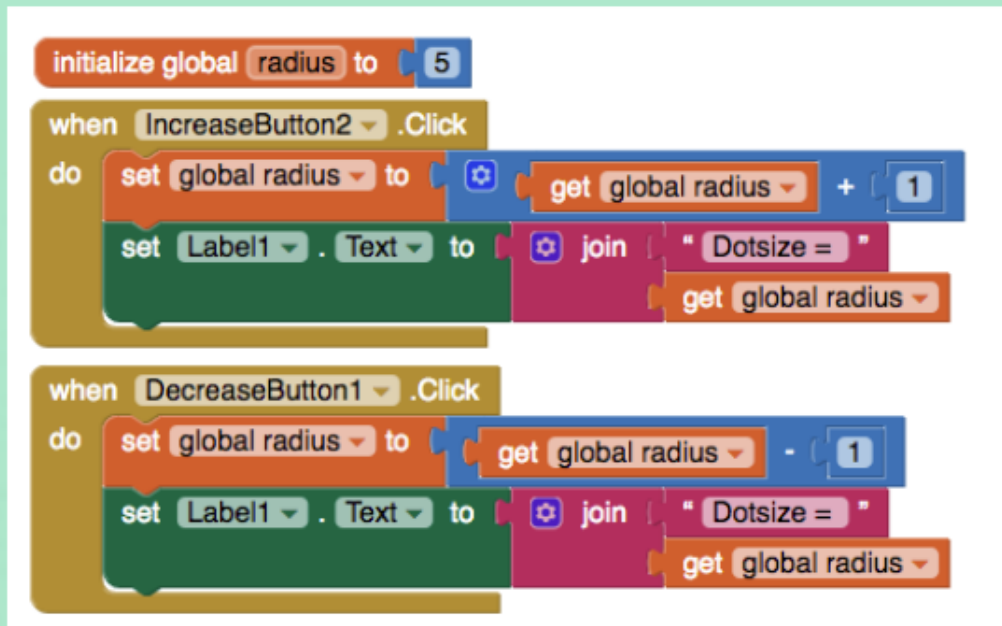
Number Theory

- Using different bases (binary, hexadecimal)
 - With unit conversion (1 byte = 8 bits)
 - Basic combinatorics (How many values can this system encode?)
 - Exponents and very large numbers



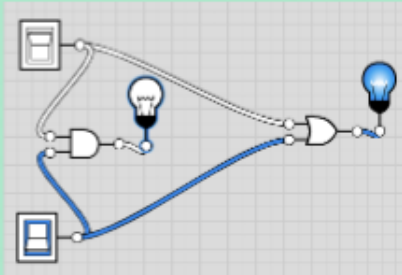
- Modular arithmetic
 - mod 2 for error detection (parity arguments)
 - Pseudo-random number generators (recursion: $x_{n+1} = (2x_n + 1) \bmod 13$)
 - RSA encryption: $m^k \bmod N$, factoring, and relatively prime numbers

Variables



Logic

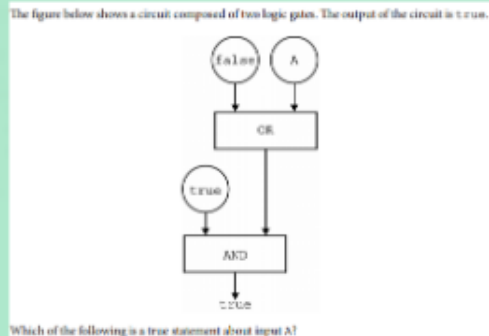
- As physical gates and wiring diagrams
 - Simulated in logic.ly
- Abstracted to truth tables
 - with differences in English



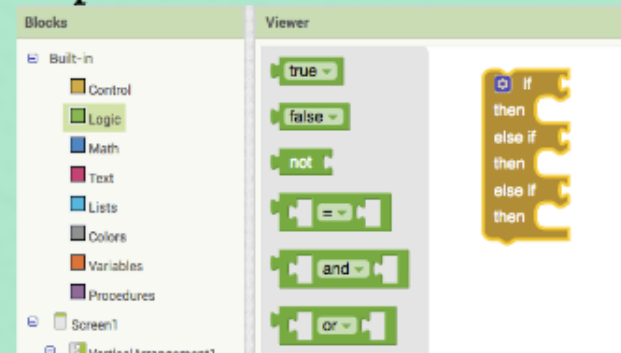
A	B	Z
0	0	
0	1	
1	0	
1	1	

A	B	Z
0	0	
0	1	
1	0	
1	1	

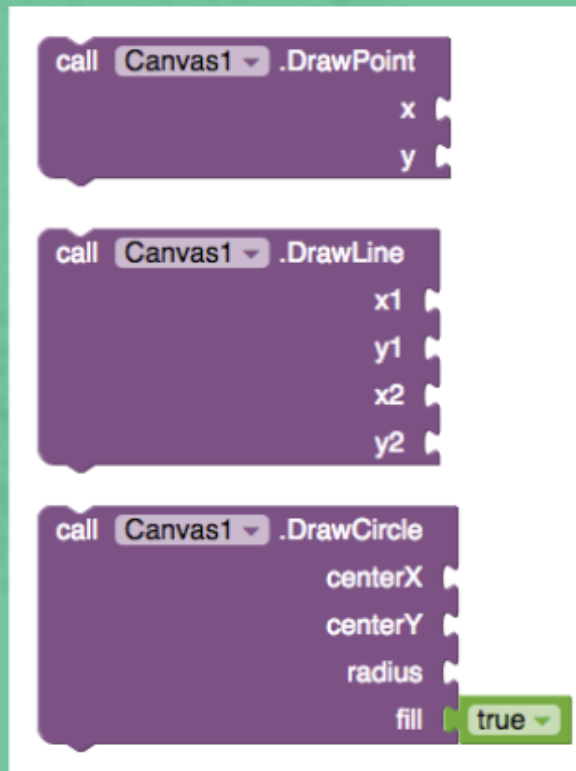
- In flow charts as program outlines



- As parts of useable code



Geometry



- **Determining necessary rotations to produce regular n-gons**

Functions

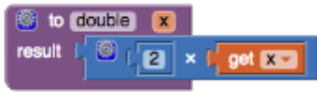
Write a function, double(x), that doubles the value of its single argument.

[Hint](#) [Check Answer](#) [Show Javascript](#)

😊 Correct! Your function passed all 4 of our test cases. Good show!

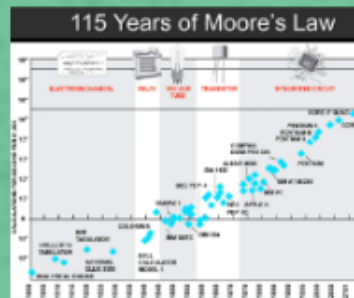
TOOLBOX

- Math
- Procedures
- Variables



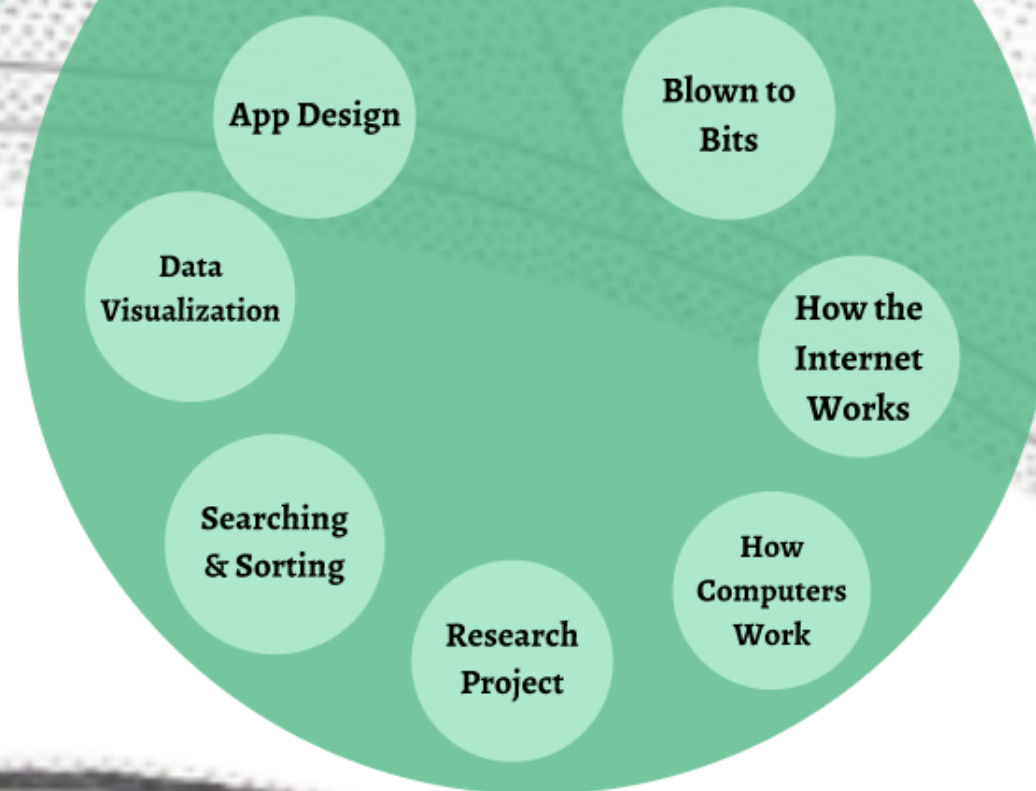
```
function double(x) {
  return x * 2;
}
```

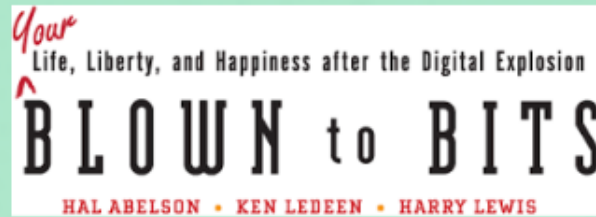
- Moore's Law (exponential growth)



- Comparing run-time of sorting and searching algorithms (logarithmic, linear, quadratic, exponential, factorial)
- Simple substitution ciphers ($f(x)=x+a$)

Not-explicitly-math Parts





- Free as PDF
- Examines issues of privacy and security in the 21st century
- Shows development of technology and how laws and practices connect



Internet Overview

- How was the internet built?
- How open-source protocols function
 - Internet vs. world wide web
- Processing big data (MapReduce)
- Factors determining internet speed
- Understanding IP addresses and how data is transferred and processed online

How Computers Work

- Parts of a computer (RAM, CPU, integrated circuits)
 - Machine language, Assembly language,
High level languages
- How graphics & sounds are expressed using 0's and 1's

Practice for AP CSP

Explore Task

- Research a computing innovation
- Write ~1 paragraph explaining:
 - Its impact on society (benefits & drawbacks)
 - How the device deals with data
- Find relevant, recent sources and cite them
- Make a non-prose description of what the innovation does

Searching & Sorting Algorithms

- Searching
 - Linear
 - Binary
 - When to use each
 - Rough overview of Google's search algorithm
- Sorting
 - Bubble sort
 - Merge sort
 - Radix sort
- Run-time/complexity

Data Visualization

- How to spot a misleading graph
- Using spreadsheets to add, average, find extremes
- Making charts & graphs with Google Sheets
- Drawing conclusions from visual representations

App Design

**Using
Databases**

Soundboards

Quiz Games

Painting

Logo Simulator

Map Tours

Whack-a-Mole

Soundboards

Provided template



Emotions Project

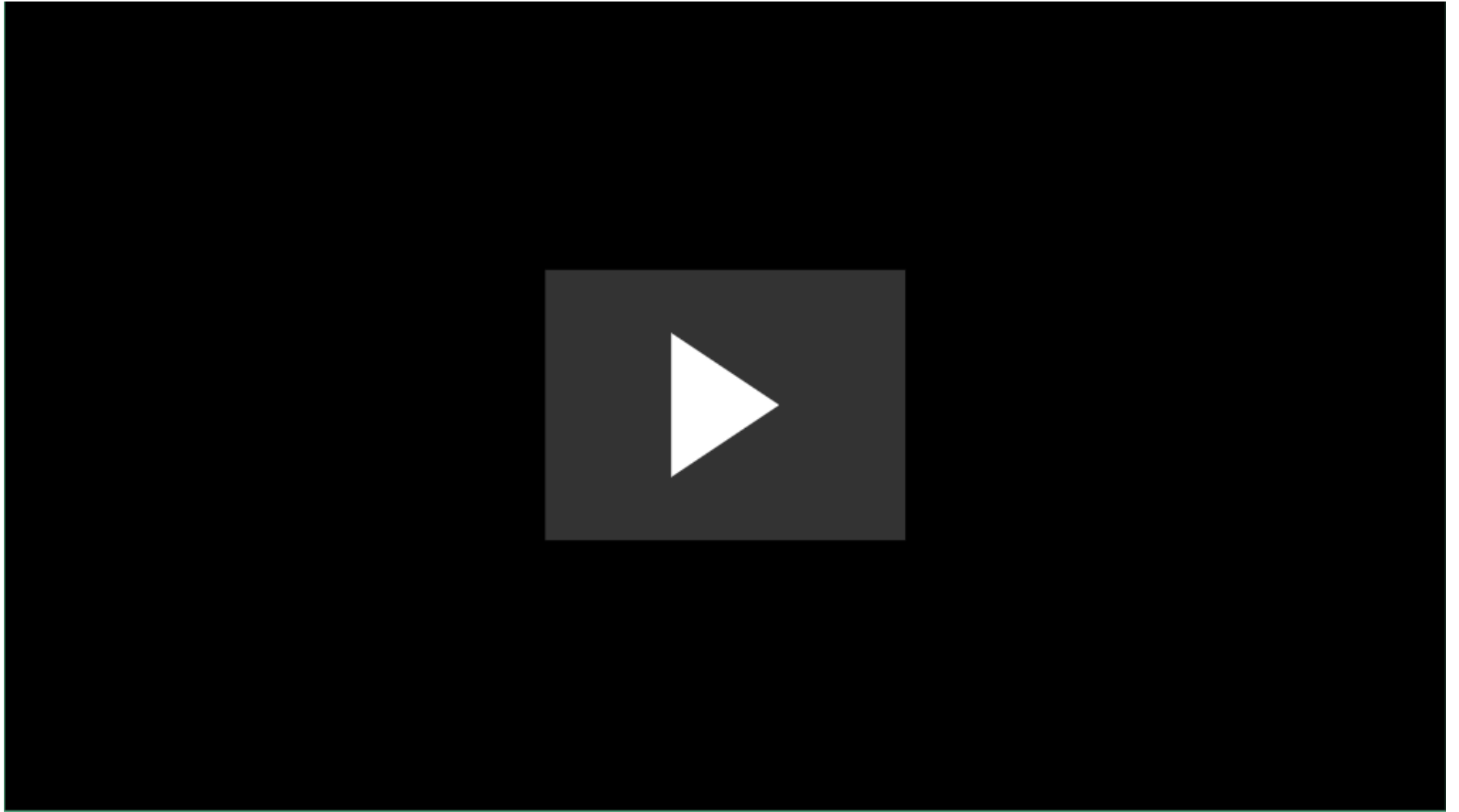


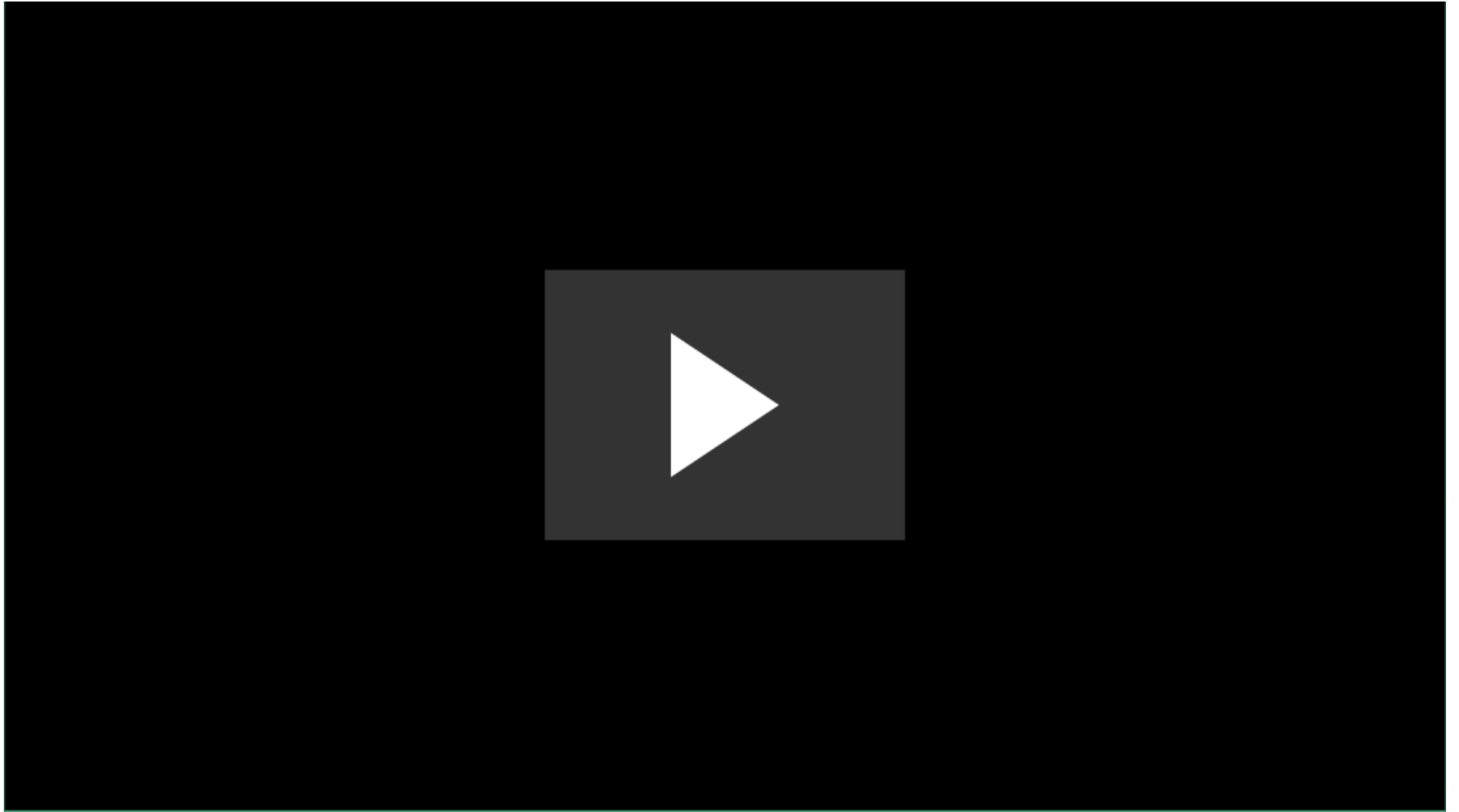
Animals Project

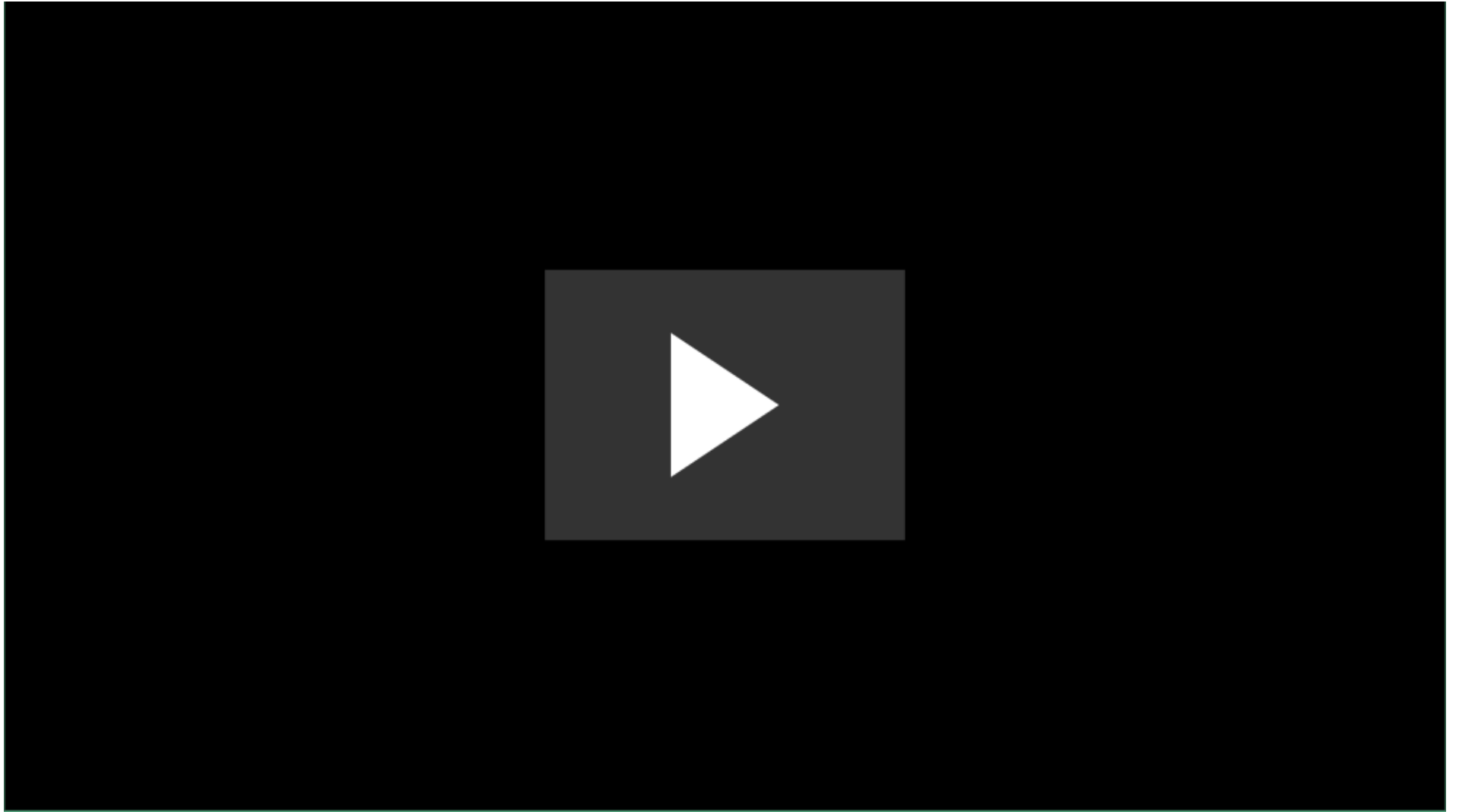


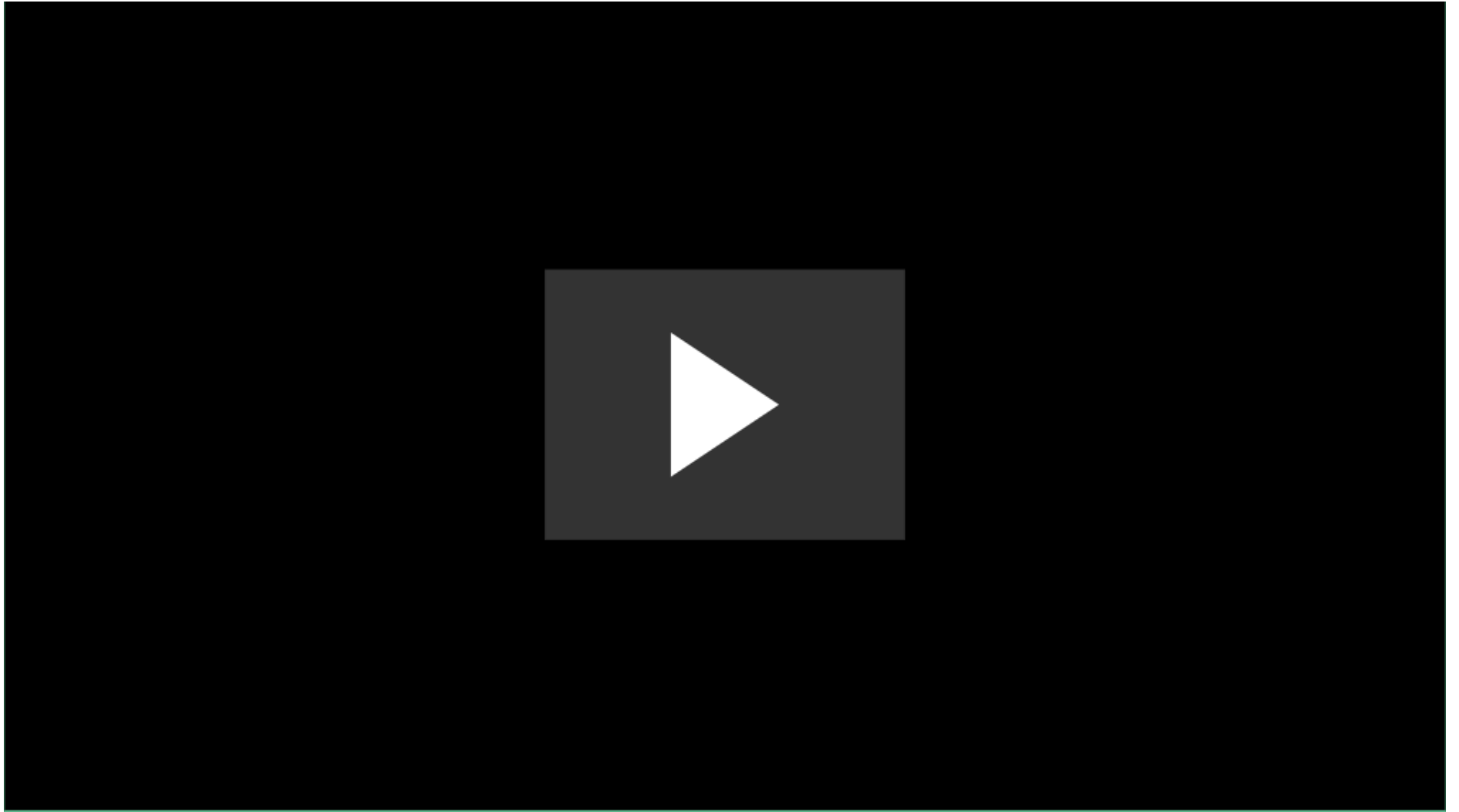
Trump Project











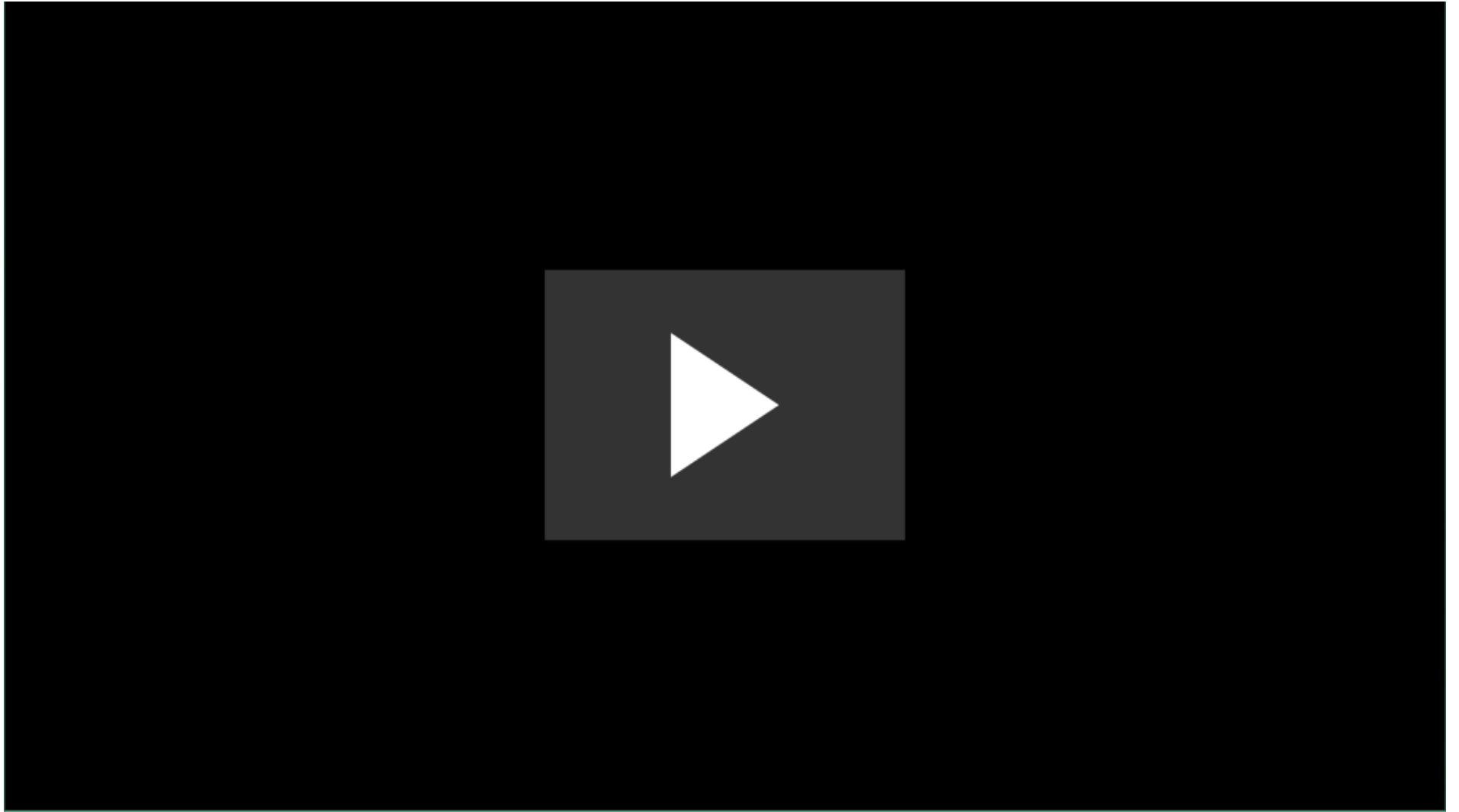
Painting

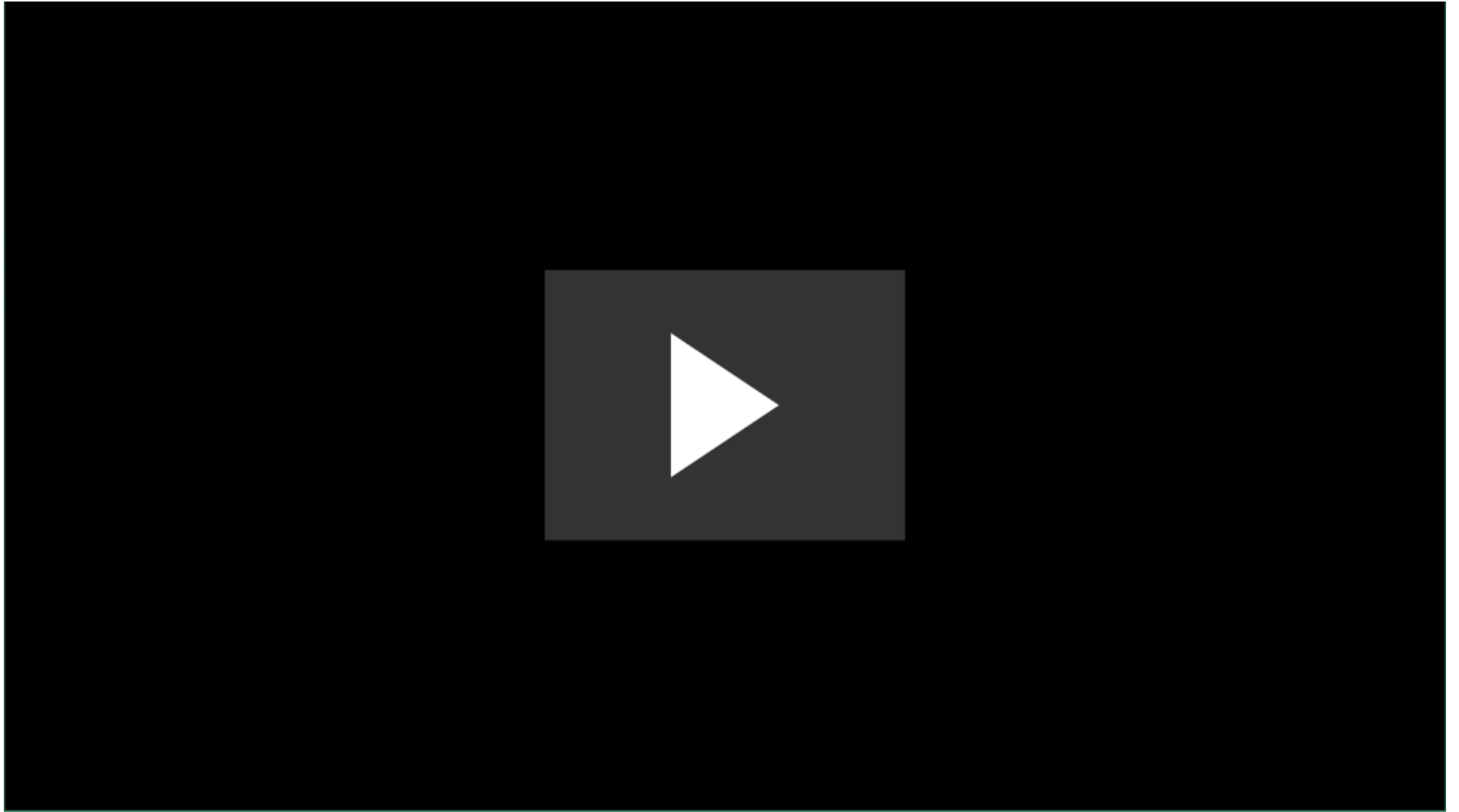
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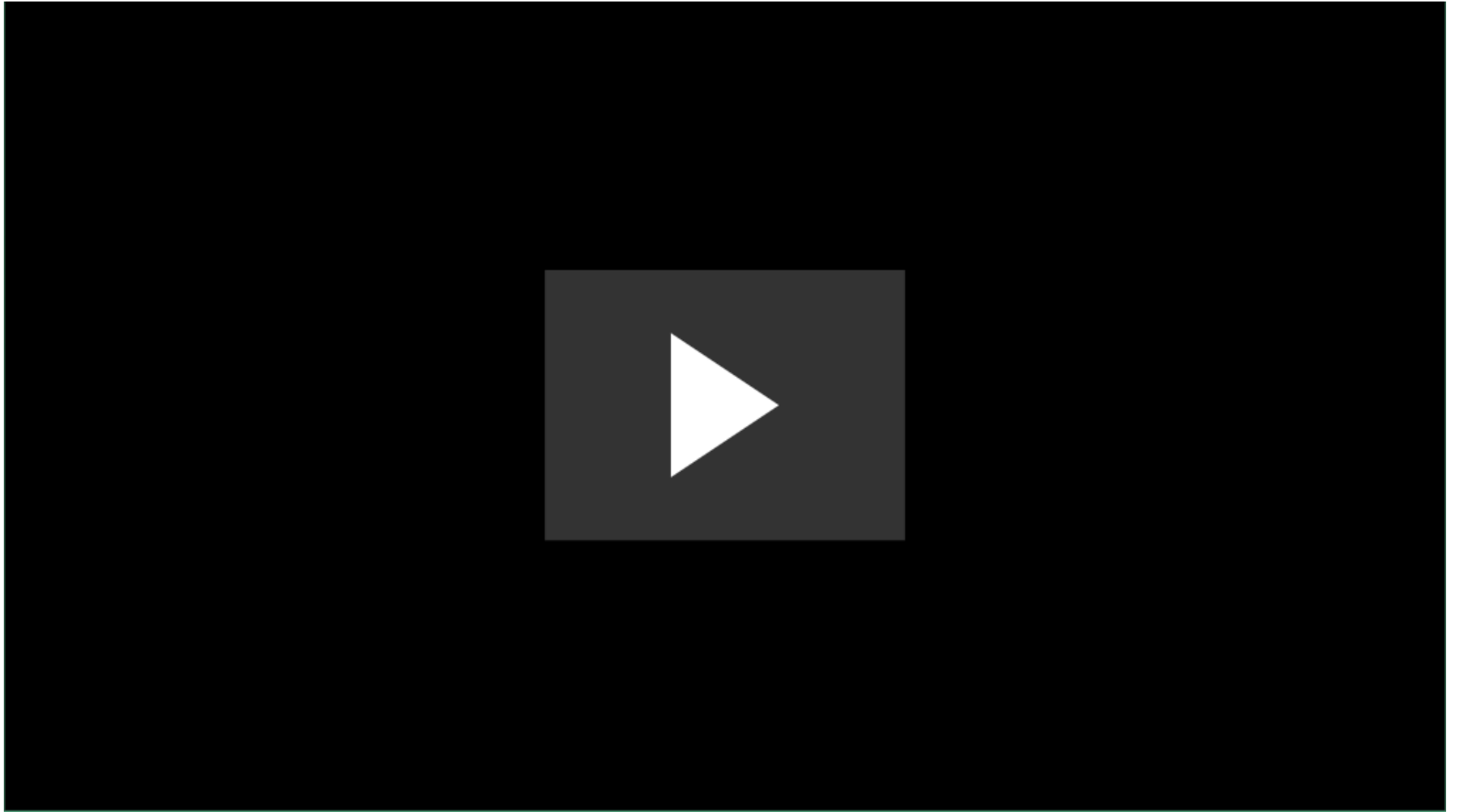


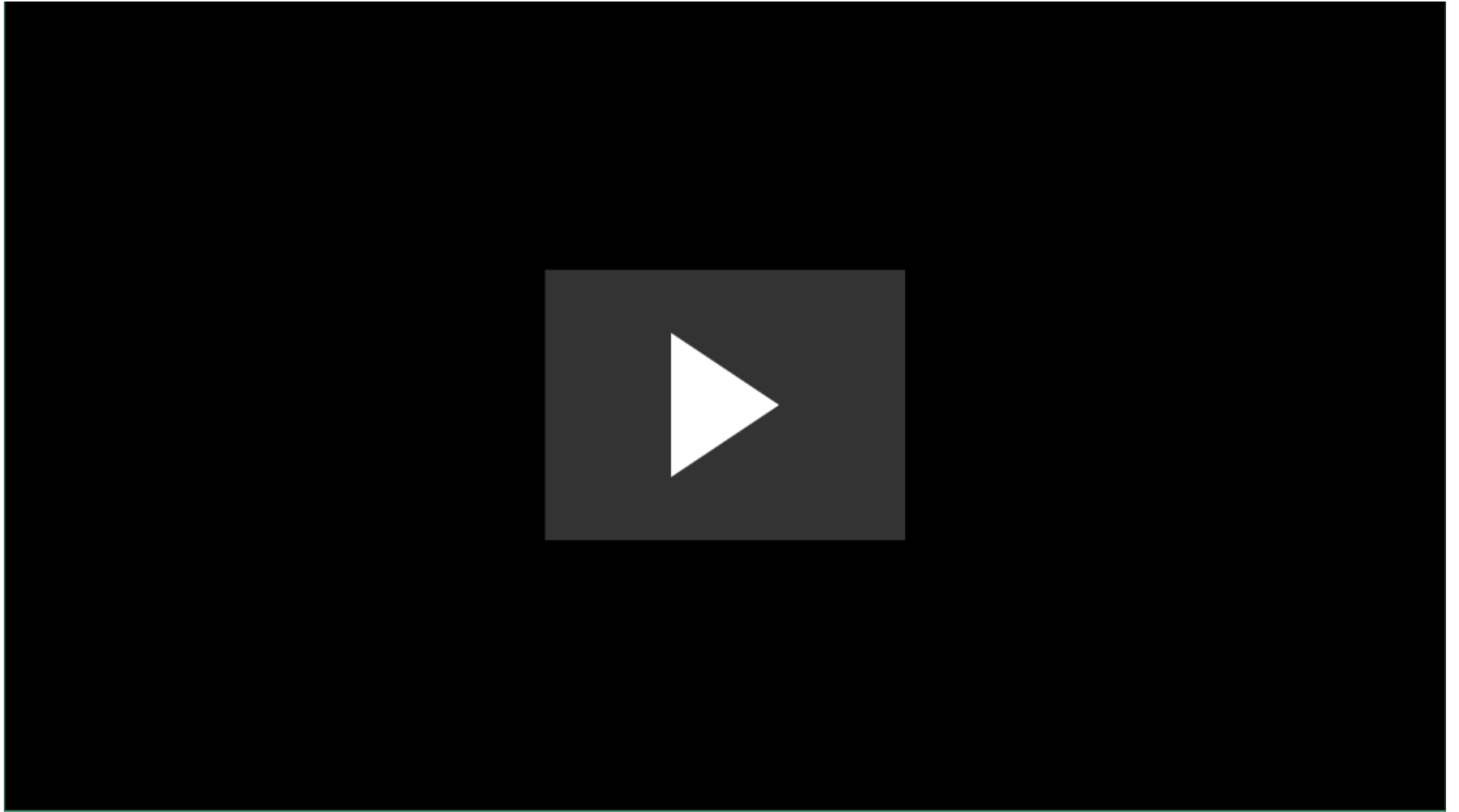
Personalizations & Enhancements



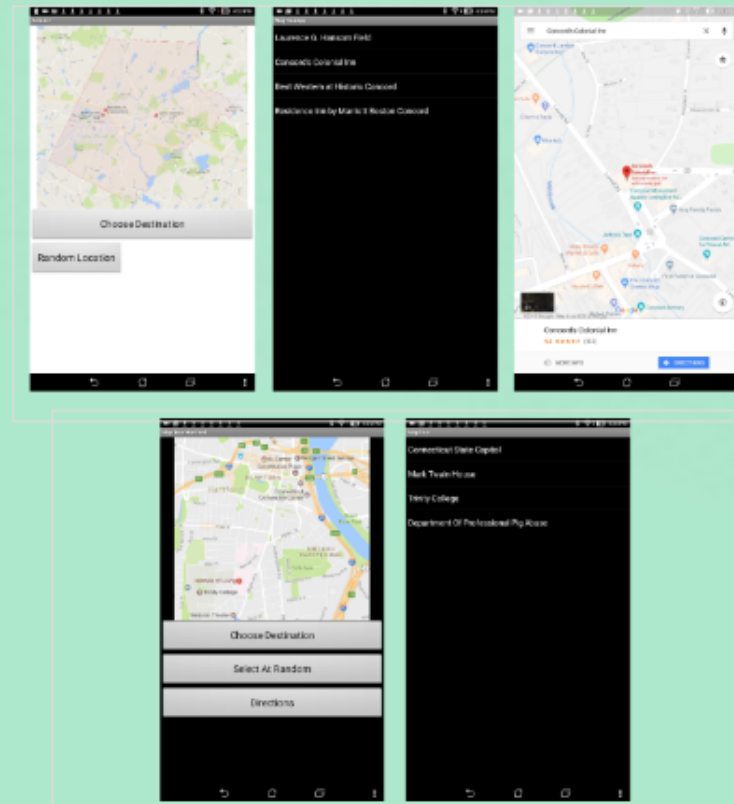


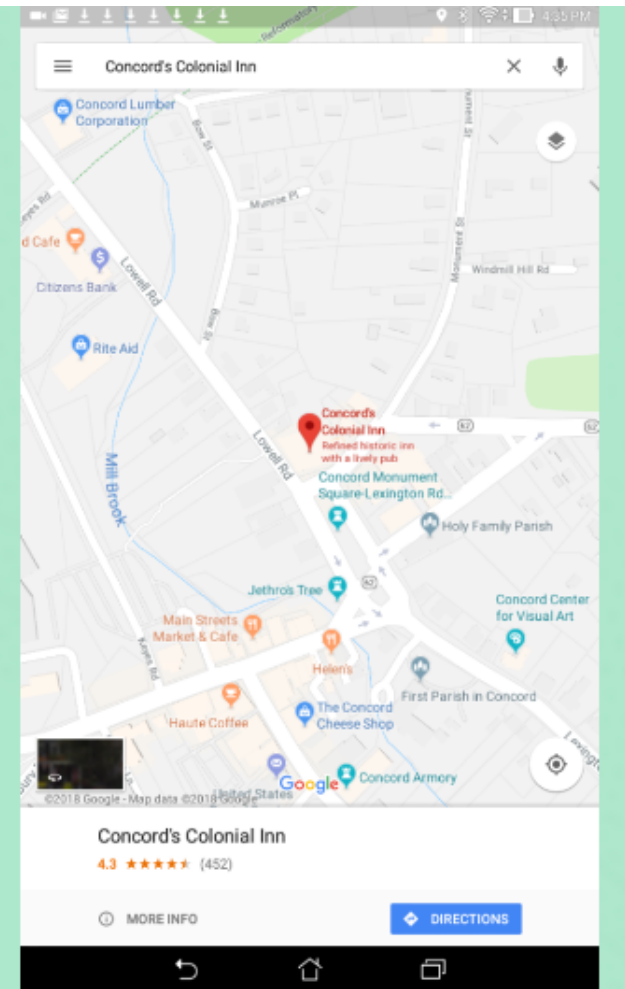
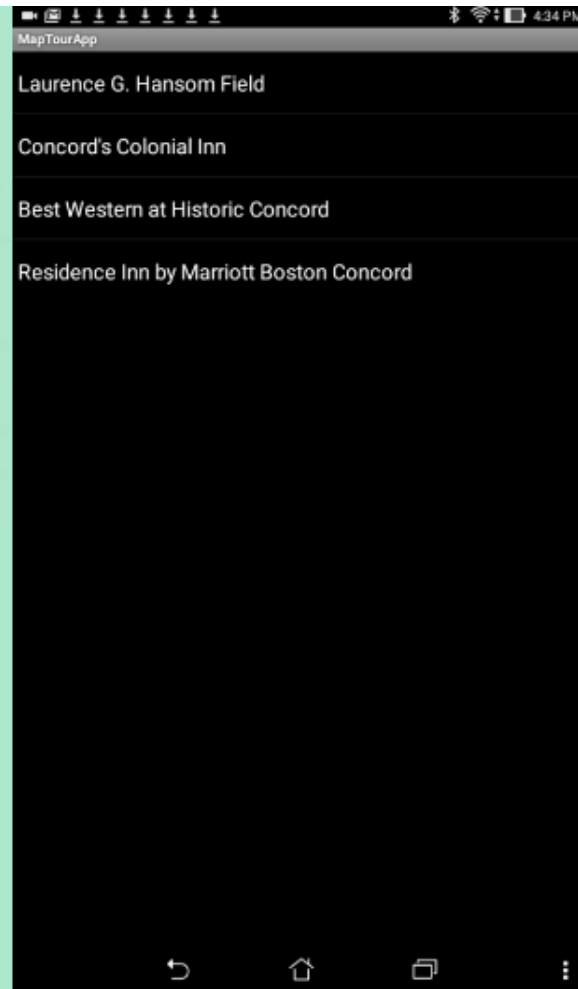
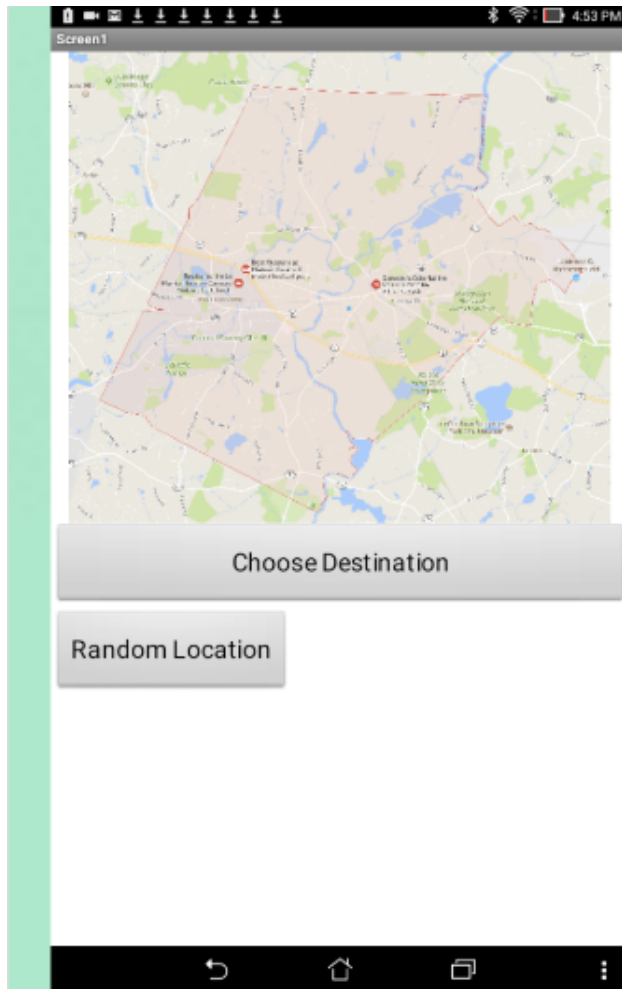


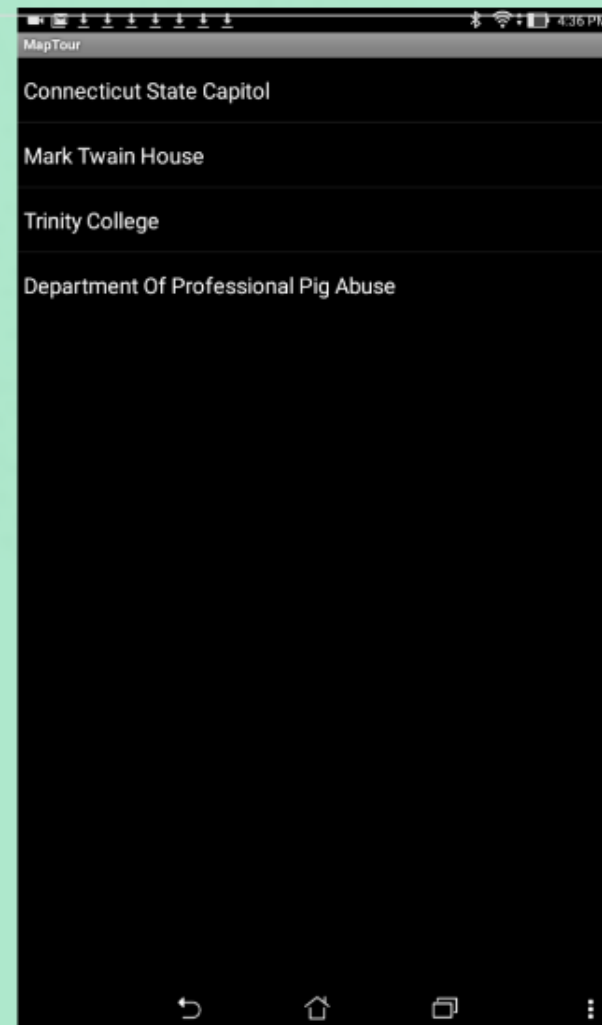
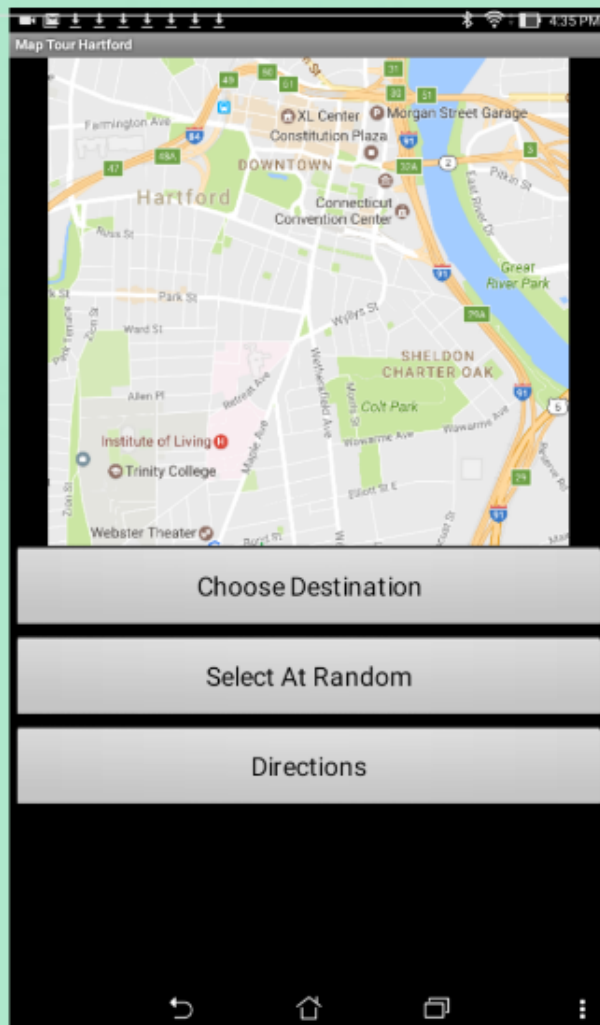




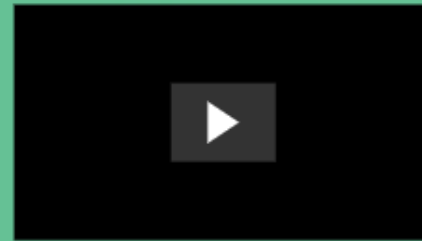
Map Tours







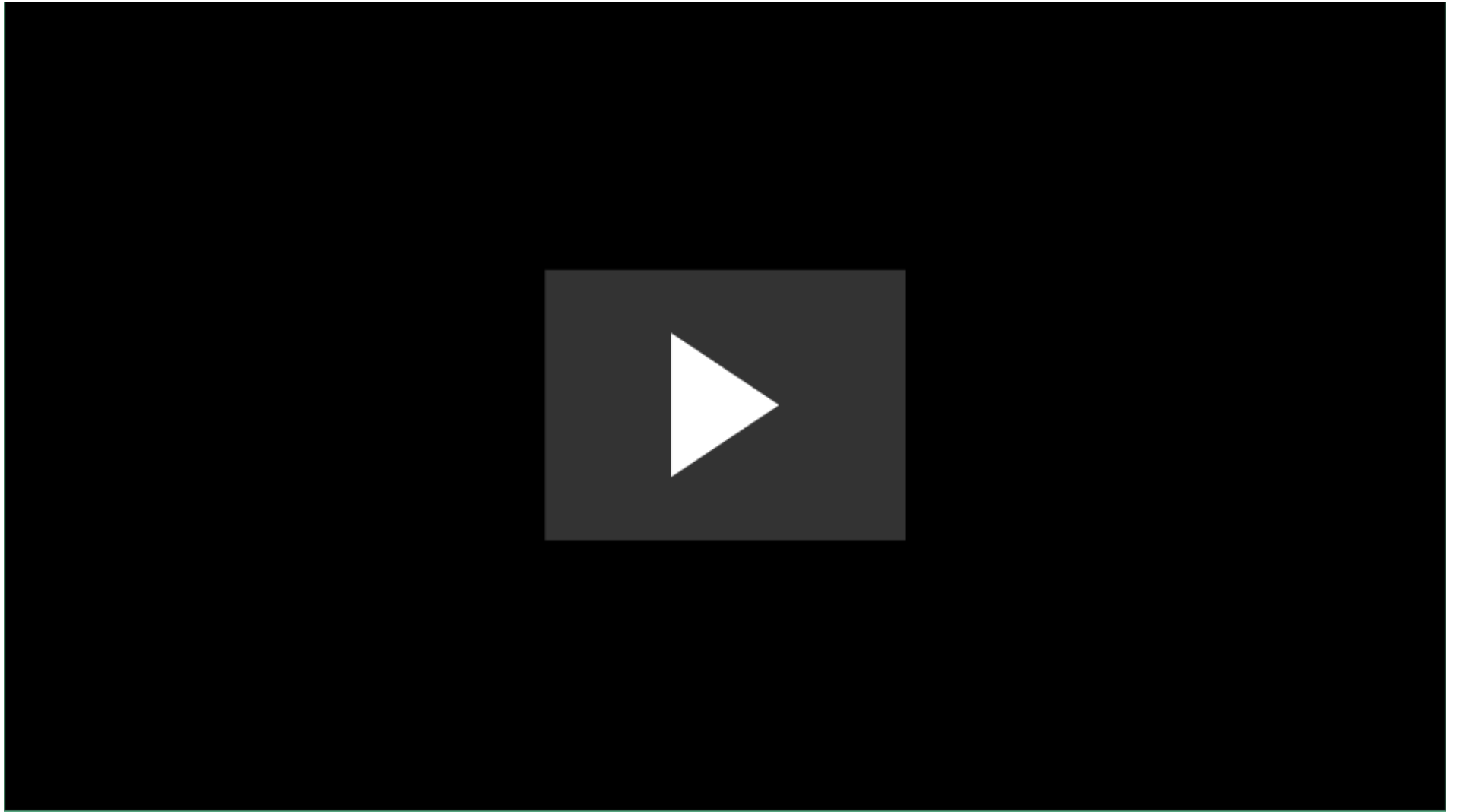
"Lights Out"

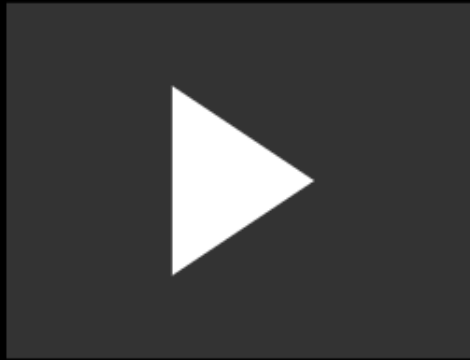


Turn Off The Lights

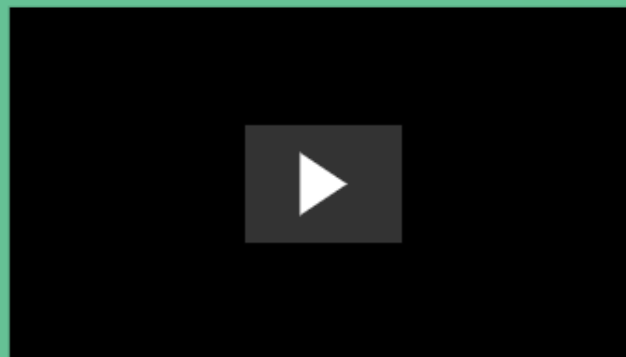
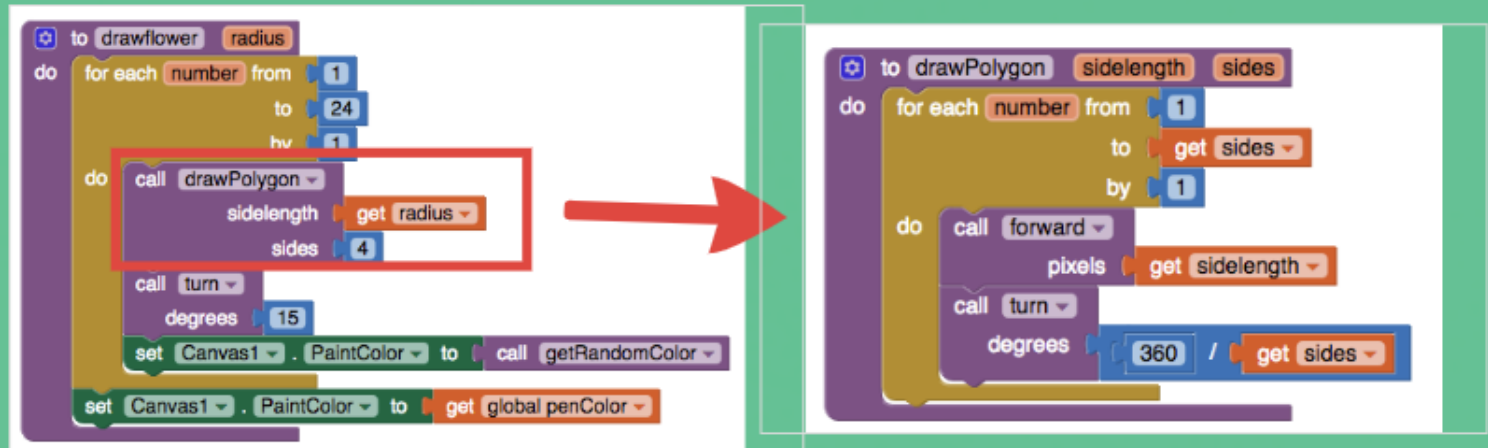


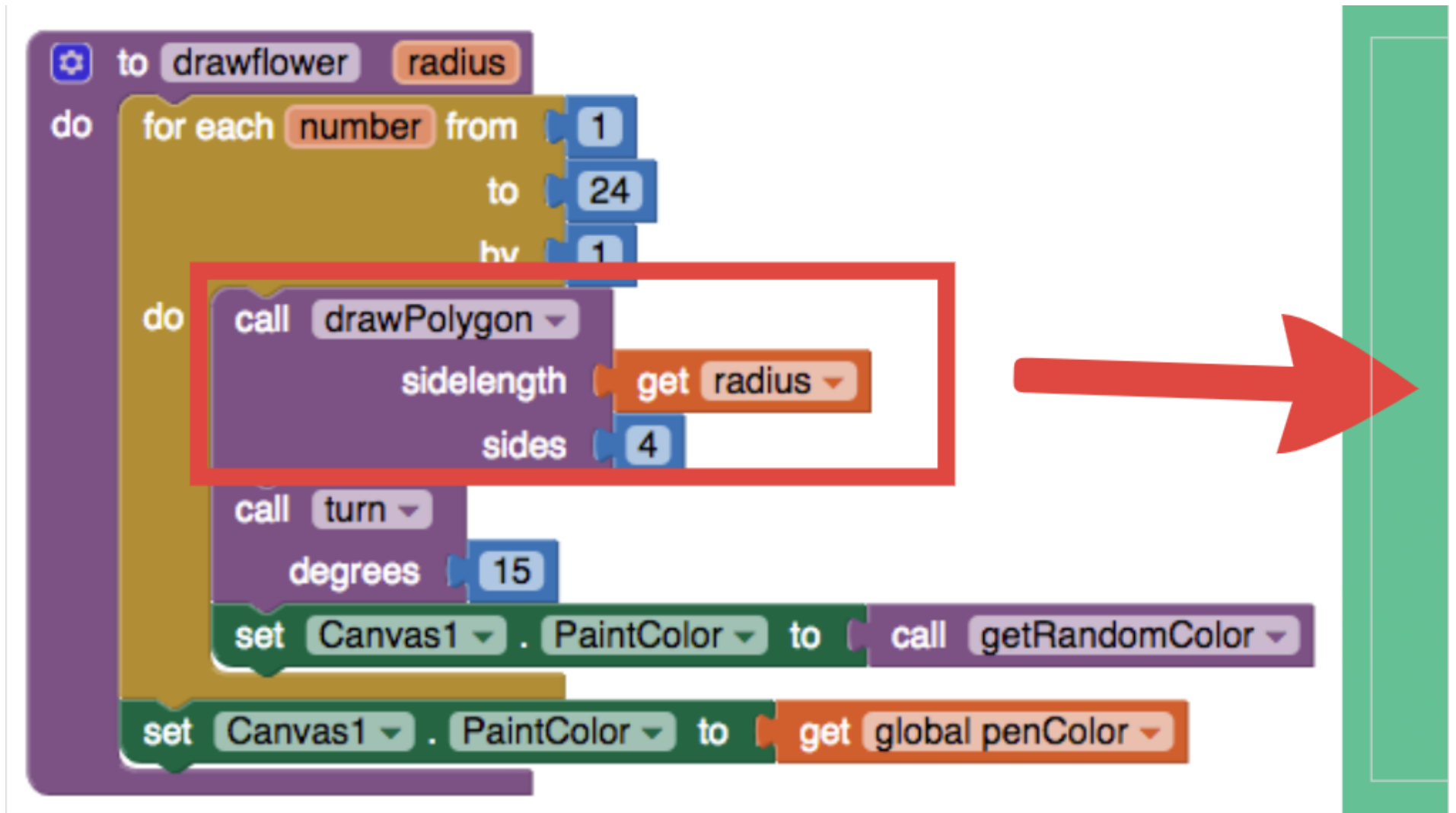
Turn off the lights!

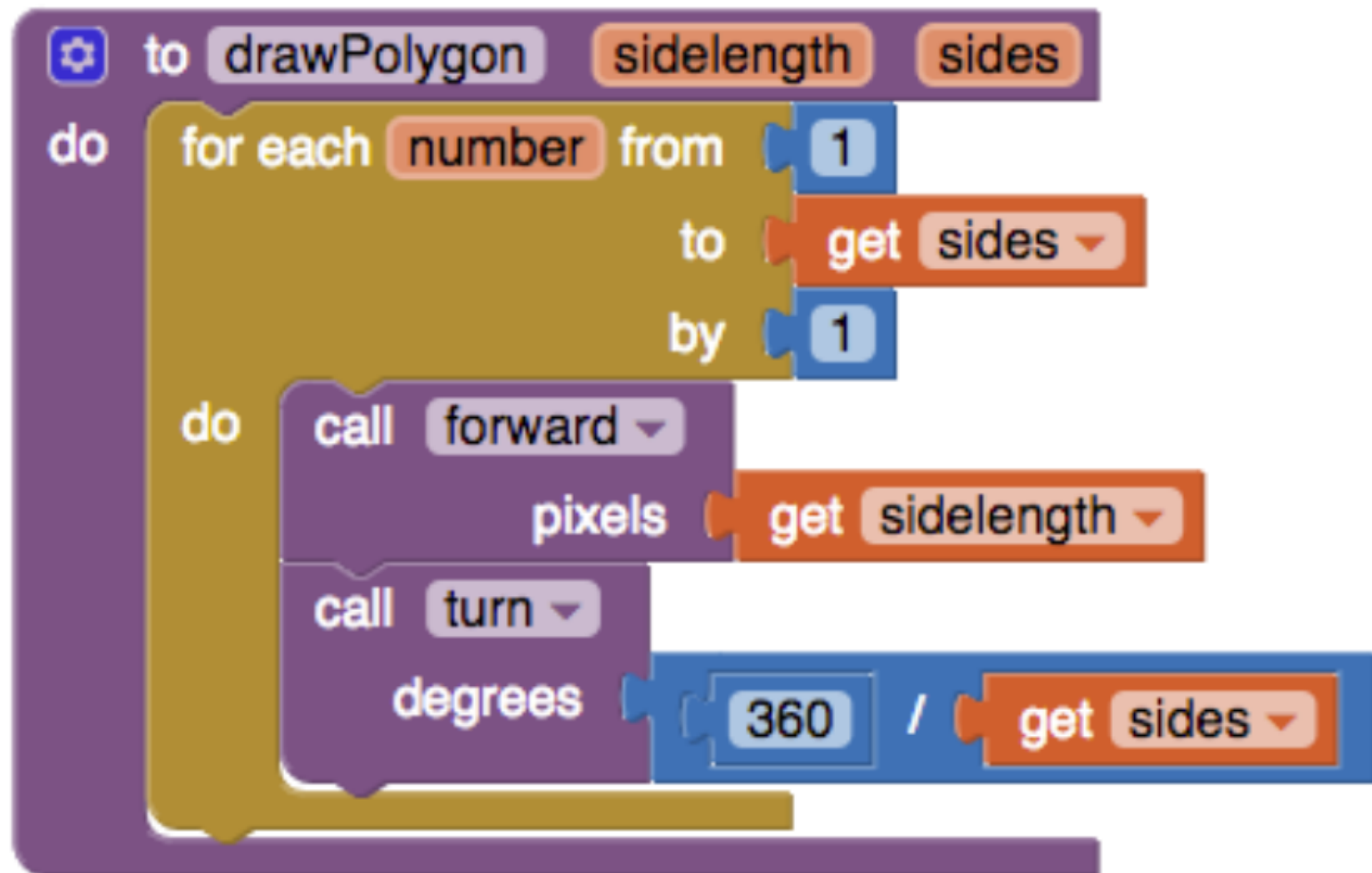


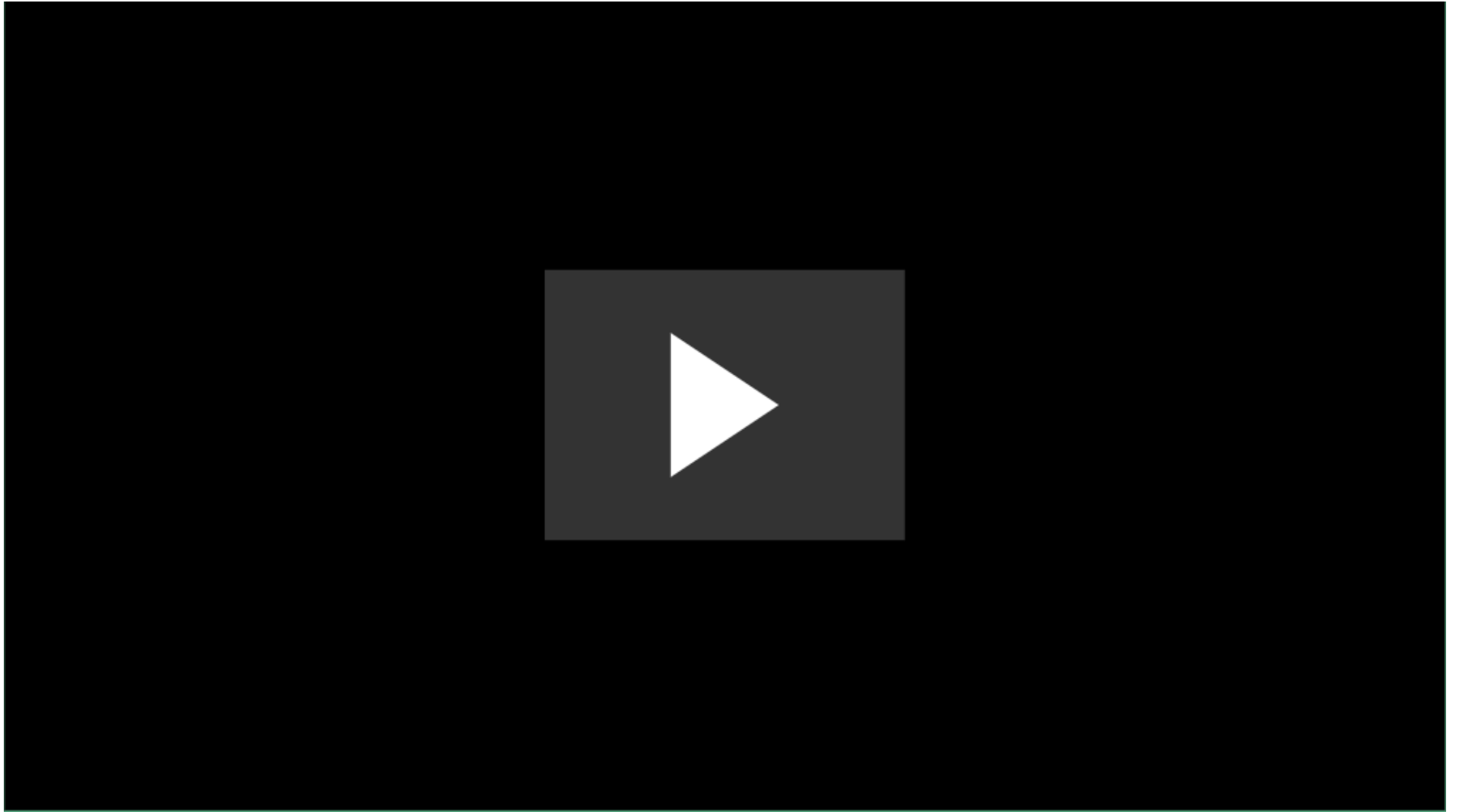


Logo Simulator



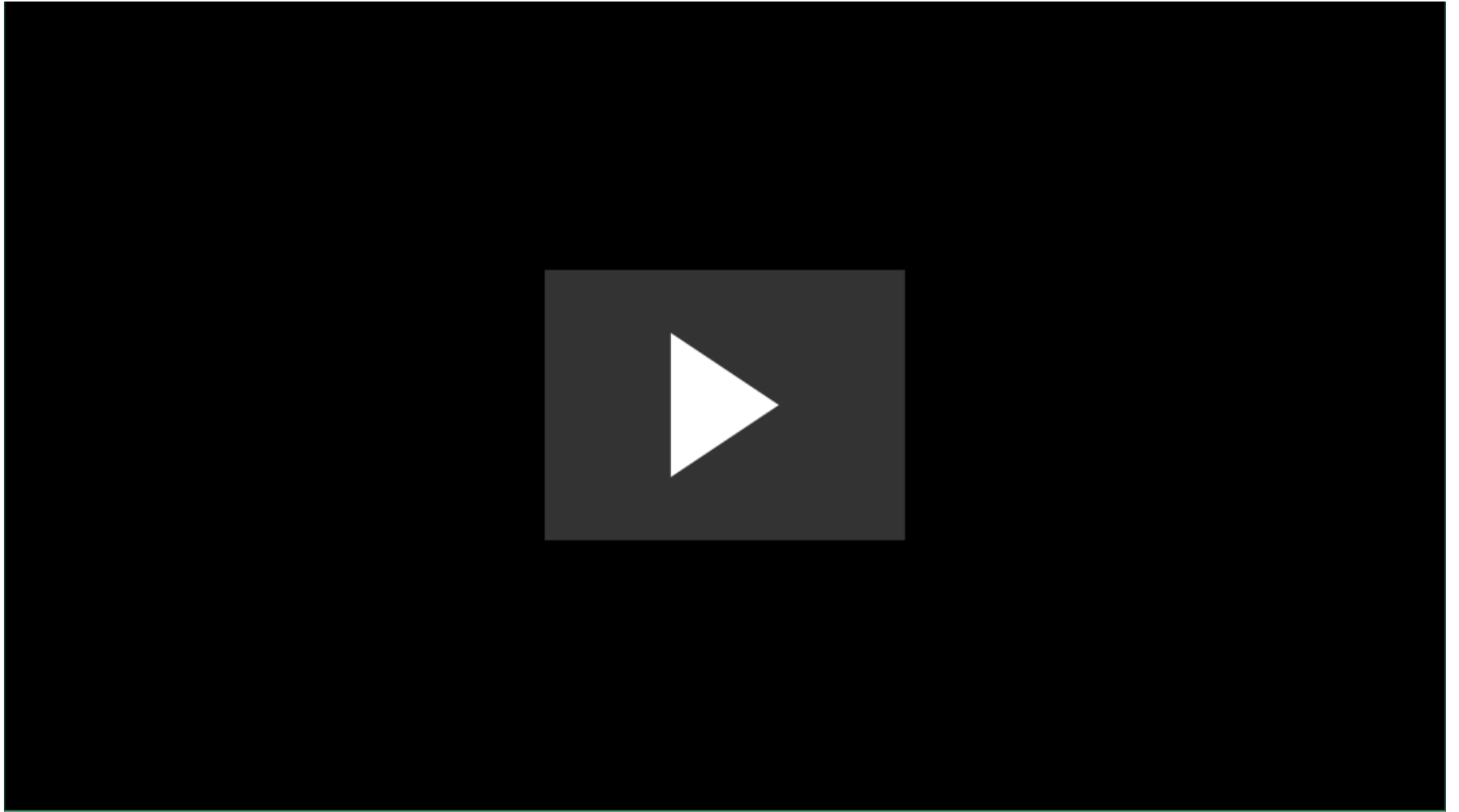


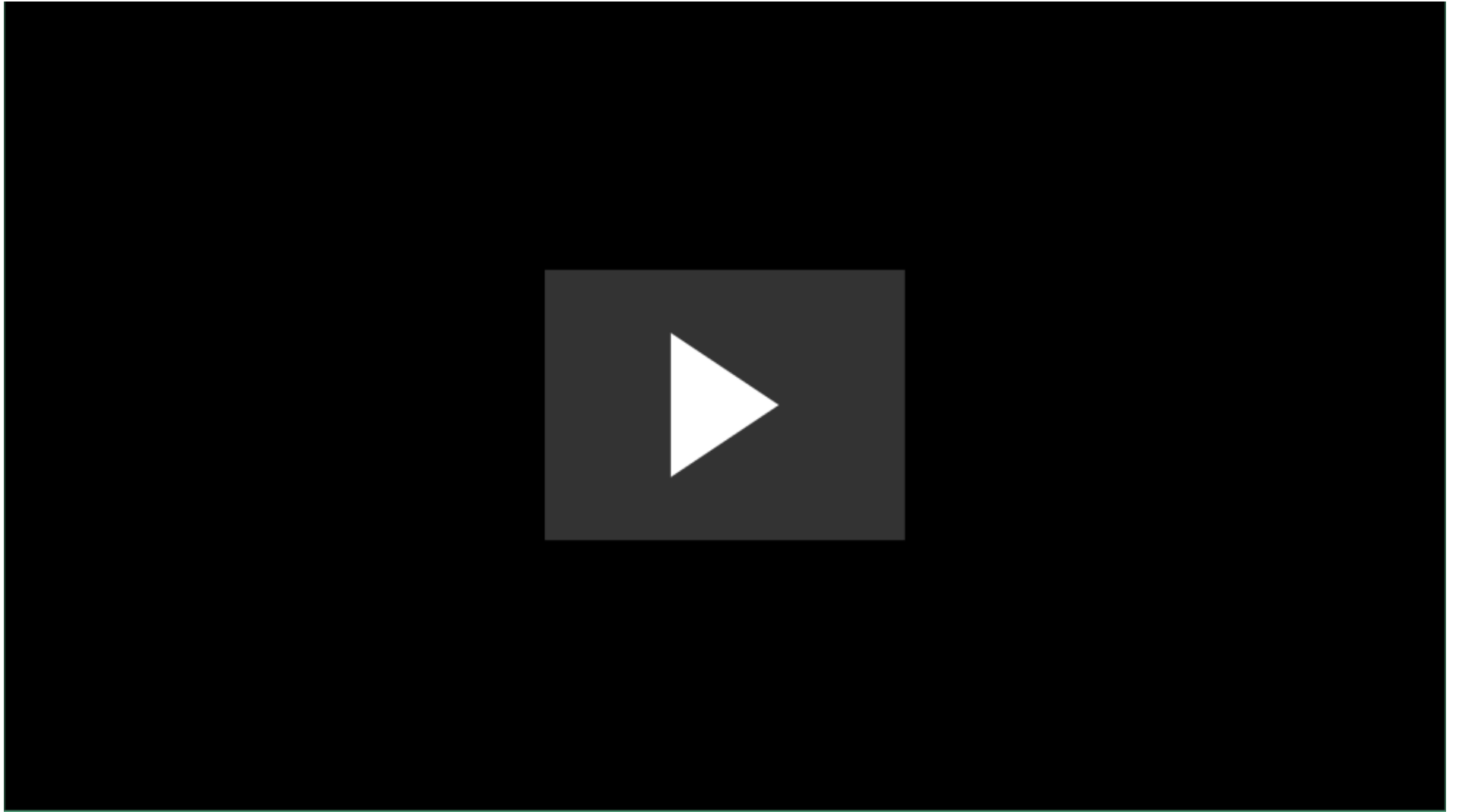




Quiz Games

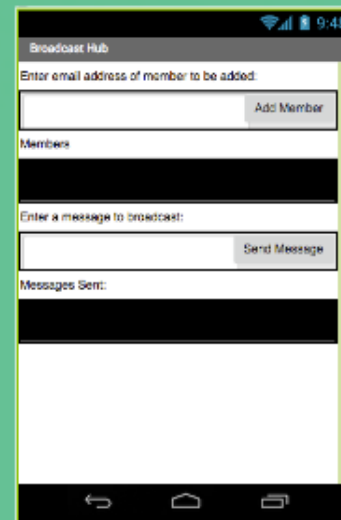
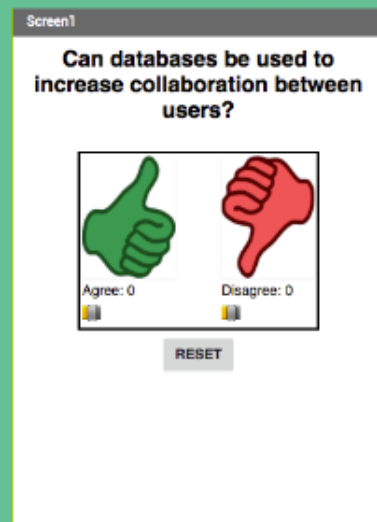






Using Databases

- Clickers with App Inventor's database (TinyWebDB) and Google's Firebase
- E-mail or text Broadcasting Hub

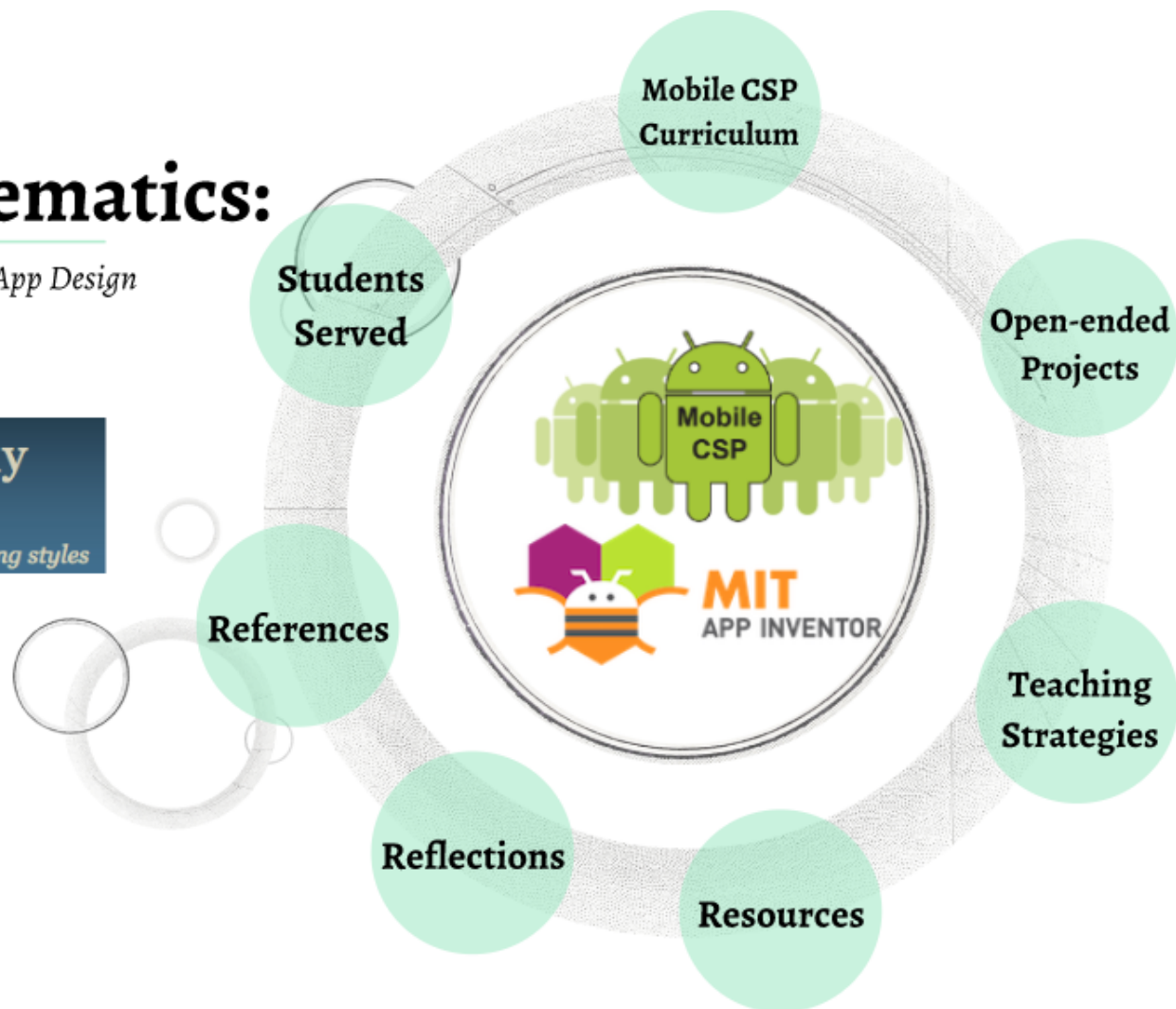


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Student-led Projects

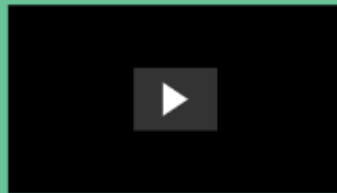
**Open-ended
Projects**

**Apps to Fill
a Need**

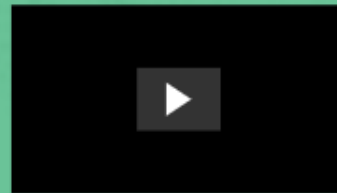
Context-Inspired Apps

Authentic project-based learning

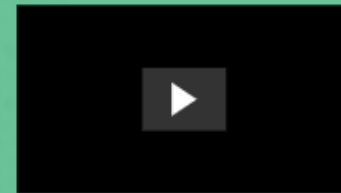
Nautilus Game



Nautilus Tour



**Battle of Groton
Heights Book**

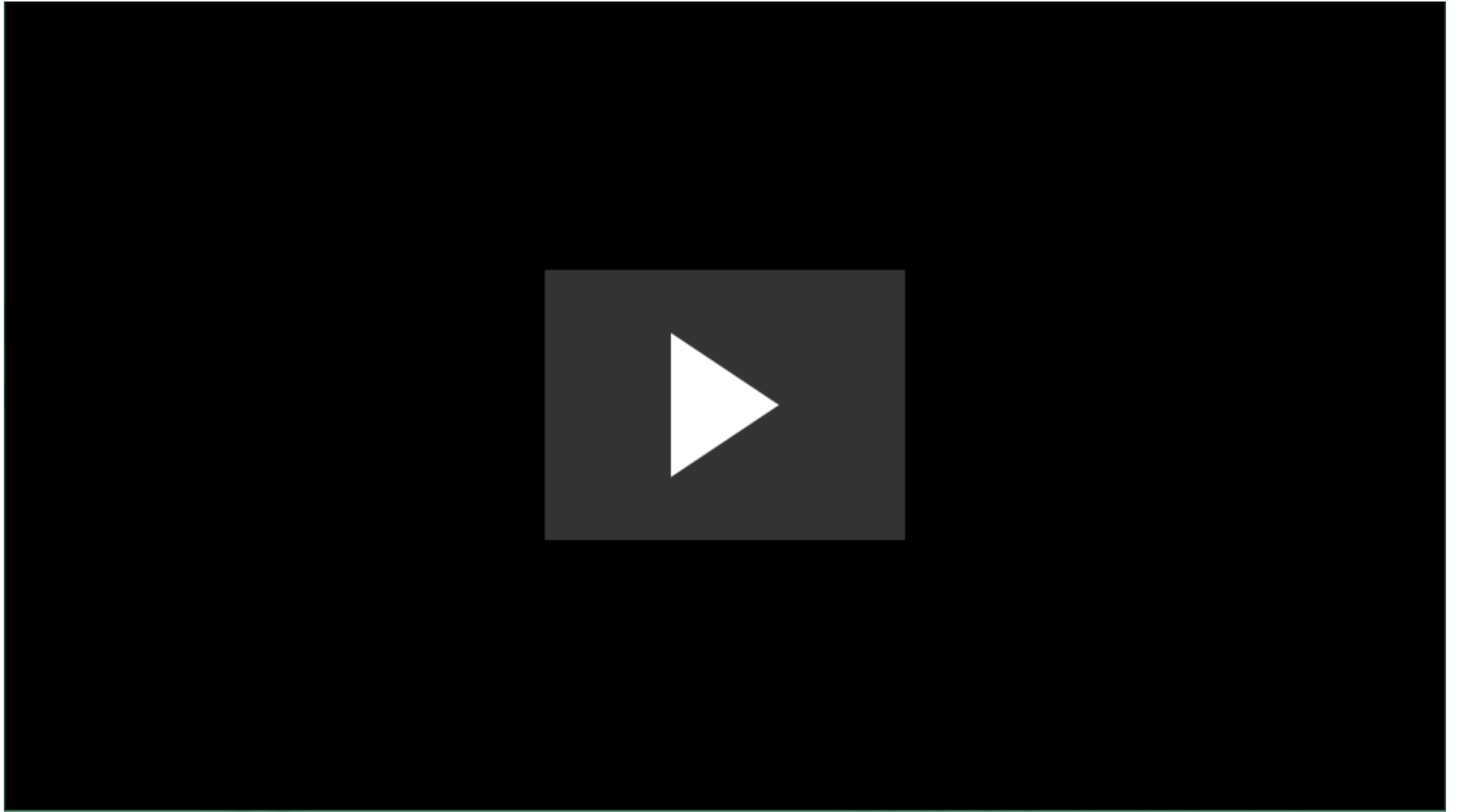


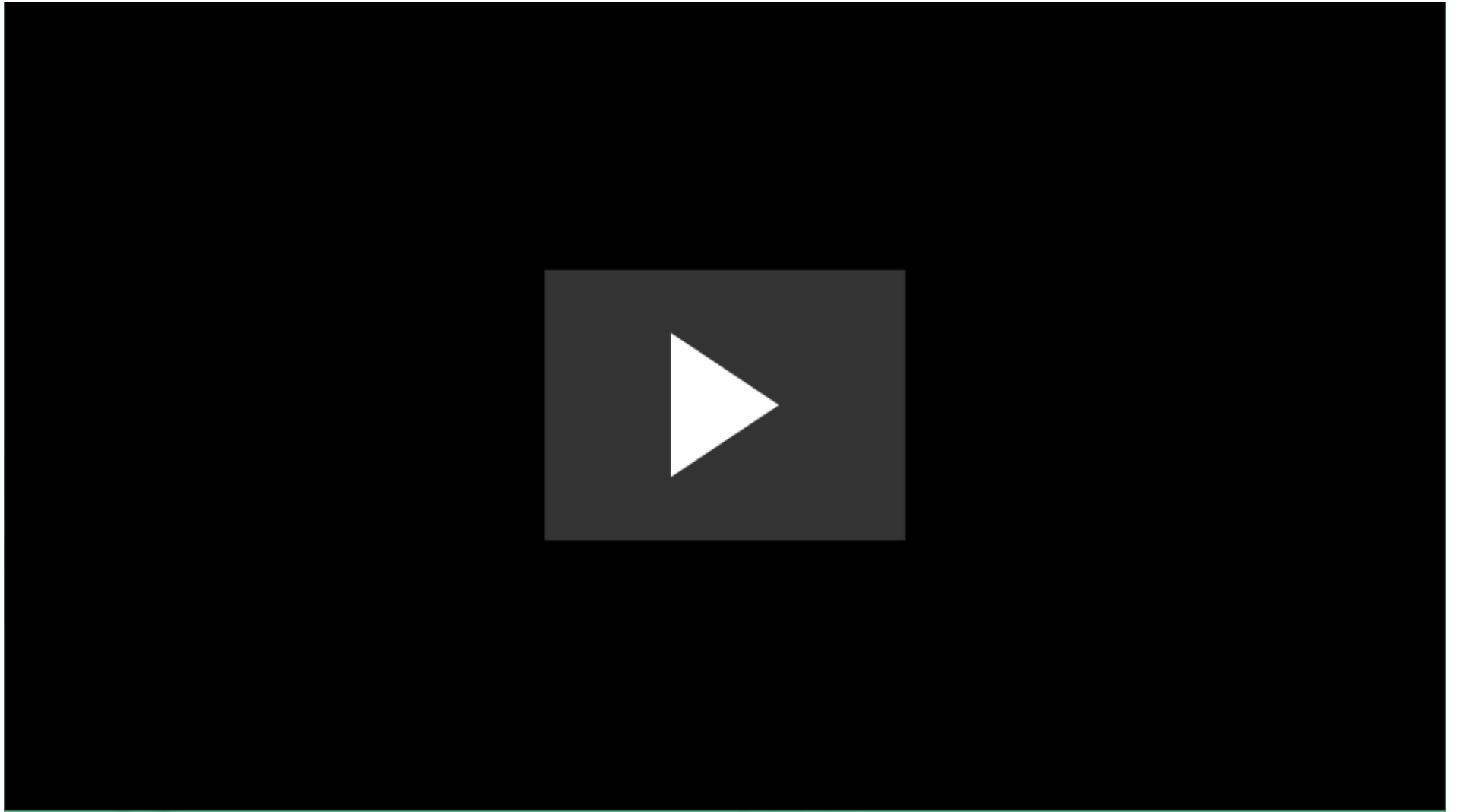
Narratio Chat

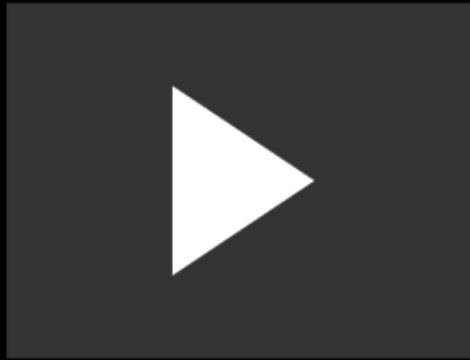


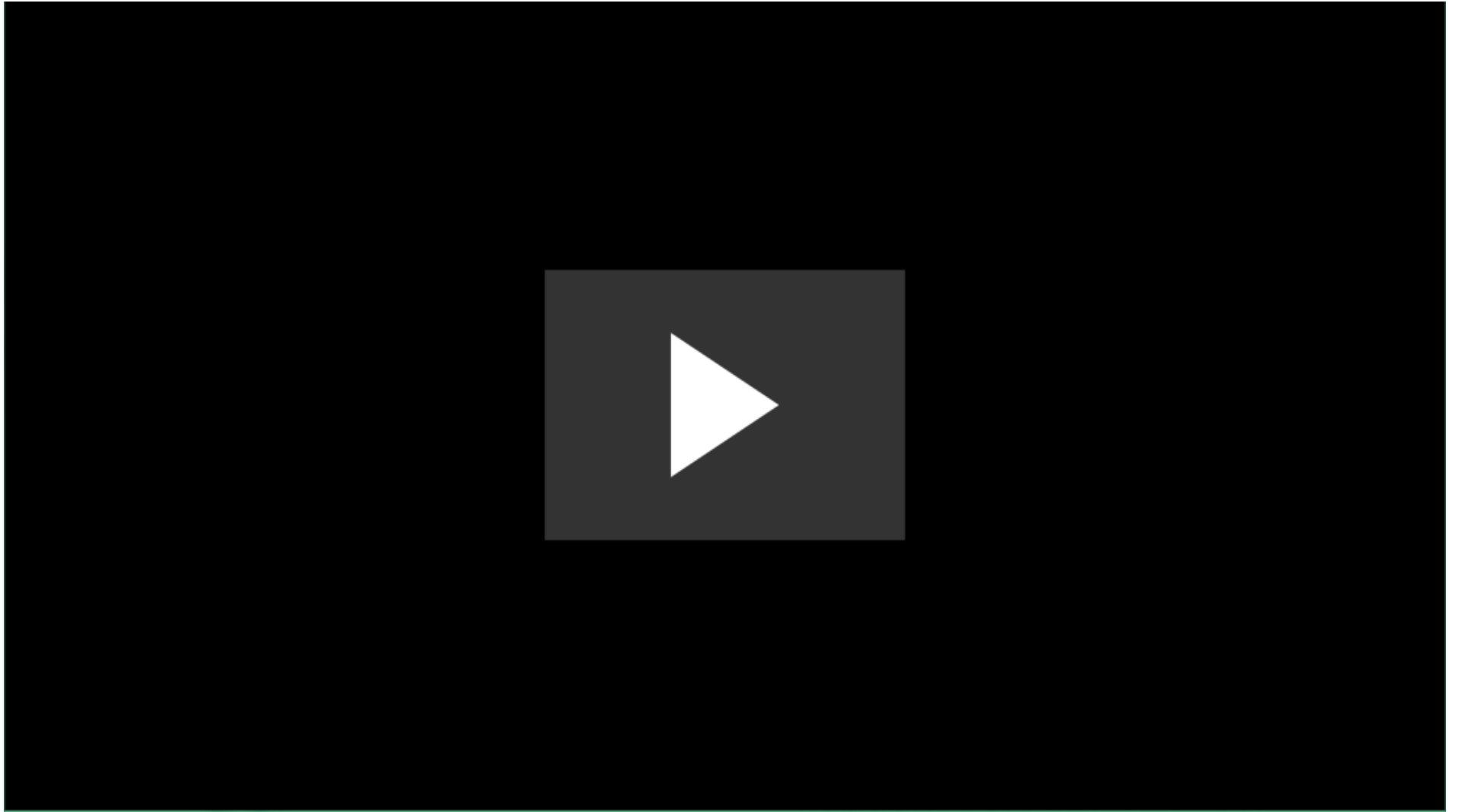
Montage Initiative Education

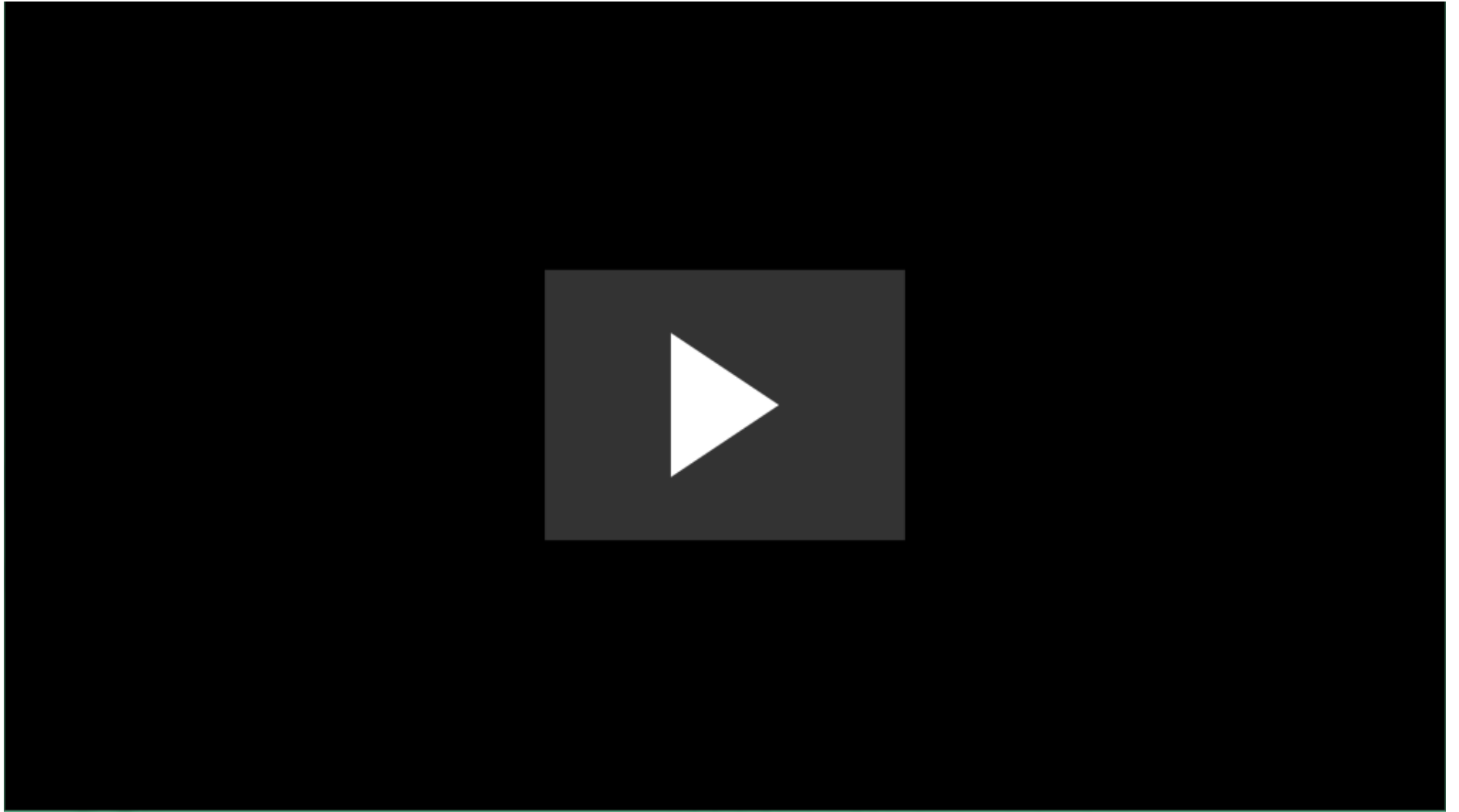






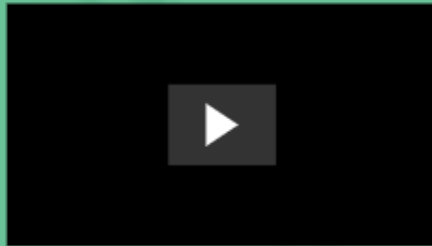






100% Open-Ended

Abstract Art Generator

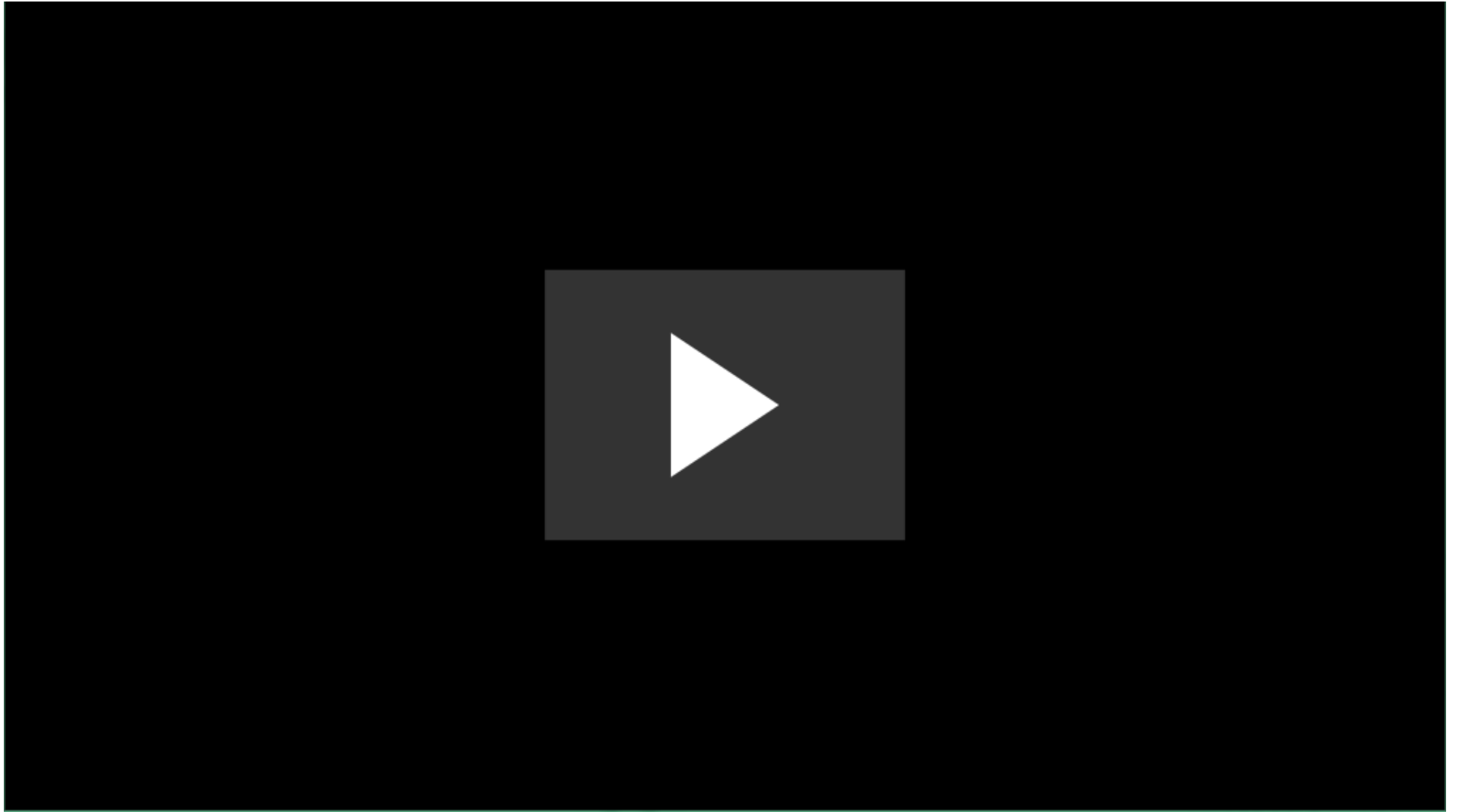


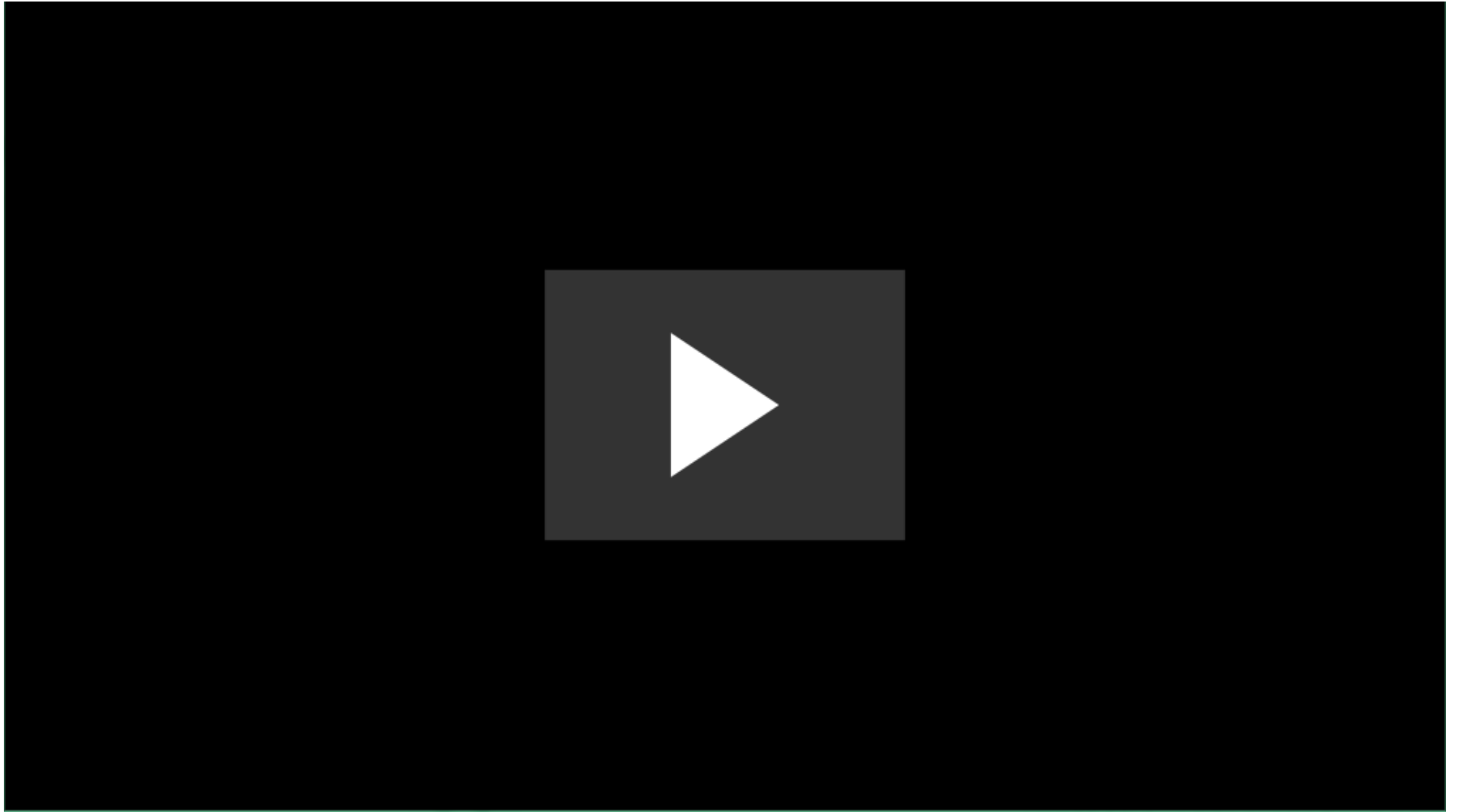
War Game Set Up

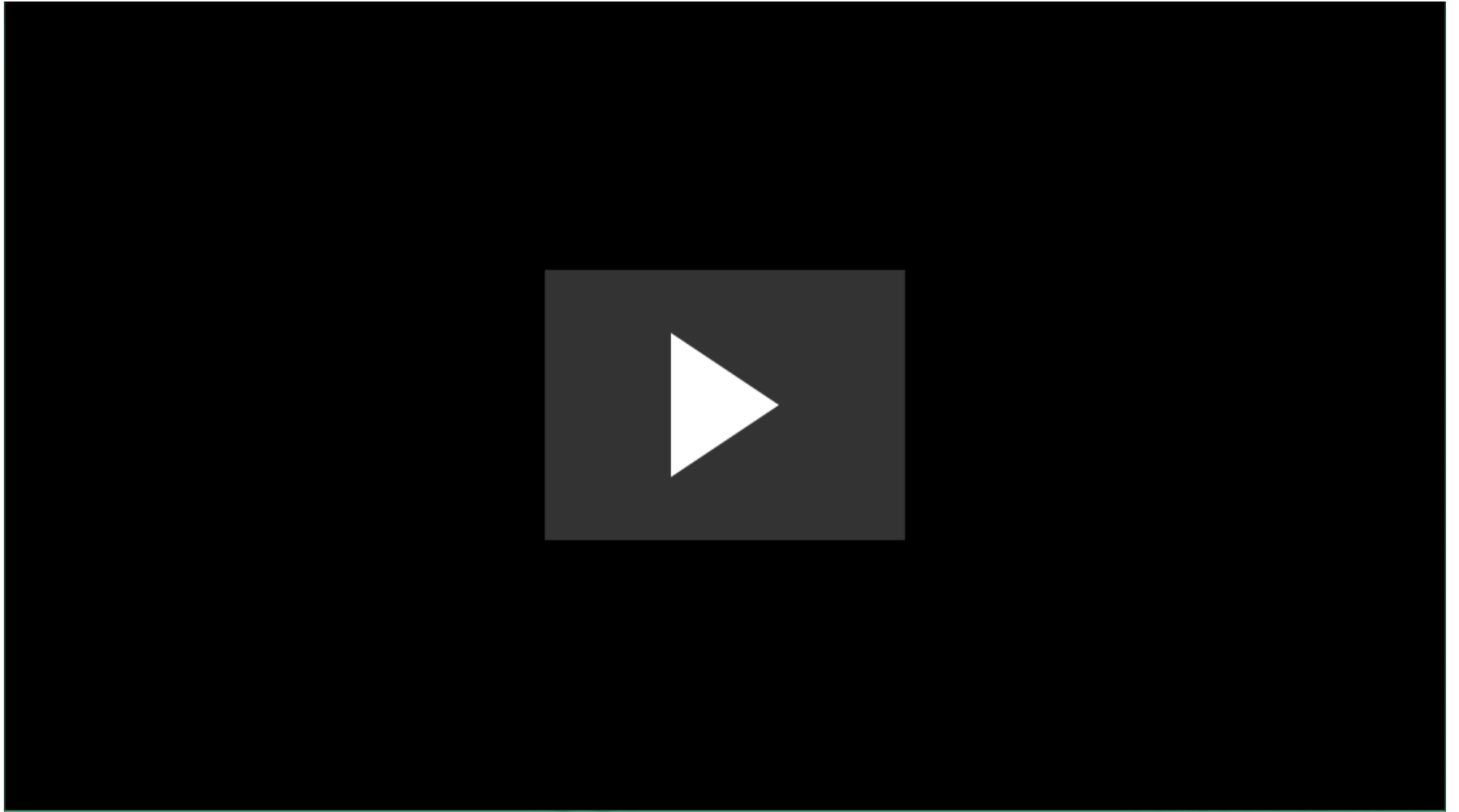


Sorting Algorithms Demo







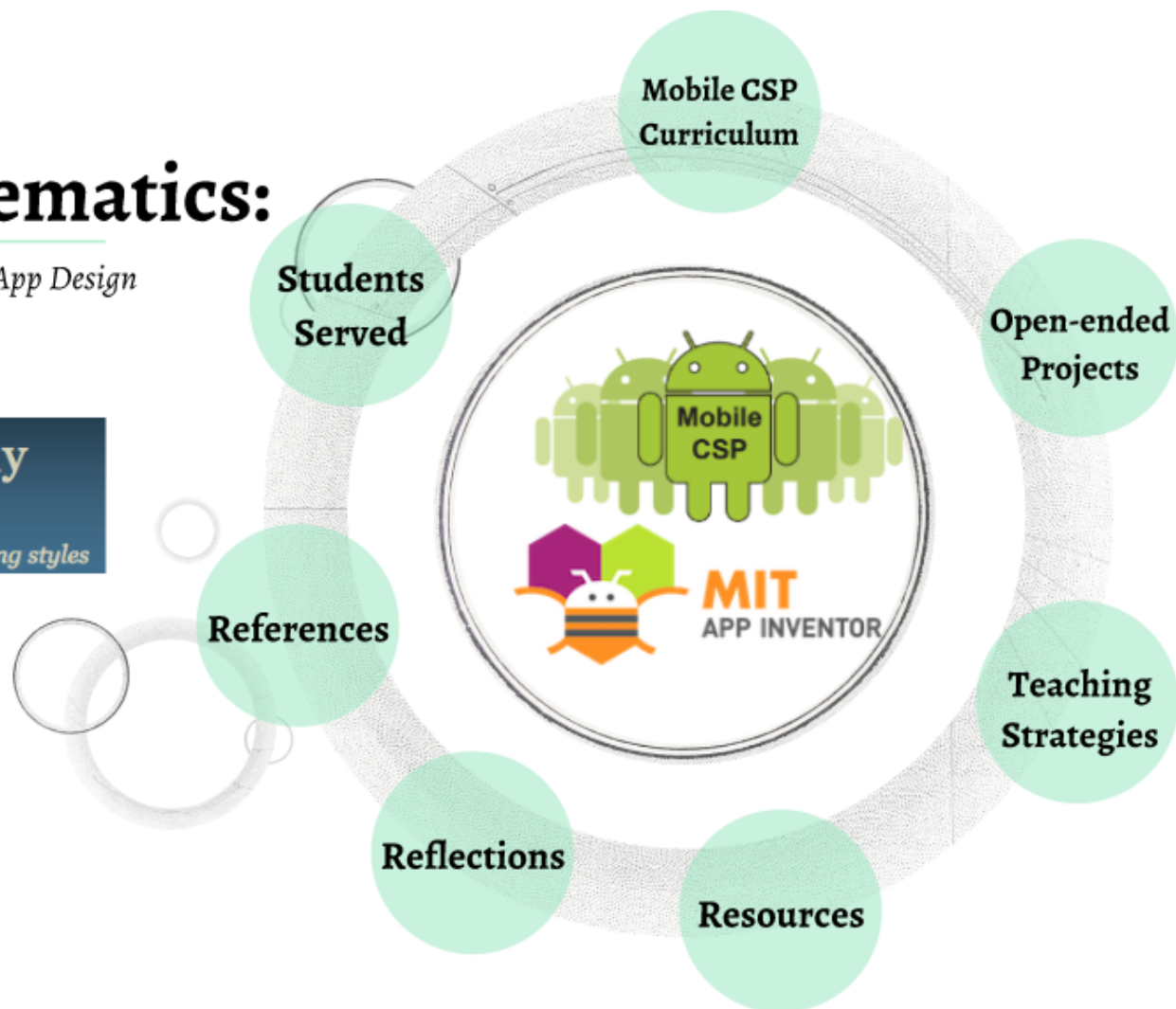


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Teaching Strategies for Computer Science

Adapted from Neil C.C. Brown & Greg Wilson

**Pair
Programming**


Live Coding

Debugging

**Peer
Instruction**

Peer Instruction

- 1.) Give a mini-lesson or brief overview of concepts
- 2.) Pose a multiple choice question that 40-60% of students are likely to get right
- 3.) Students vote individually
- 4.) Students discuss in small groups
- 5.) Reconvene and vote again
- 6.) Respond as needed (move on or clarify)

 **Self-Check** [Hide Answers](#)

For which of the problems would the *bubble sort* algorithm provide an appropriate solution. Choose all that apply.

- ☒ Arranging a deck of cards from the lowest to the highest value cards.
- ☐ Looking up a name in the phone book.
- ☒ Sorting a stack of paper money into denominations – i.e., \$1, \$5, \$10 etc.
- ☐ Sorting a basket of laundry into socks, shirts, shorts, and sheets.
- ☒ Arranging books on a bookshelf by author's last name.

Check Answer

Debugging

- Predicting outcome (solve on paper)
- Fixing provided mistakes
- Using students' natural mistakes as learning opportunities
 - Creating a climate that anticipates and encourages regular reflection and improvement

Live Coding

- I do/ we do method
- Stresses the problem solving process
 - Breaking into smaller parts
 - Testing code
- Have some parts already done!

Pair Programming

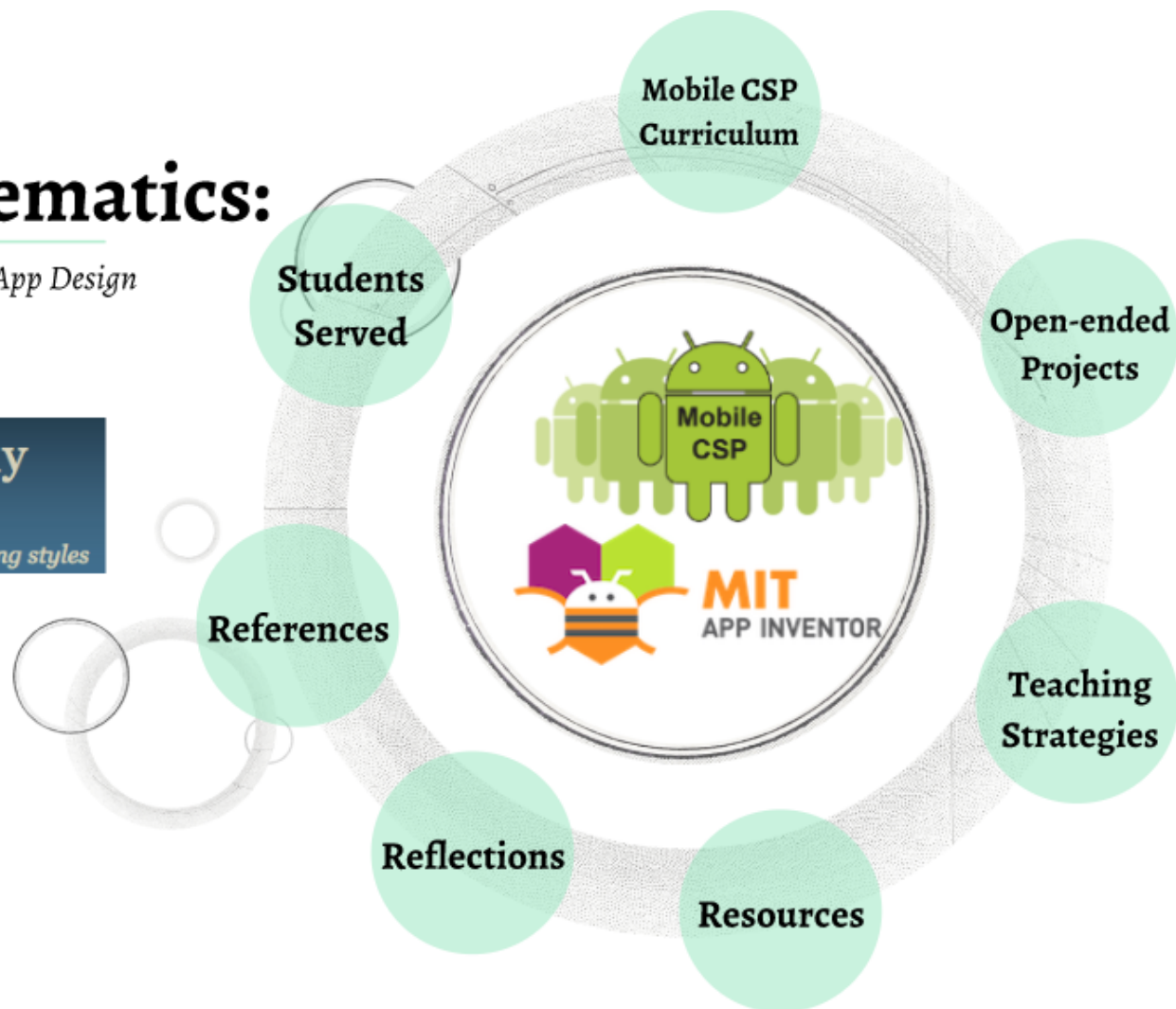
- One "driver"
- One "navigator"
 - This person can also research and interpret documentation
- Switch places frequently

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Resources

- Infy.com/Pathfinders

Take the course yourself over the summer!

Free curriculum:

- Mobile CSP -- nice videos, should create your own questions
- Code.org -- works with iPhone,
has <https://code.org/curriculum/algebra>
- Beauty and Joy of Computing - all text-based, Snap! (not apps)
<https://csforallteachers.org/group/bjcile>
- CS50 AP-- most rigorous

**Using App
Inventor**

App Inventor Requirements

- A Google account (one account/file)
- Can run emulator on PC or OSX 10.12 or before (not High Sierra)
 - Otherwise use BlueStacks emulator
- Android device or tablet (~\$100) that can use same wifi connection as computer
- iOS version "coming soon"



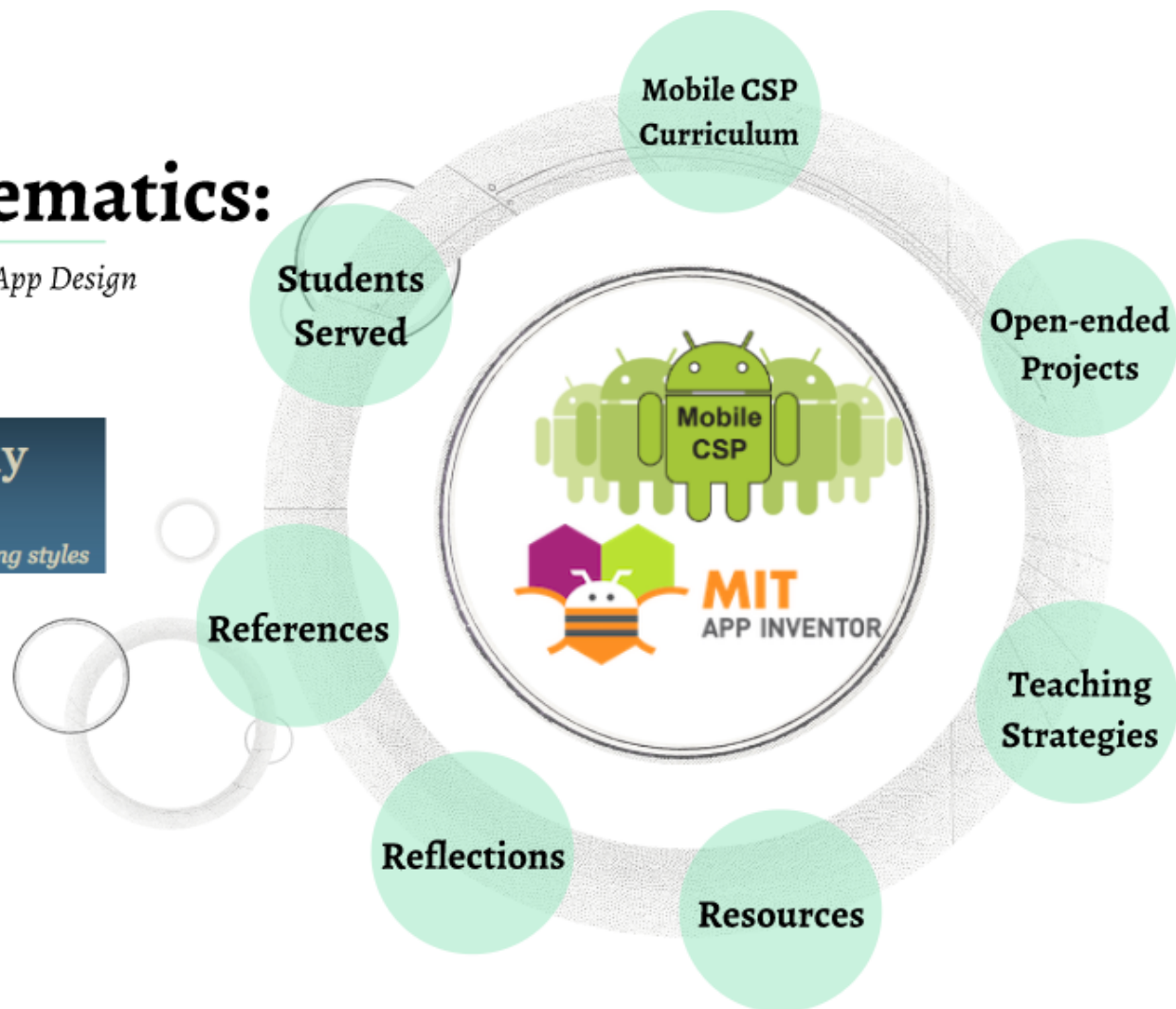
[http://www.appinventor.org/
book2](http://www.appinventor.org/book2)

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Reflections

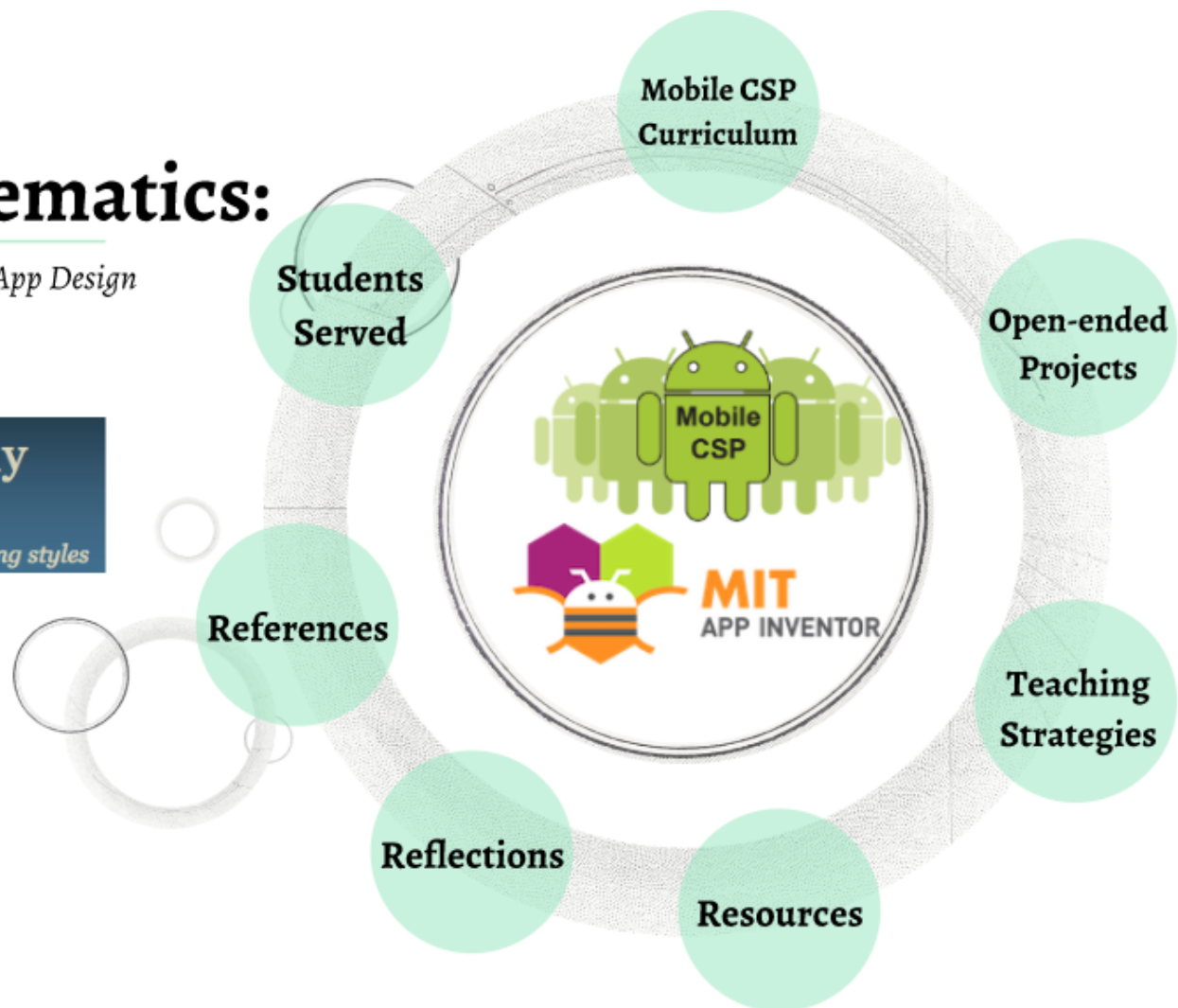
- AP?
 - Best for younger students
 - Lots of writing, little programming
- Don't use website/portfolio question format
- Multiple choice -> class discussion exercises
 - Pre-make some of the step-by-step apps
OR live code as a class
- Prepare for tech setbacks!

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References

Brown Neil C.C., Wilson Greg. "Ten quick tips for teaching programming." PLoS Computational Biology. 14(4). Published April 5, 2018. <https://doi.org/10.1371/journal.pcbi.1006023>

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