

Let's Start with a Problem!

Grades 3-5

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Problem Situations

	Verbal	Static	Dynamic	Symbolic
Application (Modeling)				
Math Structures				
Games				
Math Representations				

One Fish, Two Fish

3 Guppies



\$186

5 zebrafish



\$325



Are guppies or zebra fish cheaper?

Possible Solutions

Two Divisions

$$\begin{array}{r} \$62 \\ 3 \overline{) 186} \\ \hline \end{array} \quad \begin{array}{l} 1 \text{ guppy} \\ \uparrow \\ \text{cheaper} \end{array}$$
$$\begin{array}{r} \$65 \\ 5 \overline{) 325} \\ \underline{300} \\ 25 \\ \underline{25} \\ 0 \end{array} \quad \begin{array}{l} 1 \text{ zebrafish} \end{array}$$

Divide & Multiply

$$\$186 \div 3 = \$62 \text{ for } 1 \text{ guppy}$$

$$5 \times 62 = 300 + 10 = \$310 \text{ for } 5$$

Guppies are cheaper

Use Number Sense

Both about \$60.

Guppies \$6 over for 3 - so cost \$62

Zebras \$25 over for 5 - so cost \$65

Guppies cheaper

Aunt Martha's Cupcakes

- ▶ Aunt Martha has 5 trays of cupcakes.
- ▶ There are 100 total cupcakes on the trays.
- ▶ The first and second trays have 52 cupcakes.
- ▶ The second and third trays have 43 cupcakes.
- ▶ The third and fourth trays have 34 cupcakes.
- ▶ The fourth and fifth trays have 30 cupcakes.
- ▶ How many cupcakes are on each tray?



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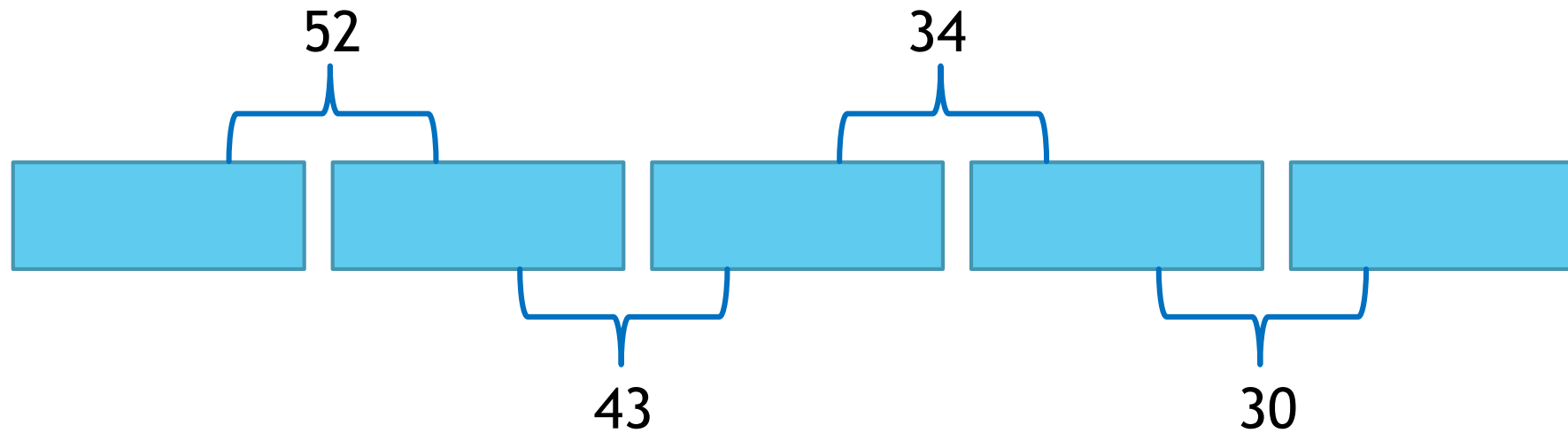
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Can a picture help?

100 in all



Possible Scaffolding

- ▶ To help students get started
- ▶ To help students who are stuck
- ▶ To help students going down a wrong path
- ▶ To help students clarify thinking

Array-bow of Colors

- ▶ Act 1: Watch the video



Problems without Words

What's Gone Wrong?

$$37 \times 5$$

$$\begin{array}{r} 3 \\ 37 \\ \times 5 \\ \hline 185 \end{array}$$

$$406 \times 4$$

$$\begin{array}{r} 2 \\ 406 \\ \times 4 \\ \hline 1664 \end{array}$$

$$320 \times 6$$

$$\begin{array}{r} 1 \\ 320 \\ \times 6 \\ \hline 1926 \end{array}$$

$$315 \times 8$$

$$\begin{array}{r} 4 \\ 315 \\ \times 8 \\ \hline 2520 \end{array}$$

What's Gone Wrong?

$$\begin{array}{r} 3258 \div 6 \\ 0241 \\ 6 \overline{) 3258} \end{array}$$

$$\begin{array}{r} 84 \div 2 \\ 42 \\ 2 \overline{) 84} \end{array}$$

$$\begin{array}{r} 180 \div 5 \\ 610 \\ 5 \overline{) 180} \end{array}$$

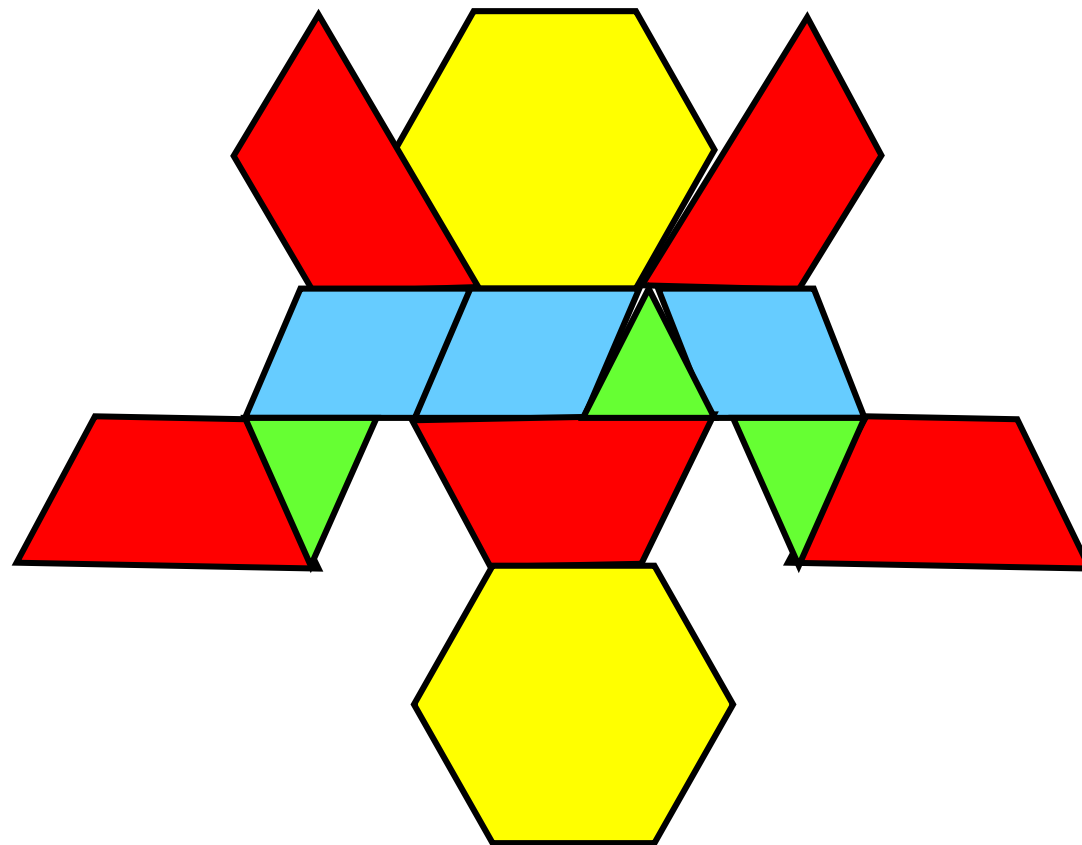
$$\begin{array}{r} 261 \div 3 \\ 450 \\ 3 \overline{) 261} \end{array}$$

The Pencil Task

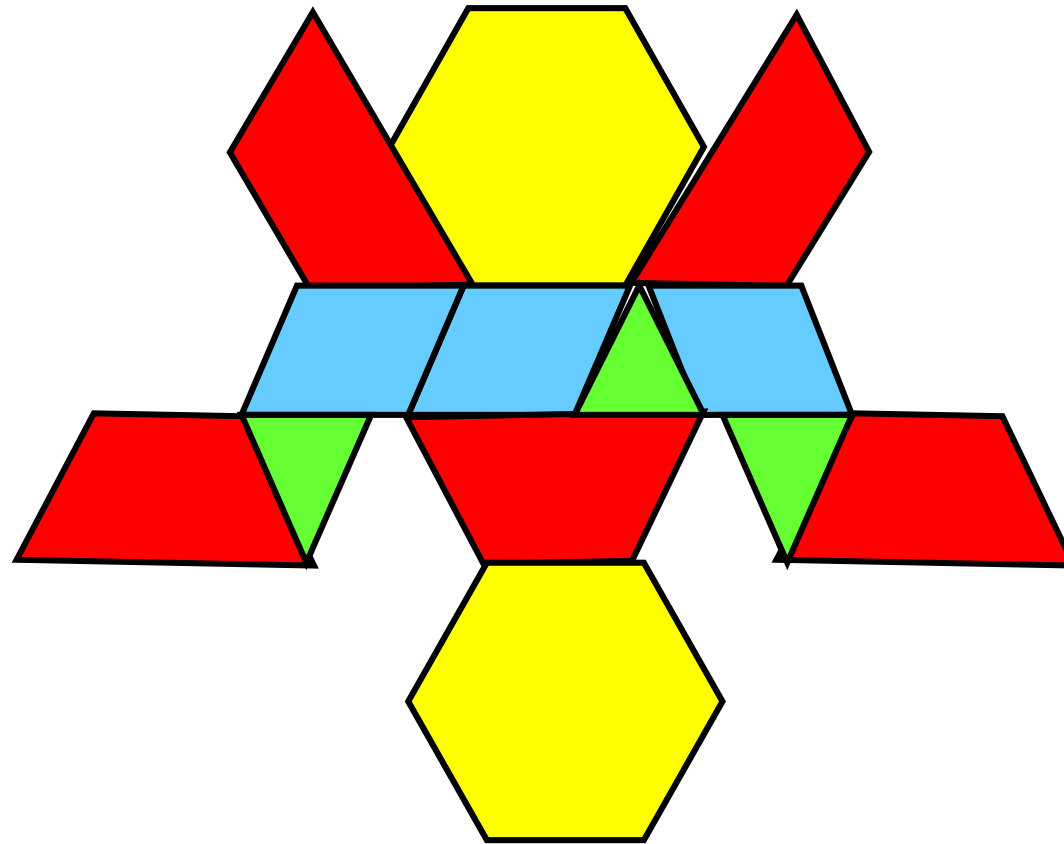


- ▶ Mrs. Washington cleans her classroom on the last day of school and finds some pencils left over from the year. She knows there are 24 pencils in a full box. Mrs. Washington finds $\frac{1}{4}$ of a box in her desk. How many pencils does she find in her desk?
- ▶ Mrs. Washington finds $\frac{3}{4}$ of a box of pencils in the closet of her classroom. How many pencils does she find in the closet?
- ▶ Mrs. Washington finds $1\frac{1}{8}$ boxes of pencils in the lost and found in her classroom. How many pencils does she find in the lost and found?

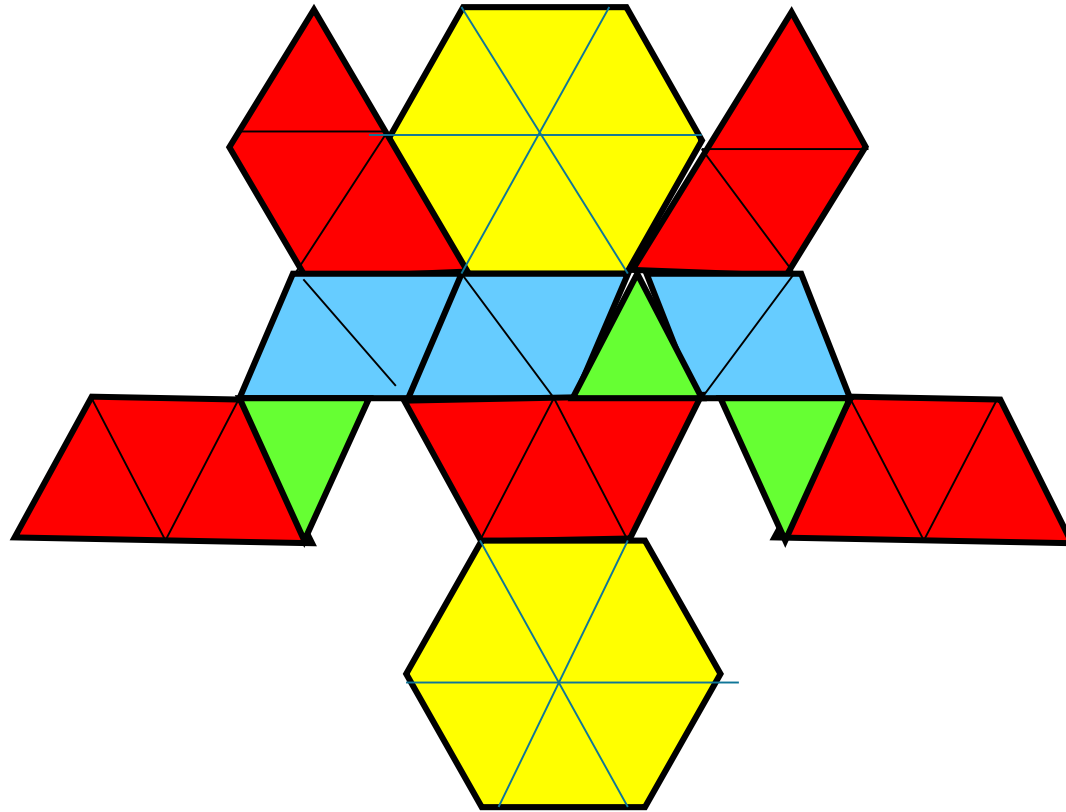
What fraction is blue?



Part of a Set - 3 of 13 pieces

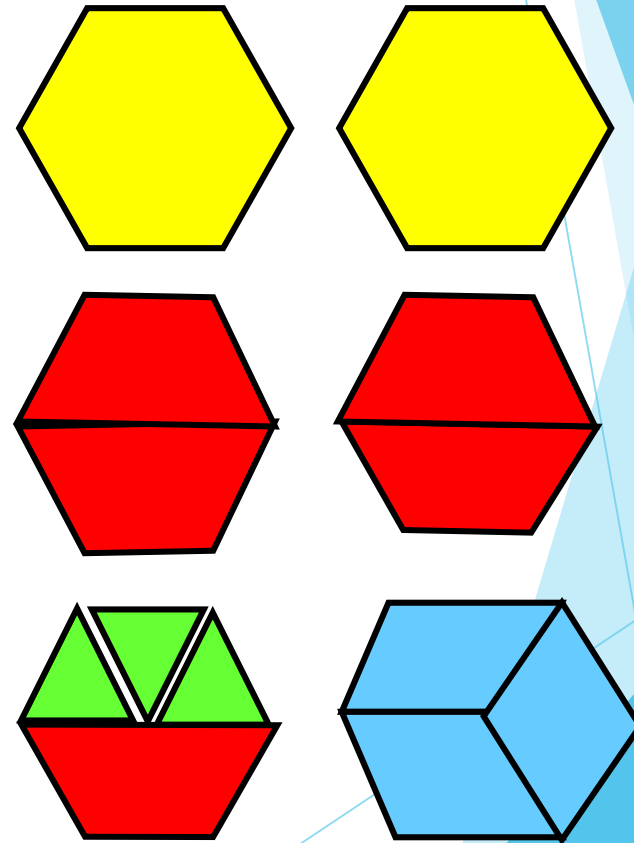
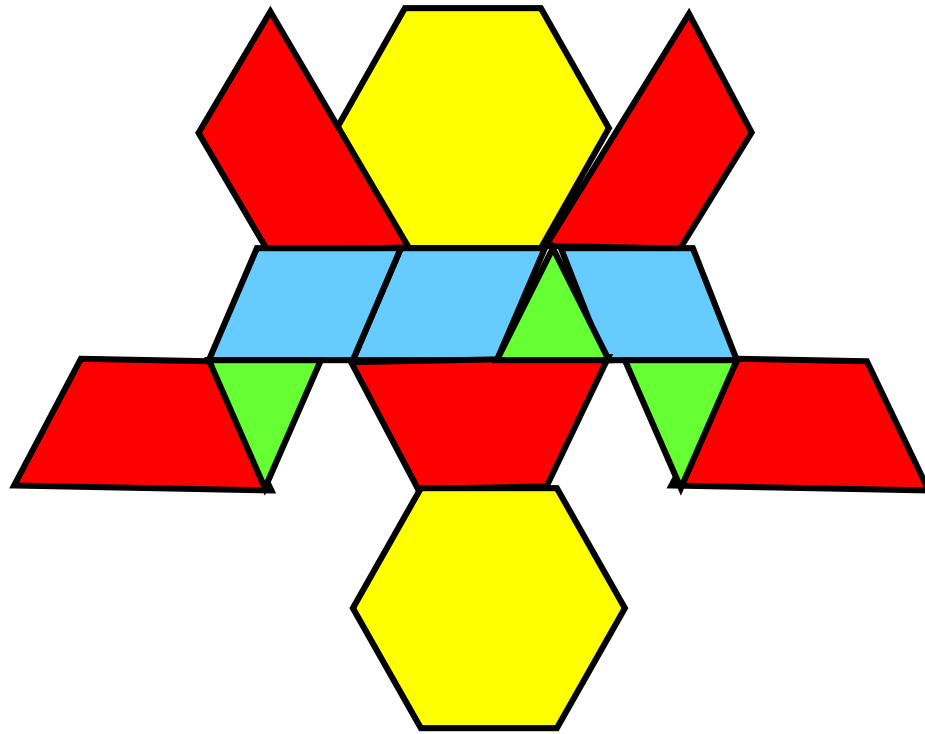


Part of an Area - 6 of 36 triangles

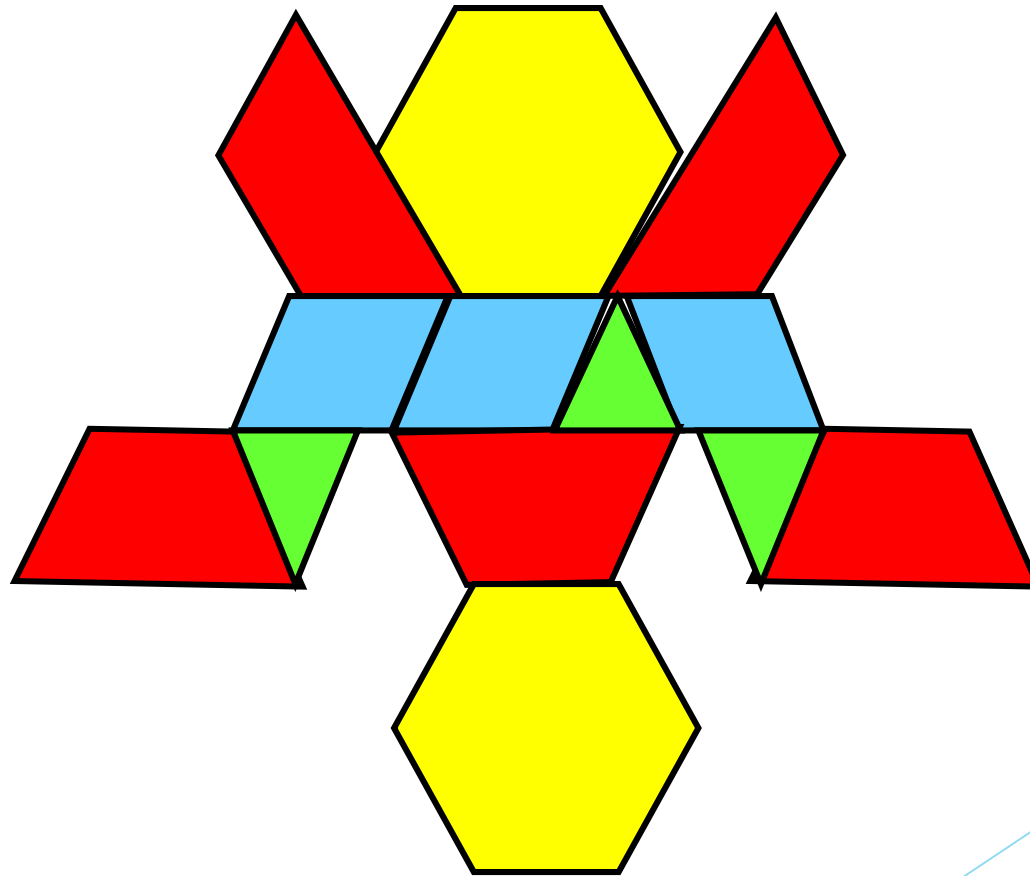


Part of an Area

1 of 6 hexagons



Part of an area -
Blue is $\frac{1}{3}$ of largest piece



NIM

- ▶ Goal is to make 21st tally mark.
- ▶ Two people take turns adding to one set of tally marks.
- ▶ On each turn, you may make 1, 2, or 3 tallies.

