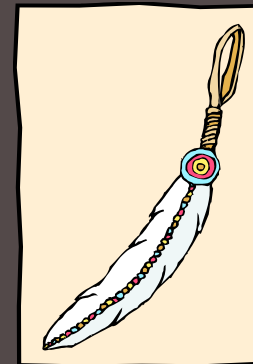


# NATIVE AMERICAN-BASED MATERIALS FOR INTEGRATION INTO UNDERGRADUATE MATHEMATICS COURSES

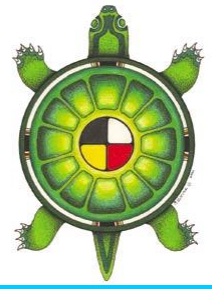
NCTM Annual Meeting  
April 15-18, 2015  
Boston, MA

PI-Dr. Charles P. Funkhouser  
Co-PI Miles Pfahl  
NSF Funded Project  
DUE Award #1122823





# PRESENTATION OUTLINE

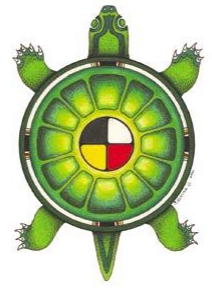


- Welcome and Introductions
- Project Purpose and Summary
- Project Description and Objectives
- Integration into Courses
- Lesson Piloting Protocol
- Facebook Page and Website
- The Lessons





# INTRODUCTIONS



## Miles Pfahl

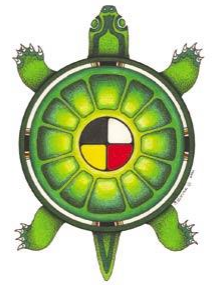
- Mathematics Instructor  
14 years at Turtle Mountain Comm. Coll. located on the Turtle Mountain Chippewa Res. Belcourt, ND
- Mathematics Teacher  
12 years at Turtle Mountain Comm. High School
- Project Director, PI, Co-PI  
Numerous grants and programs (7-12 and higher ed)

## Dr. Charles Funkhouser

- Mathematics Professor  
20 years at the University of Wyoming and Cal State Universities
- Math and Computer Sci. Teacher  
17 years at Frenchtown High School, Frenchtown, Montana
- NSF Project PI  
2003 – 2007 TUES Type I  
2011 – present TUES Type 2



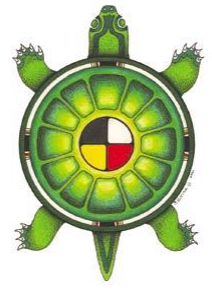
# MORE INTRODUCTIONS



- **Harriet Edwards – CoPI at California State University – Fullerton**
- **Patrick Weasel Head – Project Tribal Cultural Liaison**  
University of Montana (Retired)
- **Luther Olson – Project Materials Developer**  
Mathematics Instructor, Turtle Mountain Community College
- **Roberto Wheaton – Project Materials Developer**  
High School History/Science Instructor – Desert Hot Springs, CA
- **Michael Little Crow – Project Materials Developer**  
Mathematics Instructor, Scottsdale Community College
- **Cecelia Myerion and Frances Allard Abbott – Cultural Advisors**  
Turtle Mountain Community College



# PURPOSE



Infrequently mentioned in most mathematics instructional settings in the US is a parallel, rich system of mathematics developed and used by indigenous people of North America.

- These materials allow instructors of undergraduate courses to infuse culturally relevant and interesting mathematics activities into their courses.
- These materials will not only allow Native American students to be more fully involved in their learning, but also give all students a fuller appreciation of the universal nature and power of mathematics.

# NATIVE AMERICAN BASED MATERIALS FOR INTEGRATION INTO UNDERGRADUATE MATHEMATICS COURSES

## *PROJECT SUMMARY*

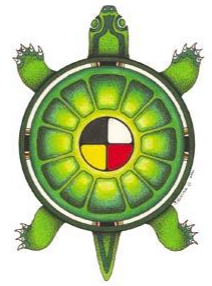


- Researches and develops undergraduate math materials based in the culture of Native American peoples.
- Materials are classroom ready.
- Various mathematical concepts that coincide with traditional math content in undergraduate courses.
- Give additional perspective as to how traditional math topics can be incorporated into real world situations in the Native American culture.





# PROJECT DESCRIPTION



- CSUF and TMCC develop materials based in intellectual and cultural traditions of Native American peoples to be used in undergraduate math courses.
- Integrate these materials into mainstream university and Tribal Community college mathematics courses.
- Foster faculty expertise in the materials' mathematics, methods and cultural bases.
- Assesses the materials' effects on student and instructor attitudes.
- Make the materials available for dissemination to universities and Tribal Community colleges.



# PROJECT OBJECTIVES



- 17 classroom ready lessons are being / have been developed including a powerpoint presentation and instructor guide for each lesson.
- Materials are being/have been piloted at CSUF, TMCC and other universities and community and Tribal colleges.
- Other technological enhancements have been developed such as a project website and Facebook page.
- Faculty training in deliverance of materials has taken place.
- Native American and other students will have integrated exposure to the traditional mathematics and methods of Native Peoples within courses taught in their undergraduate curriculum.



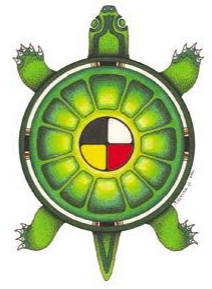
## CONTINUED...



- University and Tribal college faculty will have an opportunity to integrate traditional mathematics and methods of Native Peoples into the undergraduate courses they teach.
- The following topics from Native American mathematics will be integrated and implemented into undergraduate course: number theory, numeration systems, topology, measurement, probability and chance, statistics and data mining and geometry.
- The appropriateness and efficacy of the materials used in undergraduate courses will be assessed and evaluated.
- Changes in student and instructor attitudes towards Native American traditional mathematics and intellectual traditions will be assessed.
- Results will be widely disseminated.



# INTEGRATION INTO COLLEGE LEVEL MATHEMATICS COURSES



- Following is a list of Potential Undergraduate mathematics courses where the developed lessons may be integrated:
  - MATH 100 Applied Mathematics
  - MATH 102 Intermediate Algebra
  - MATH 111 College Algebra I
  - MATH 112 College Algebra II
  - MATH 103 University Algebra
  - MATH 212 Statistics I
  - MATH 213 Statistics II
  - MATH 335 Mathematical Probability
  - MATH 303 Fundamental Concepts in Elementary Mathematics
  - MATH 380 History of Mathematics
  - MATH 417 Foundations of Geometry
  - MATH 402 Logic and Geometry for the Secondary Teacher.



# LESSON PILOTING PROTOCOL



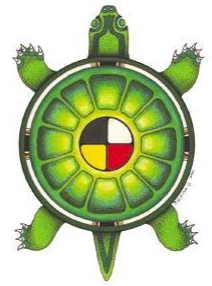
- Pre Attitude survey will be administered to the students participating in the project by faculty.
- Pre Attitude survey will be completed by the faculty member participating in the project.
- Post Attitude survey will be administered to both students and faculty participating in the project.
- A Post Student Focus Group session will be conducted after the lessons have been piloted.

## Documents:

1. Survey Administration Instructions
2. Student Survey
3. Instructor Survey
4. Protocol for Student Focus Group



# FACEBOOK PAGE



www.facebook.com/NativeAmericanMathematicsMaterials

The screenshot shows the Facebook page interface for "Native American based Mathematics Materials for Undergraduate Courses". At the top, the page name is displayed in the search bar, along with navigation icons for Home, 20+ notifications, and a user profile (Patty). Below the navigation bar, the page is set to post as "Patty Pfahl".

The main content area features an "Admin Panel" with options for "Edit Page", "Build Audience", "Help", and "Show". A "Promote Page" button is also visible. The page cover image shows the entrance to Turtle Mountain Community College. The page name "Native American based Mathematics Materials for Undergraduate Courses" is prominently displayed, with "2 likes" shown below it. An "Update Page Info" button and a "Liked" status are also present.

The "Community" section contains a description: "This project develops and researches undergraduate mathematics materials based in the culture and mathematics of Native American Peoples for integration into undergraduate courses. These materials are classroom ready." Below this, there are "About", "Photos", and "Likes" (2) sections.

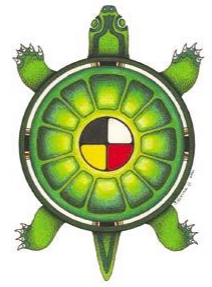
A "Highlights" dropdown menu is visible. The "Status" section prompts the user to post, with options for "Photo / Video" and "Event, Milestone +". A recent post from April 26 is shown, featuring the same cover image and a link to the project's website. The post text reads: "Check out our website of classroom ready materials for undergraduate math courses at our link in the 'about' section." Below the post are "Like", "Comment", and "Share" options.

An "Invite Your Friends to Like this Page" section is active, showing a search bar and a list of three friends: Ricanda D Gunville, Jaci Gunville, and Cheyenne Gunville, each with an "Invite" button.

At the bottom right, there is a "See Your Ad Here" section for the page, with a "Promote Page" button. The ad text repeats the project's description: "This project develops and researches undergraduate mathematics materials based in the culture and ma...". Below the ad, it shows a notification: "Like · Patty Pfahl likes this." and another "Promote Page" button.



# THE PROJECT WEBSITE



<http://math.fullerton.edu/cfunkhouser/>

## Native American-based Mathematics Materials

Departments of Mathematics, CSUF and TMCC



- [Home](#)
- [Teaching](#)
- [Research](#)
- [Lessons](#)
- [FAQs](#)

### Home

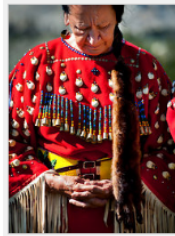
Hello! Here you'll find information on our NSF-sponsored DUE TUES Type 2 Project, "Native American-based Mathematics Materials for Integration into Undergraduate [Courses](#)," in partnership between California State University Fullerton (CSUF), and Turtle Mountain Community College (TMCC).



Information includes the cultural, mathematical and pedagogical stories behind the Project materials, the American Indian and mathematics personnel involved, and ongoing projects and opportunities for wider dissemination--and an [invitation](#) for your participation in our collaborative efforts. Information on current the types of materials being developed for this Project can be found on the [Teaching](#) page. More about the individual Project participants and their contact information can be found by clicking here at [Project Participants](#).

Our collaborative efforts focus on finding connections between traditional and current Native American culture, and mathematics as it taught in undergraduate [courses](#) at universities, and Tribal and community colleges. The results of our current research can be found on the [Research](#) page.

We also have collected some resources to help you begin using these culturally-based mathematics materials in a classroom setting or on your own. We encourage all undergraduate mathematics instructors and students, whether Native or non-Native, to explore the universal nature of mathematics presented here as products of our research. On the [Lessons](#) page, we have collected some files to help you to [get started](#).



**2013-2014 Info:**

**Office:**  
MH-157

**Address:**  
231 Coursey Lane  
Port Ludlow WA 98365

**Email:**  
cfunkhouser@fullerton.edu

**Phone:**  
206-300-3322

**Collaborators**  
Charles Funkhouser, PI  
Harriet Edwards, CoPI  
Miles Pfahl, CoPI (TMCC)  
Patrick Weasel Head  
Roberto Wheaton  
Michael Little Crow

## Native American-based Mathematics Materials

Department of Mathematics, CSUF and TMCC



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Scott Annin, CoPI  
Miles Pfahl, CoPI (TMCC)  
Patrick Weasel Head  
Roberto Wheaton  
Michael Little Crow

### Lessons

Below, you can [download](#) current versions of some of the materials that we've created!



#### Some useful notes on these lessons:

Each of the twelve lessons has at least three components: 1) traditional Lesson Materials available in Word format for user duplication and modification, 2) a Power Point presentation to give an overview of the lesson to the instructor and students, and 3) a Solution Key/Teacher's Guide for instructor use.

[Lesson 1](#) (*Transformational Geometry/Native Design Materials*)

[Lesson 1 PPT](#) (*PowerPoint*)

[Lesson 1 Solutions](#) (*Solutions*)

[Lesson 2](#) (*Probability/Plumstone Game Materials*)

[Lesson 2 PPT](#) (*PowerPoint*)

[Lesson 2 Solutions](#) (*Solutions*)

[Lesson 3](#) (*Numeration/Gesture Counting Materials*)

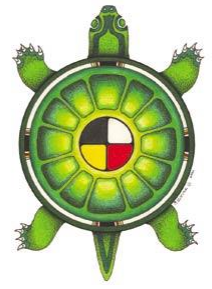
[Lesson 3 PPT](#) (*PowerPoint*)

[Lesson 3 Solutions](#) (*Solutions*)

[Lesson 3 Tutorial](#) (*Salish Counting Tutorial*)



# THE 17 LESSONS



- Transformational Geometry - Native Design
- Probability - Plumstone Game
- Numeration - Gesture Counting
- Geometry - Medicine Wheel
- Geometry - Tepee Surface Area and Volume
- Probability - Stick Game
- Numeration - Beading
- Geometry - Arrowheads
- Geometry - Beadwork
- Measurement - Hand Games
- Linear Programming - Native Clothing
- Geometry - Wigwam Surface Area
- Geometry - Tessellations Star Quilts
- Statistics - Diabetes Rates
- Geometry - Tepee Oblique Surface Area and Volume
- Algebra - Blood Quantum
- Numeration - Chippewa Grammar of Numbers



# TAKE A LOOK AT A LESSON OR TWO



*The Spirit Within Us!!*

**Miles Pfahl**  
Assistant Professor – Mathematics

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Email: [mrpfahl@tm.edu](mailto:mrpfahl@tm.edu)

EST. '72

<http://www.tm.edu>