## How to support your student as they learn about Composing and Decomposing

Mathematics is a connected set of ideas, and your student knows a lot. Encourage them to use the mathematics they already know when seeing new concepts in this module.

## Module Introduction

In this module your student will learn more about numbers and shapes and their relationships. There are four topics in this module: Factors and Multiples, Positive Rational Numbers, Shapes and Solids, and Decimals. Your student will use what they already know about area, number properties, and volume in this module.

## Academic Glossary

Each module will highlight an important term. Knowing and using these terms will help your student think, reason, and communicate their math ideas.

| Term | Analyze |
| :--- | :--- |
| Definition | - To study or look closely for patterns. <br> - To break down a concept into smaller parts <br> to gain a better understanding of it. |
| Questions to <br> Ask Your <br> Student | - Do you see any patterns? <br> - Have you seen something like this before? <br> - What happens if the shape, model, or <br> numbers change? |
| Related Phrases | - Examine <br> - Evaluate <br> - Determine <br> - Observe <br> - Consider <br> - Investigate <br> - What do you notice? |

## Example: Topic 1 Lesson 2

Determine the least common multiple of 6 and 9 .
a. List the first 9 multiple of 6 .
b. List the first 6 multiples of 9 .
c. What is the least common multiple of 6 and 9 ?

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## Math Process Standards

Each module will focus on a process (or a pair of processes) that will help your student become a mathematical thinker. The "I can" statements listed below help your student to develop their mathematical learning and understanding.

Communicate mathematical ideas, reasoning, and their implications using multiple representations including symbols, diagrams, graphs, and language as appropriate.

I can:

- explain what a problem "means" in my own words.
- create a plan and change it if necessary.
- ask useful questions when trying to understand the problem.
- explain my reasoning and defend my solution.
- reflect on whether my results make sense.

Look for examples of these processes in the Topic Summaries.

## The Carnegie Learning Way

## Our Instructional Approach

Carnegie Learning's instructional approach is based on how people learn and real-world understandings. It is based on three key components:

| ENGAGE | DEVELOP | DEMONSTRATE |
| :---: | :---: | :---: |
| Purpose: Provide an <br> introduction that creates <br> curiosity and uses what <br> students already know <br> and have experienced. <br> Questions to Ask: <br> How does this problem <br> look like something you <br> did in class? | Purpose: Build a deep <br> understanding of <br> mathematics through <br> different activities. <br> Questions to Ask: <br> Do you know another <br> way to solve this <br> problem? Does your <br> answer make sense? | Purpose: Reflect on <br> and evaluate what was <br> learned. |
| Is there anything you do <br> not understand? |  |  |



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## Module Overview



## Topic 1: Factors and Multiples

| Key Terms |  |  |
| :---: | :---: | :---: |
| - numeric expression <br> - equation <br> - Distributive Property <br> - base <br> - power | - exponent <br> - common factor <br> - relatively prime <br> - greatest common factor (GCF) | - multiple <br> - Commutative Property <br> - least common multiple (LCM) |
| The Distributive Property, when applied for multiplication, states that for any numbers $a, b$, and $c$, $a(b+c)=a b+a c$. | The exponent of the power is the number of times the base is used as a factor. $8^{4}=8 \cdot 8 \cdot 8 \cdot 8$ <br> exponent | A multiple is the product of a given whole number and another whole number. <br> multiples of 10 : |
| Follow the link to access the Mathematics Glossary: https://www.carnegielearning.com/texas-help/students-caregivers/ |  |  |

In this topic, students will learn more about factors and multiples. They use area models to show the factors of a given number and the common factors of two or more numbers. Students use factor trees to organize the prime factors of a number. Then, they use tables to determine common factors, the greatest common factor (GCF), and the least common multiple (LCM) of two or more numbers.

## Area Models

The equation $5 \cdot 27=135$ shows that the expression $5 \cdot 27$ is equal to the expression 135 . An equation is a mathematical sentence that uses an equals sign to show that two or more quantities are the same as one another.

The area model shows the side length of 27 split into two parts.


$$
5 \cdot 27=5(20+7)
$$

The factors for each region are $(5 \cdot 20)+(5 \cdot 7)$.
The area of each smaller region is $100+35$.
The total area is 135 .

## Factor Trees to Determine the Prime Factors of a Number

A factor tree is a way to organize the prime factors of a number. Choose any factor pair to get started.

- Begin with the number 36 .
- Pick any whole number factor pair of 36, other than 1 and 36 .
- Draw a branch from 36 to each factor, 3 and 12.
- Since both of the factors are not prime, you are not finished.
- Use branches to write a factor pair for 12.
- Since both of the factors of 12 are not prime, you are not finished.

- Because 2 and 3 are prime, this factor tree is complete.

$$
36=2 \cdot 2 \cdot 3 \cdot 3
$$

Repeated Multiplication as a Power
$36=2 \cdot 2 \cdot 3 \cdot 3$
$36=2^{2} \cdot 3^{2}$
The prime factorization shown has repeated factors. You can
repreparts: the base and the exponent.
the base of a power is the factor multiplied by itself
repeatedly, and the exponent of the power is the number
of times you use the base as a factor.


Using a Table to Determine the GCF and LCM

You can organize the prime factors of two or more numbers into a table. Only list shared factors that are in both rows in the same column.

| Number | Prime Factors |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 56 | 2 | 2 | 2 |  | 7 |  |
| 42 | 2 |  |  | 3 | 7 |  |

In the table shown, the common prime factors of 56 and 42 are 2 and 7 .

The greatest common factor (GCF) is the product of the shared prime factors. $2 \cdot 7=14$, so the GCF of 56 and 42 is 14 . The least common multiple (LCM) is the product of the shared and non-shared prime factors. Both 2 and 7 are shared factors. They are only used once in the product. $2 \cdot 2 \cdot 2 \cdot 3 \cdot 7=168$, so the LCM of 56 and 42 is 168 .


## Topic 2: Positive Rational Numbers

| Key Terms |  |
| :---: | :---: |
| - unit fraction <br> - equivalent fraction <br> - benchmark fractions <br> - algorithm | - rational number <br> - reciprocal <br> - multiplicative inverse <br> - complex fraction |
| Fractions that represent the same part-towhole relationship are equivalent fractions. | The multiplicative inverse of a number $\frac{a}{b}$ is the number $\frac{b}{a}$, where $a$ and $b$ are nonzero numbers. The product of any nonzero number and its multiplicative inverse is 1 . The multiplicative inverse of a number is also known as the reciprocal of a number. <br> The multiplicative inverse of $\frac{3}{7}$ is $\frac{7}{3}$. $\frac{3}{7} \cdot \frac{7}{3}=\frac{21}{21}=1$ <br> The multiplicative inverse of 5 is $\frac{1}{5}$. $\frac{5}{1} \cdot \frac{1}{5}=\frac{5}{5}=1$ |
| Follow the link to access the Mathematics Glossary: https://www.carnegielearning.com/texas-help/students-caregivers/ |  |

In this topic, students will focus on fraction multiplication and division. They will create physical models to represent and compare fractions, and determine equivalent fractions. They use an area model for multiplication with fractions before using an algorithm, or step-by-step method.

## MATH PROCESS STANDARDS

## How do the activities in Positive Rational Numbers promote student expertise in the math process standards?

NOTE: This is an example of the math process standard: Communicate mathematical ideas, reasoning, and their implications using multiple representations including symbols, diagrams, graphs, and language as appropriate.

- I can explain what this area model means in my own words.

Refer to page 2 for more " 1 can" statements.

Consider the expression $\frac{1}{4} \cdot \frac{1}{2}$ represented in the area model shown.


How are the factors of the product $\frac{1}{4} \cdot \frac{1}{2}$ represented in the model?

Also in this topic, students use models of fractions with division, and then use a dividing across strategy.

## Using Strip Diagrams to Represent Quotients with Fractions

A strip diagram can show the quotient of two fractions, such as $\frac{3}{4} \div \frac{1}{4}$. The division expressions asks, "How many $\frac{1}{4}$ are in $\frac{3}{4}$ ?"


There are 3 one-fourths in $\frac{3}{4}$, so $\frac{3}{4} \div \frac{1}{4}=3$.


Finally, students learn the standard algorithm, or steps, for dividing fractions. They rewrite division expressions as multiplication by the reciprocal, or multiplicative inverse.

Dividing Fractions



Rewrite the division expression as a complex fraction.

Multiply the numerator and denominator by the multiplicative inverse of $\frac{3}{4}$.

Perform multiplication and rewrite the denominator as 1 .

## Topic 3: Shapes and Solids

| Key Terms |  |  |
| :---: | :---: | :---: |
| - Triangle Inequality Theorem <br> - Triangle Sum Theorem <br> - parallelogram <br> - variable <br> - straightedge | - trapezoid <br> - geometric solid <br> - polyhedron <br> - face <br> - edge | - vertex <br> - right rectangular prism <br> - cube <br> - volume <br> - unit cube |
| The Triangle Sum Theorem states that the sum of the measures of the interior angles of a triangle is $180^{\circ}$. | A geometric solid is a bounded three-dimensional geometric figure. | A right rectangular prism is a polyhedron with three pairs of congruent and parallel rectangular faces. |
| Follow the link to access the Mathematics Glossary: https://www.carnegielearning.com/texas-help/students-caregivers/ |  |  |

In this topic, students determine if three given line segments will create a triangle or not.

## Triangle Inequality Theorem

The Triangle Inequality Theorem states that the sum of the lengths of any two sides of a triangle is greater than the length of the third side.
$A C+C B>A B$
$B A+A C>B C$


Also in this topic, students use hands-on tools to learn about the sum of the interior angles of a triangle and the relationship between triangle side and angle measures.

## Triangle Sum Theorem

The Triangle Sum Theorem states the relationship between the three angles in a triangle.


The sum of the measures of the interior angles of a triangle is $180^{\circ}$.

Trevor organizes a bike race called the Tri-Cities Criterium. Criteriums consist of several laps around a closed circuit. He designs a triangular circuit.


Use the Triangle Sum Theorem to determine the measure of the third angle in the triangular circuit.

$$
\begin{gathered}
x+90^{\circ}+50^{\circ}=180^{\circ} \\
x+140^{\circ}=180^{\circ} \\
x=40^{\circ}
\end{gathered}
$$

From their knowledge of rectangles and area, students also develop the formula, or rule, for determining the area of parallelograms, triangles, and trapezoids. Students calculate the volume of right rectangular prisms.

## Area of a Parallelogram

A parallelogram is a four-sided figure with two pairs of parallel sides with each pair equal in length. In a parallelogram, the height is the distance from the base to the opposite side at a right angle. The area of a parallelogram is equal to $b \cdot h$, where the variable $b$ represents the base and $h$ represents the height. A variable is a letter used to represent a number.

For example, in this parallelogram, the base, $b$, is 20 feet and the height, $h$, is 12 feet.

Area of a parallelogram $=b h$

$$
\begin{aligned}
& =(20)(12) \\
& =240 \text { square feet }
\end{aligned}
$$




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## Area of a Triangle

The area of a triangle is equal to $\frac{1}{2} b h$. The base of a triangle can be any of its sides.


Draw a line straight down from the top corner of the triangle to the bottom, or base at a right angle. This is called the height of the triangle.

For example, in this triangle, the base, $b$, is equal to 3 feet and the height, $h$, is equal to $2 \frac{1}{5}$ feet.

Area of a triangle $=\frac{1}{2} b h$

$$
\begin{aligned}
& =\frac{1}{2}(3)\left(2 \frac{1}{5}\right) \\
& =3 \frac{3}{10} \text { square feet }
\end{aligned}
$$



## Area of a Trapezoid

A trapezoid has two bases that are parallel to each other, often labeled $b_{1}$ and $b_{2}$. The other two sides of a trapezoid are called the legs of the trapezoid. A height of a trapezoid is the length of the shortest line drawn from one base to the other at a right angle.


The area of a trapezoid is equal to $\frac{1}{2}\left(b_{1}+b_{2}\right) h$.

## Topic 4: Decimals

| Key Terms |  |
| :---: | :---: |
| - kite <br> - composite solid | - terminating decimal <br> - repeating decimal |
| A composite solid is made up of more than one geometric solid. | When you write a fraction as a decimal using division, and a digit or a group of digits repeats without end in the quotient, the resulting decimal is a repeating decimal. $\begin{aligned} & \frac{1}{9}=0.111 \ldots \quad \frac{7}{12}=0.58333 \ldots \\ & \frac{22}{7}=3.142857142857 \ldots \end{aligned}$ |
| Follow the link to access the Mathematics Glossary: https://www.carnegielearning.com/texas-help/students-caregivers/ |  |

In this topic, students plot decimals on a number line and compare and order decimal values.

## Plotting, Comparing, and Ordering Rational Numbers

Compare $\frac{1}{2}$ and 0.35 . Which value is greater? First, convert $\frac{1}{2}$ to a decimal. $\frac{1}{2}$ is equivalent to $\frac{5}{10}$, or 0.5 . Plot each value on a number line.


Because $\frac{1}{2}$ is to the right of 0.35 on the number line, $\frac{1}{2}$ is greater than 0.35 , or $\frac{1}{2}>0.35$.

Students review addition and subtraction of decimal numbers and practice calculating correctly and quickly.

## Adding and Subtracting Decimals

When adding or subtracting decimals, it is important to line up the digits on the correct place values. Estimating sums or differences gives students a sense of the reasonableness of an answer before calculating the sum or difference.

$$
18.205-3.91
$$

First, estimate the answer so you know the approximate difference.
$18-4=14$

Then, line up the decimals so that correct place values are in the same column and subtract.

$$
\begin{array}{r}
7.1110 \\
18.8 Q 5 \\
-3.910 \\
\hline 14.295
\end{array}
$$

Compare the answer to your estimate to check your work.

The estimate of 14 and the difference of 14.295 are reasonably close, so the difference appears to be correct.

## Multiplying Decimals

In this topic, students review whole-number and decimal multiplication.


A poster is rolled up and mailed in a cardboard box in the shape of a rectangular prism. Determine the volume of the box.

The formula for determining the volume of a rectangular prism is volume $=$ length $\cdot$ width $\cdot$ height, or $V=l \cdot w \cdot h$. Multiply the three values. $36 \cdot 2 \cdot 3.46=249.12$ The volume of the box is 249.12 cubic inches.


## Using a Standard Algorithm to Divide Decimals

The long division algorithm uses organized estimation and place value to determine a quotient, or the number of times the divisor is contained in the dividend.

Let's use the standard algorithm to solve $3.57 \div 3$. The dividend is 3.57 and the divisor is 3 .

5 tenths divided into 3 equal groups is 1 tenth in each group with 2 tenths left over.

3 ones divided into 3 equal groups is 1 one in each group with 0 ones left over.


The quotient is 1.19 ; therefore, $3.57 \div 3=1.19$.

Discuss important dates throughout this module such as assessments, assignments, or class events with your student. Use the table to record these dates and reference them as your student progresses through the module.

| Important Dates |  |
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| Date |  |
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Using the link below, visit the Texas Math Solution Support Center for students and caregivers to access additional resources such as:

- Mathematics Glossaries
- Videos
- Topic Materials
- A Letter to Families and Caregivers

