



Deeper Dive into Cypher.PL

Executable semantics of Cypher 9
written in logic

{JAN.POSIADALA,PAWEL.SUSICKI}@GMAIL.COM

Cypher.PL academia advisor

Prof. at University of Warsaw
Institute of Informatics

Fields of research

- Logic in Computer Science
- Databases
 - semi-structured databases
 - XML Schema mappings
- Knowledge representation
 - description logics
 - ontology-mediated query answering
- Automata Theory
 - tree automata



Filip Murlak

Cypher.PL

What is Cypher.PL

- executable specification
- of declarative query language (Cypher)
- in formal declarative language of logic (Prolog)
- as close to the semantics as possible
- as far from the implementation issues as possible
- a tool for collective designing, verification, validation
- without losing of preciseness and explicitness

Policy Paper

Specifications Are (Preferably) Executable

by Norbert E. Fuchs, Software Engineering Journal, September 1992

Series of symposiums 1980/90:

Programming Language Implementation and Logic Programming

Why Prolog?

- declarative language
- with built-in unification...
- ...which is more general than pattern matching
- super-native data (structures) representation
- multiple solutions/evident ambiguity
- easy constraint verification
- DCG: notation for grammars
- meta-programming
- generative aspect of nature

Current status

Specifies semantics of Cypher 9+

- 100% compatibility to TCK test set
- reflects semantics ambiguity due to driving table order
- graph values support

Language extension: support for graph values (also known as 'g-records', graph-records or graphlets) and operations on them:

- binary functions: gunion, gintersection, gminus
- aggregation functions: agunion, agintersection

As graph value generalizes node, relationship and path values, all new listed functions accept arguments of those types.

Basic Concepts

Cypher.PL basic concepts:

- I. Query intermediate representation
- II. Environment: Tables × Graphs
- III. General schema of clause evaluation

One-slide tutorial of logic programming

```
% Logical connectives
```

```
?- (true;false),(false>true).  
true.
```

```
?- false;false.  
false.
```

```
% Unification
```

```
?- member(X,[1,2]).  
X = 1 ;  
X = 2.
```

```
% Rules
```

```
father(X,Y) :- parent(X,Y), man(X).  
mother(X,Y) :- parent(X,Y), woman(X).
```

```
% Meta-programming
```

```
?- call(member(X,[1,2])). % member is callable term  
X = 1 ;  
X = 2.
```

```
% Partial application
```

```
?- call(member(X),[1,2]).  
X = 1 ;  
X = 2.
```

```
?- call(member,X,[1,2]).  
X = 1 ;  
X = 2.
```

```
%Multiple solutions
```

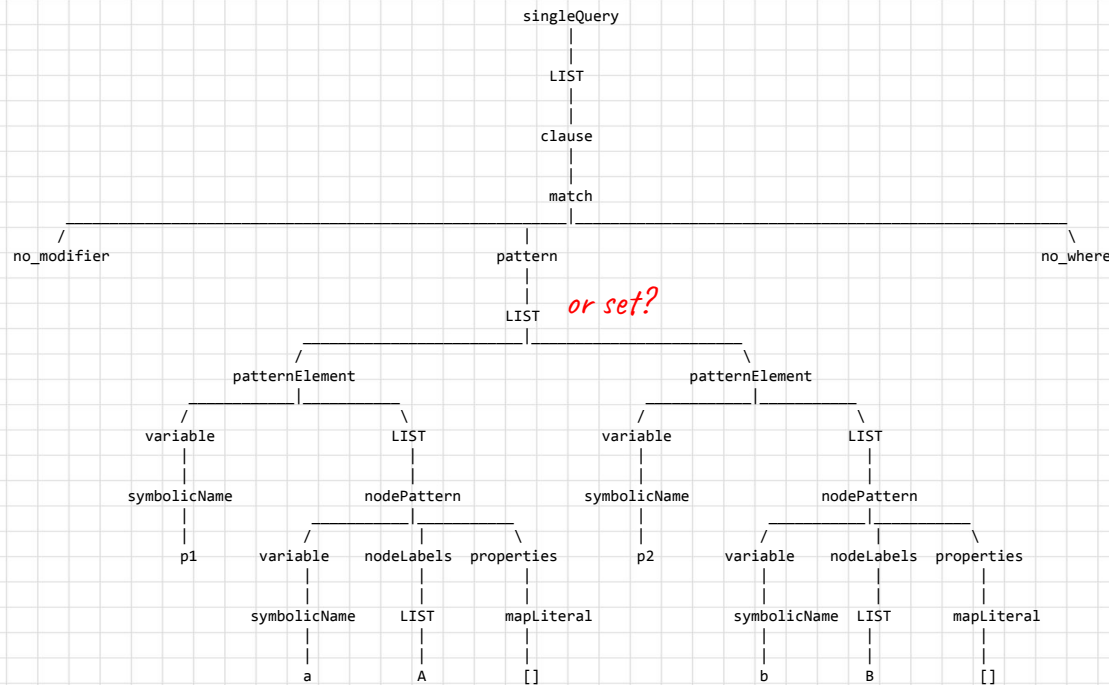
```
?- findall(X,member(X,[1,2]),Xs).  
Xs = [1, 2].
```

```
% Lambda expressions
```

```
?- maplist([X]>>between(1, 5, X),[1,2,3,5]).  
true.
```

Intermediate Representation: just a tree

```
match p1=(a:A),p2=(b:B)
```



Syntax-sugar-free query
Base for semantics definition

Machine-oriented

- *Verbose*
- *Explicit*
- *Unambiguous*

Planner-friendly

- *Minimal ordering constraints*
- *Unique variable names*
- *Human-friendly*

Mainly for debugging, not a primary goal

IR.pl: just a tree definition

```
single_query(singleQuery(Clauses)) :- maplist(clause,Clauses).
```

```
%%% Clauses %%%
```

```
clause(clause(Clause)) :- match(Clause).
```

```
% ...
```

```
clause(clause(Clause)) :- with(Clause).
```

```
clause(clause(Clause)) :- return(Clause).
```

```
%%% Match %%%
```

```
match(Clause)
```

```
:-
```

```
Clause = match(MatchModifier,Pattern,Where),
```

```
match_modifier(MatchModifier),
```

```
pattern(Pattern),
```

```
where(Where).
```

```
match_modifier(no_modifier).
```

```
match_modifier(optional).
```

```
%match_modifier(mandatory). %in the future
```

```
pattern(pattern(PatternElements)) :-
```

```
maplist(pattern_element,PatternElements).
```

```
pattern_element(patternElement(Variable,Patterns)) :-
```

```
variable(Variable),
```

```
patterns(Patterns).
```

```
node_pattern(nodePattern(Variable,NodeLabels,Properties)) :-
```

```
variable(Variable),
```

```
node_labels(NodeLabels),
```

```
properties(Properties).
```

```
node_labels(nodeLabels(Labels)) :- maplist(name,Labels).
```

```
relationship_pattern(relationshipPattern(Variable  
,Direction  
,RelationshipTypes  
,RelationshipRange  
,Properties))
```

```
:-
```

```
variable(Variable),
```

```
direction(Direction),
```

```
relationship_types(RelationshipTypes),
```

```
relationship_range(RelationshipRange),
```

```
properties(Properties).
```

```
direction(direction(left)).
```

```
direction(direction(right)).
```

```
direction(direction(both)).
```

```
relationship_types(relationshipTypes(Types)) :- maplist(name,Types).
```

```
relationship_range(relationshipRange(one_one)).
```

```
relationship_range(relationshipRange(L,U)) :-
```

```
(L=unlimited;integer(L)),%L >= 0,
```

```
(U=unlimited;integer(U)) %U >= 0
```

```
.
```

```
properties(properties(mapLiteral(Properties)) :-
```

```
maplist([(propertyKeyName(PropertyName),Expression)]>>(schema_name(PropertyName),expression(Expression)),
```

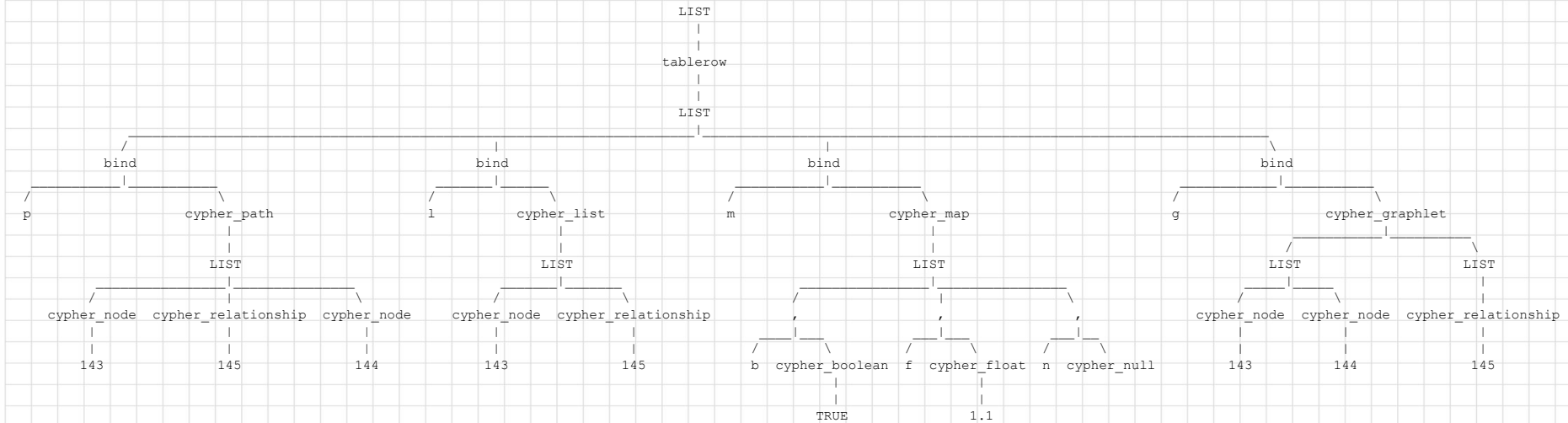
```
Properties).
```

```
where(where(Expression)) :- expression(Expression).
```

```
where(no_where).
```


Environment: driving table...

```
create p=(a:A {int: 1, string: 'S', boolean : true, float: 1.1 }-[r:RELTYPE]->(b)
return p, [a,r] as l, {b : a.boolean, f : a.float, n : a.n} as m, union(p,p) as g
```



Environment: driving table...

```
is_row_of_driving_table(tablerow(TableRow)) :-  
is_list(TableRow),  
maplist([bind(Name,Value)]>>(name(Name),cypher_value(Value)),TableRow).  
  
%primitives:  
%     cypher_null,  
%     cypher_string(Value),  
%     cypher_integer(Value),  
%     cypher_float(Value),  
%     cypher_boolean(Value),  
%entities:  
%     cypher_node(NodeId),  
%     cypher_relationship(RelationshipId),  
%     cypher_path(NodesRelationshipsAlernatingList),  
%     extended with cypher_graphlet(CypherNodesList,CypherRelationshipsList)  
%structures:  
%     cypher_list(CypherValuesList),  
%     cypher_map(NamesCypherValuesPairsList)
```

Environment: ... and property graph

```
graph TD
    LIST --> node137
    LIST --> node138
    LIST --> label137
    LIST --> relationship137
    LIST --> type139
    LIST --> property137_boolean
    LIST --> property137_float
    LIST --> property137_int
    LIST --> property137_list
    LIST --> property137_string

    node137 --- node138
    node137 --- label137
    node137 --- relationship137
    node137 --- type139
    node137 --- property137_boolean
    node137 --- property137_float
    node137 --- property137_int
    node137 --- property137_list
    node137 --- property137_string

    label137 --- A
    relationship137 --- 139
    relationship137 --- 138
    type139 --- RELTYPE
    property137_boolean --- boolean
    property137_boolean --- cypher_boolean
    cypher_boolean --- TRUE
    property137_float --- float
    property137_float --- cypher_float
    cypher_float --- 1.1
    property137_int --- int
    property137_int --- cypher_integer
    cypher_integer --- 1
    property137_list --- list
    property137_list --- cypher_list
    cypher_list --- LIST
    LIST --- cypher_integer1
    cypher_integer1 --- 1
    LIST --- cypher_integer2
    cypher_integer2 --- 2
    property137_string --- string
    property137_string --- cypher_string
    cypher_string --- S
```

```
%read (matching) "api"
node(NodeId,Graph) :- member(node(NodeId),Graph).
relationship(NodeStartId,RelationId,NodeEndId,Graph) :- member(relationship(NodeStartId,RelationId,NodeEndId),Graph).
property(NorRId,Key,Value,Graph) :- member(property(NorRId,Key,Value),Graph).
label(NodeId,Label,Graph) :- member(label(NodeId,Label),Graph).
type(RelationshipId,Type,Graph) :- member(type(RelationshipId,Type),Graph).

%write "api"
create_node(NodeId,Graph,ResultGraph) :-....
delete_node(NodeId,Graph,ResultGraph) :-....

set_label(NodeId,LabelName,Graph,ResultGraph) :-....
remove_label(NodeId,LabelName,Graph,ResultGraph) :-....

create_relationship(NodeStartId,NodeEndId,RelationshipType,RelationshipId,Graph,ResultGraph) :-....
delete_relationship(RelationshipId,Graph,ResultGraph) :-....

set_property(Id,Key,Value,Graph,ResultGraph) :-....
remove_property(Id,Key,Graph,ResultGraph) :-....
```

General schema of clause evaluation

```
eval_single_query(Graph,  
                  singleQuery(Clauses),  
                  environment(ResultTable, ResultGraph))  
  
:-  
foldl(eval_clause,  
      Clauses,  
      environment([tablerow([])], Graph),  
      environment(ResultTable, ResultGraph)).  
  
eval_clause(clause(Clause), %clause(match(MatchModifier, Pattern, Where))  
           %clause(with(WithModifier, ReturnBody, Where))  
           %clause(unwind(Expression, Variable))  
           %...  
           environment(Table, Graph),  
           environment(ResultTable, ResultGraph))  
  
:-  
%particular clause semantics definition
```

CIR's with Cypher.PL's contribution

- #219 Grouping key selection for aggregating subqueries
- #264 Expressions allowed in WHERE subclause of WITH clause with aggregations

J. Posiadata, P. Susicki *Semantics of implied group by clause with mixed expressions. A simple use case of Cypher.PL – an executable specification of Cypher query language.* (withdrawn from GraphSM 2018 due to date conflict).

- #263 Node/relationship accessibility after DELETE operations
- #315 Ambiguity in parsing [value in list]
- #296 Resolving MERGE being dependant on evaluation order

As the source of ambiguity in openCypher is generally reducing semantics of unordered bag to semantics of ordered list, now in Cypher.PL driving table has no order.

#296 Ambiguity due to evaluation order

```
create
  ({num : 1}),({num : 2})
with
  *
match
  (n)
return
  (collect(n)[1]).num as nn
```

nn
1

nn
2

```
CREATE
  (:A{x:1}), (:A{x:2}), (:B)
WITH
  *
MATCH
  (a:A), (b:B)
SET
  b.x = a.x
return
  b.x
```

b.x
1

b.x
2

```
create
  (a {num: 1})-[r1:T]->(b {num: 2})-[r2:T]->(c {num: 3})
match
  (x)-[z]->(y)
set
  x.num = maximum([(k)-->(1) | 1.num]) + 10
return
  x.num as xnum //ambiugous result
```

xnum
23
13

xnum
13
13

Ambiguity handling in Cypher.PL

```
eval_clause(clause(Clause),environment(Table,Graph), environment(ResultTable,ResultGraph))
```

```
:-
```

```
scall(set(Table),  
      eval_clause_(Clause,Graph),  
      environment_eq,  
      environment(ResultTable,ResultGraph)).
```

```
scall(set(Set),Goal,EqGoal,Solution) :-
```

```
findall(PermutationSolution  
      ,(permutation_(Set,Permutation),call(Goal,Permutation,PermutationSolution))  
      ,PermutationSolutions),
```

```
gr_by(EqGoal,PermutationSolutions,SolutionsGroups),  
member([Solution | _],SolutionsGroups).
```

```
eval_clause_(Clause,Graph,Table,environment(ResultTable,ResultGraph)) :- %particular clause semantics definition
```

```
environment_eq(environment(Table1,Graph1),environment(Table2,Graph2))
```

```
:-
```

```
permutation(Table1,Table2),  
isomorphic(Graph1,Graph2).
```

Intuitiveness (1/3)



boggle commented on 2 Feb • edited ▾

Contributor

That makes me wonder if it might be (conceptually possible) to express `MERGE` using subquery operators like this:

```
MATCH (a)
MATCH {
  MATCH {
    MATCH (a)-[:X]->(m {prop: n.prop})
    RETURN n, m
  }
  OTHERWISE // query-level xor that has been discussed in the past
  MATCH {
    CREATE (a)-[:X]->(m {prop: n.prop})
    RETURN n, m
  }
}
```

This shows where the problem is: It still would create duplicates and the only way to emulate `MERGE` that I could see would be a graph-level squashing operation of similarly looking entities. Even that would still not be the same, giving a real argument why `MERGE` is a core feature.

Intuitiveness (2/3)

```
eval_merge(merge(patternElement(Variable,Patterns), MergeActions),
           Graph,
           TableRow,
           environment(ResultMatchTable,ResultMergeGraph))

:-
eval_clause(clause(match(no_modifier,pattern([patternElement(Variable,Patterns)]),no_where)),
            environment([TableRow],Graph),
            environment(ResultMatchTable,Graph)),
not(ResultMatchTable = []),
!,
convlist([onMatch(Set),Set]>>true, MergeActions,OnMatchActions),
foldl(eval_merge_actions,
      OnMatchActions,
      environment(ResultMatchTable,Graph),
      environment(ResultMatchTable,ResultMergeGraph)).
```

Intuitiveness (3/3)

```
eval_merge(merge(patternElement(Variable, Patterns), MergeActions),
           Graph,
           TableRow,
           environment(ResultCreateTable, ResultMergeGraph))

:-
eval_clause(clause(create(pattern([patternElement(Variable, Patterns)]))),
            environment([TableRow], Graph),
            environment(ResultCreateTable, ResultCreateGraph)),
convlist([onCreate(Set), Set]>>true, MergeActions, OnCreateActions),
foldl(eval_merge_actions,
      OnCreateActions,
      environment(ResultCreateTable, ResultCreateGraph),
      environment(ResultCreateTable, ResultMergeGraph)).
```

Future directions

Cypher 9:

- examining TCK test set in ambiguity sensitive mode
- define rules of errors rising as explicitly as possible with preservation of distinction between 'compile time and 'runtime'
- to specify node/relationship accessibility after DELETE operation

Cypher 10/CAPS draft specification including:

- multiple graphs family features
- RPQ
- configurable morphism of pattern matching

Other languages: G-Core, GQL

- executable semantics

Current version is accessible to experiment in console mode:

```
$ ssh cypherpl/cypherpl@185.25.216.85
```

Bibliography

- [1] M. A. AlTurki, J. Meseguer, **Executable rewriting logic semantics of Orc and formal analysis of Orc programs**, Journal of Logical and Algebraic Methods in Programming, Volume 84, Issue 4, Pages 505–533, 2015,
- [2] K. R. Apt. **From Logic Programming to Prolog**. Prentice-Hall, Inc., Upper Saddle River, NJ, USA. 1996
- [3] C. Ellison and G. Rosu. **An executable formal semantics of C with applications**. SIGPLAN Not. 47, 1 533–544, (January 2012).
- [4] M. P. J. Fromherz, **A Survey of Executable Specification Methodologies**, Technical Report 89.05, Department of Computer Science, University of Zurich
- [5] Norbert E. Fuchs, **Specifications Are (Preferably) Executable**, Software Engineering Journal, September 1992
- [6] International Organization for Standardization. **ISO/IEC 9075:2016: Information technology – Database languages – SQL**, 2016.
- [7] G. Gupta, E. Pontelli, **Specification, Implementation, and Verification of Domain Specific Languages: A Logic Programming-Based Approach**. In: Kakas A.C., Sadri F. (eds) Computational Logic: Logic Programming and Beyond. Lecture Notes in Computer Science, vol 2407. Springer, Berlin, Heidelberg, 2002
- [8] R. A. Kowalski, **The relation between logic programming and logic specification**, in: C. A. R. Hoare, J. C. Shepherdson (Eds.), Mathematical Logic and Programming Languages, Prentice-Hall International, 1985
- [9] Neo Technology Inc. **openCypher project**, <http://www.opencypher.org/> 2018.01.01
- [10] U. Nilsson and J. Maluszynski. **Logic, Programming, and PROLOG** (2nd ed.). John Wiley & Sons, Inc., New York, NY, USA. 1995.
- [11] I. Robinson, J. Webber, and E. Eifrem. **Graph Databases**. O'Reilly Media, Inc. 2013
- [12] J. Wielemaker, T. Schrijvers, M. Triska, and T. Lager, **SWI-Prolog. Theory and Practice of Logic Programming**, 12(1–2), 67–96. doi:10.1017/S1471068411000494, 2012.