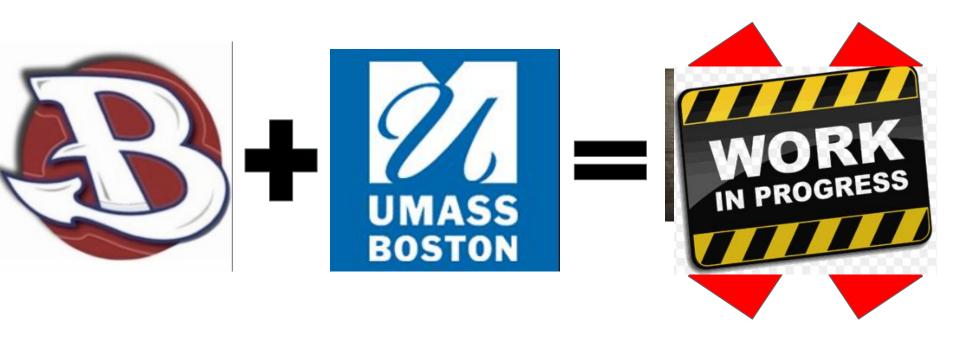
Defining: Number Concept & Number Sense

Carrie Fortunato NCTM 4/6/17

One District's Journey



Define: Number Concept and Number Sense

Number Concept-

Number Sense-

Burlington's Definition of....

Number Concept-

- 1:1 Correspondence with Sequencing
- 2. Number Recognition
- 3. Subitizing/Visual Clustering
- 4. Lexical Entry of Number
- 5. Decomposition/Recomposition of Numerals

Number Sense-

- 1. Number Concept
- 2. Number Combinations
- 3. Place Value
- 4. Computation
- 5. Application of Word Problems

Adapted from Mahesh Sharma- Professor at the Center for Teaching Mathematics for All

Materials

To Build, to borrow, or to buy?

When Building:

What format? Who helps? What does it take? What is the best way to distribute?

When Borrowing:

Why adapt? What is wrong with existing materials?

When Buying:

Where do we find evidence-based materials?

What is the cost?

Are We Missing Anything?

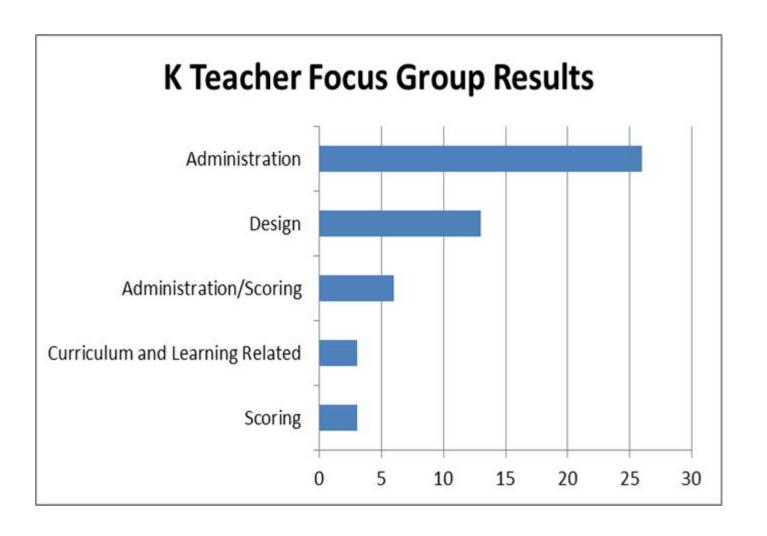


Usability!

Will teachers even use the assessments? What do we need to do to make them usable?

Buy-In for the eNumeracy
System by
Measuring
Usability

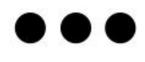


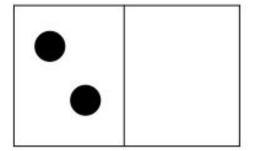


Version 1

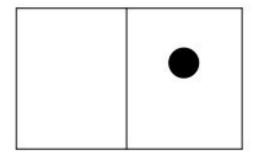
7 ...

Version 2

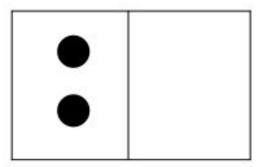








Version 3



Prepare	>	The DECOMPOSING NUMERALS demonstration item should be in front of the student.
Say	•	The number 4 [point] tells me how many dots altogether. I can only see 3 dots [point]. That means 1 dot goes here [point] because 3 [point] and 1 is 4 [point to the 4].
Do	>	Turn the page.

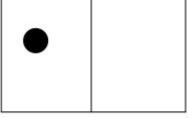
Demonstration Item



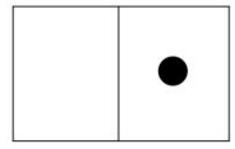


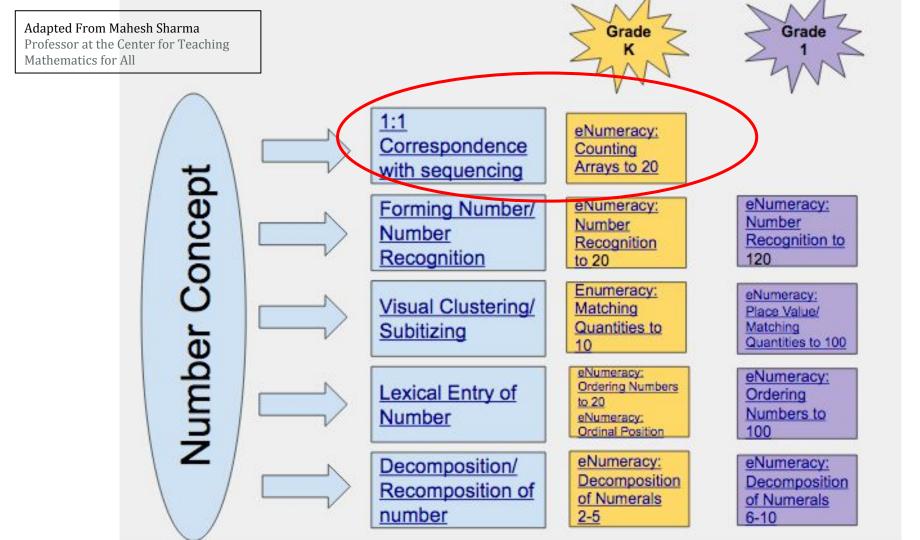
+			
1,64	Prepare	•	The DECOMPOSING NUMERALS practice item should be in front of the student.
	Say	>	Now it's your turn. How many dots go here? [point] Correct response: Correct. Let's try some more. Incorrect response: Look. There are 3 dots altogether [point]. 2 dots go here [point] because 1 and 2 is 3 [point]. Let's try some more.
	Do & Say	•	Start the timer then turn the page to the first test item. Say, What number goes here? [point]. You may use the prompt "What number goes here?" as many times as necessary.

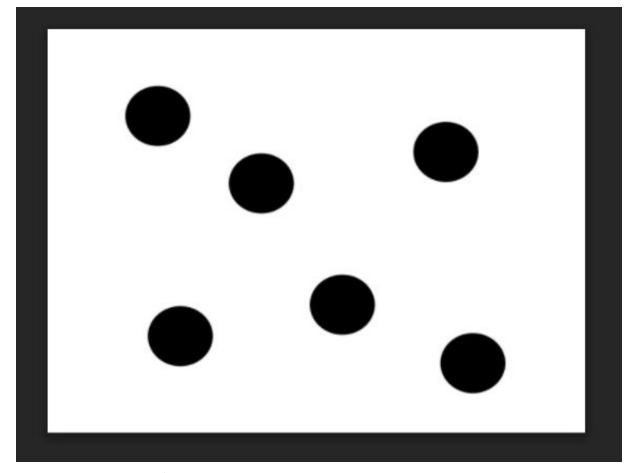
Practice Item



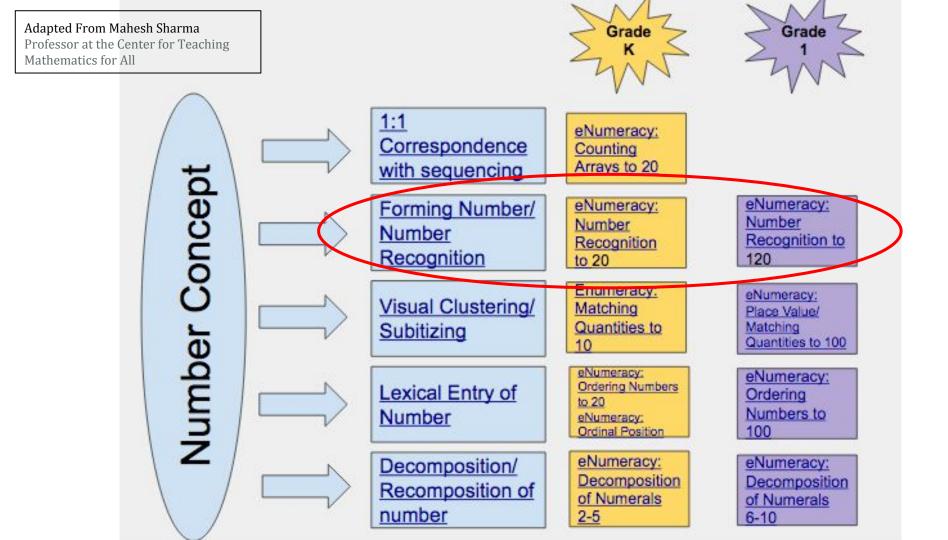
Version 4
FINAL







Grade K: Counting Arrays to 20

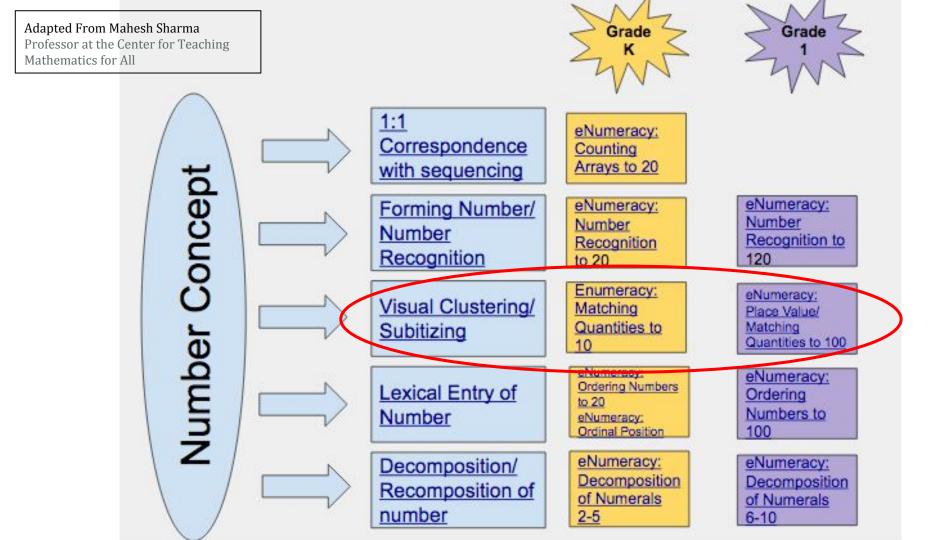


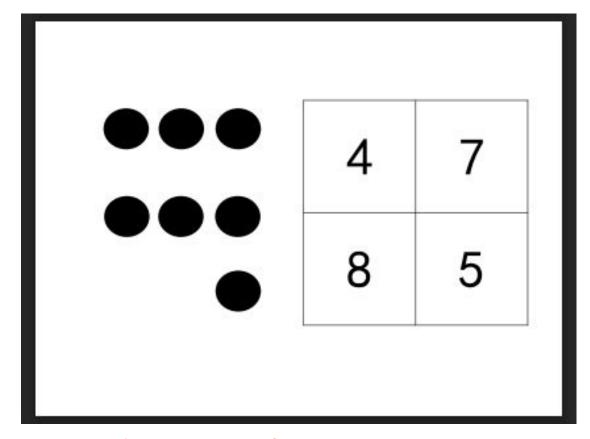
3	18	0	20	4
14	6	17	8	16
1	11	2	19	5
13	9	12	7	15
5	10	8	17	0

Grade K: Number Recognition 1 to 20

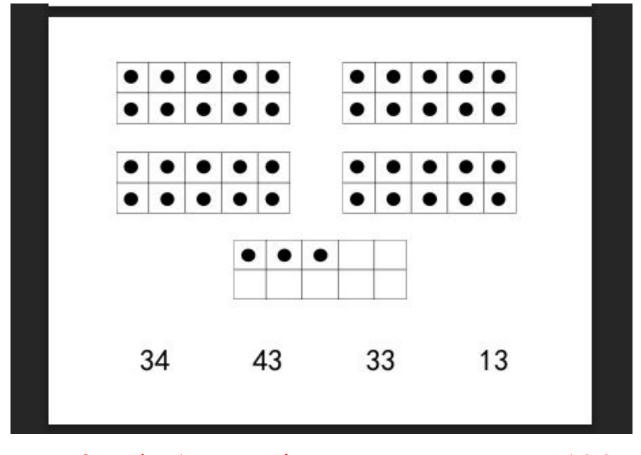
29	64	47	88	111
53	30	105	96	72
87	109	75	62	98
24	50	36	41	113
78	115	49	51	106

Grade 1: Number Recognition 1 to 120

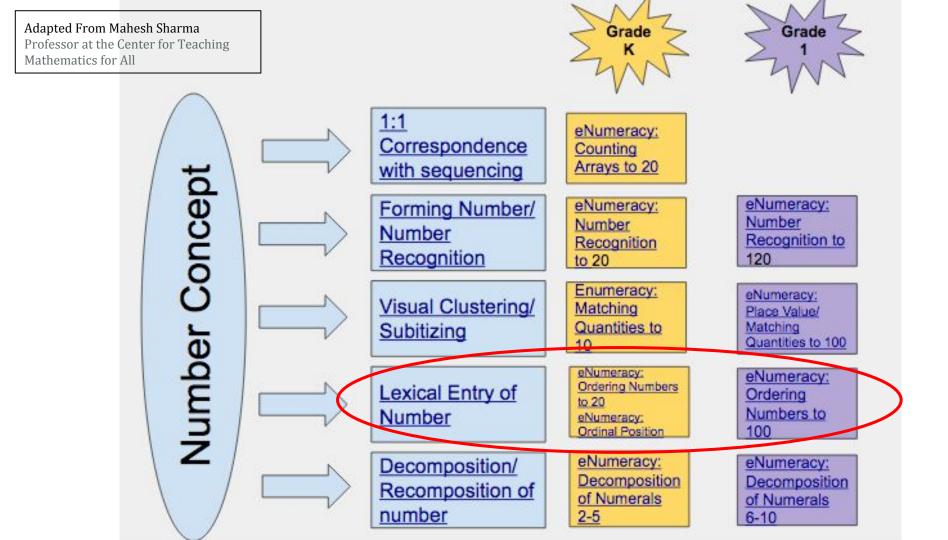


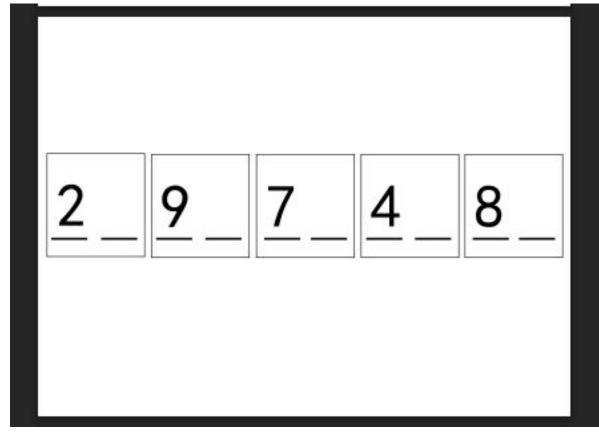


Grade K: Matching Quantities to 10 (Subitizing)

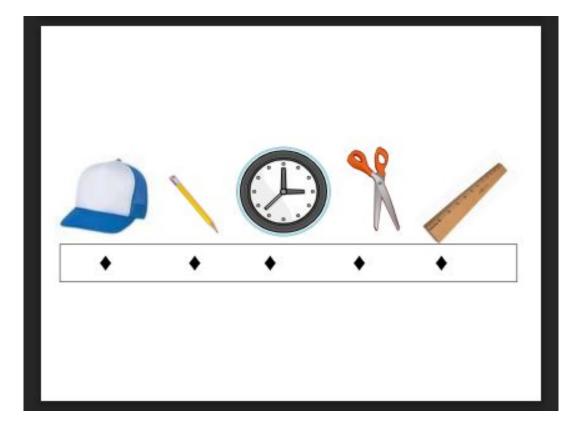


Grade 1: Matching Quantities to 100 Place Value

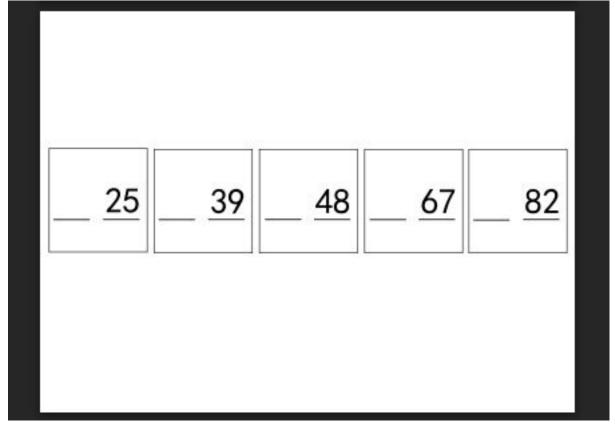




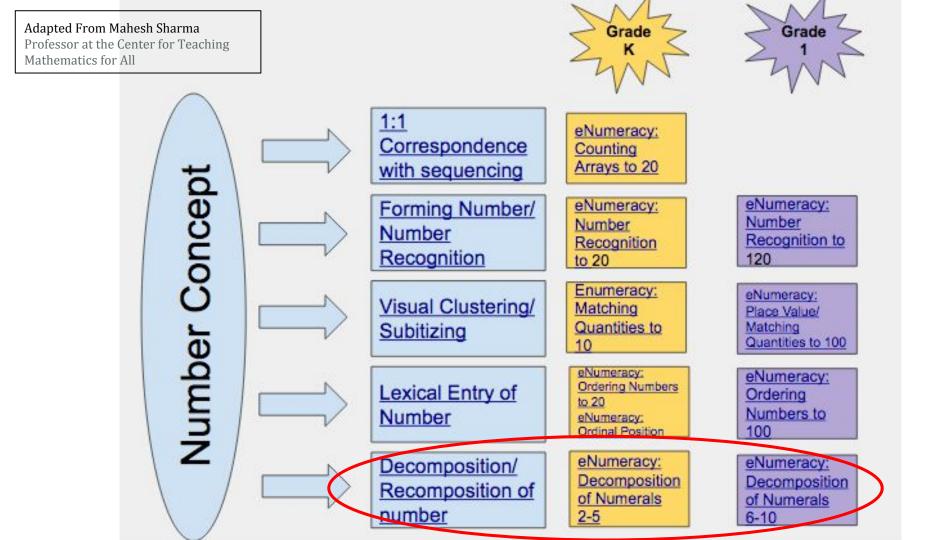
Grade K: Ordering Numbers to 20- # After (Lexical Entry of number)

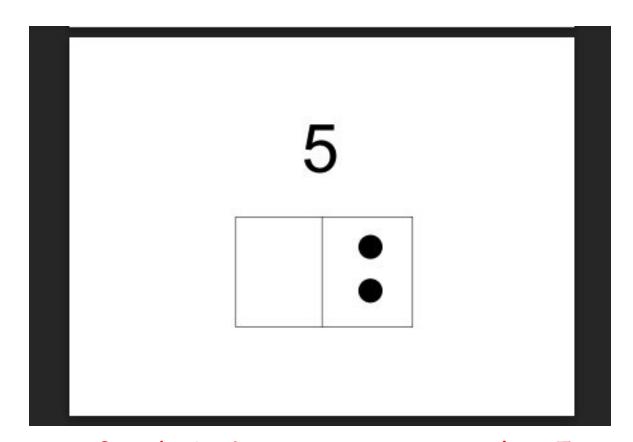


Grade K: Ordinal Position to 5 (Lexical Entry of number)

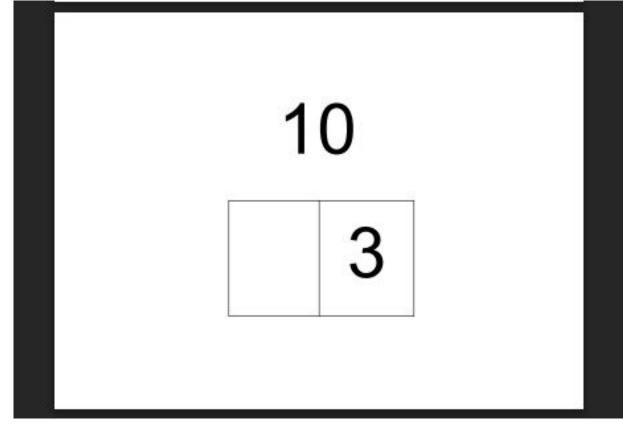


Grade 1: Ordering Numbers to 100-# Before (Lexical Entry of number)

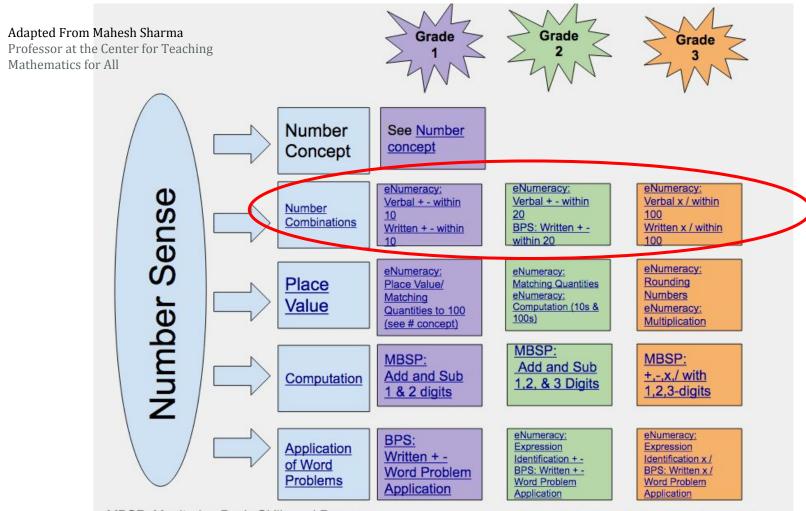




Grade K: Decomposition within 5



Grade 1: Decomposition within 10



MBSP: Monitoring Basic Skills and Progress

BPS: Burlington Public Schools created

Name:	uency Assessment on and Subtraction ombinations to 10			
9 - 7=	4 + 3=	10 - 9=	2 + 1=	4 - 4=
4 + 1=	7 + 3=	2 - 2=	1 + 3=	7 - 6=
4 + 6	7 <u>- 3</u>	3 + 3	8 <u>- 5</u>	5 <u>+ 2</u>
10 - 4=	2 + 3=	5 - 2=	1 + 7=	4 - 2=
2 + 2=	9 - 3=	9 + 1=	6 - 1=	10 - 10=
8 - 3	6 + 3	2 + 7	3 <u>+ 1</u>	6 <u>- 4</u>

Progress Monitoring - 1

Property of Burlington, MA Public Schools

Grade 1: Written Number Combinations within 10 (Addition & Subtraction)

EXAMINER SCORING SHEET - VERBAL ADDITION & SUBTRACTION (First Grade)

Student Name:	Date:	Examiner	Name:	
10.1				

If the student says the correct answer, circle the number. If the student says another number put an X through the item, and write in what s/he said.

HESITATION RULE: This is a fluid skill, so the HESITATION RULE is 3 seconds.

ITEM	QUESTION	CORRECT ANSWER		
HEM	VOLESTON	Addition	Subtraction	
1.	What is 4 plus 1?	5		
2.	What is 8 minus 5?		3	
3.	What is 2 plus 6?	8		
4.	What is 3 plus 5?	8		
5.	What is 5 plus 5?	10		
6.	What is 7 minus 6?		1	
7.	What is 5 minus 2?		3	
8.	What is 6 plus 3?	9		
9.	What is 9 minus 5?		4	
10.	What is 4 plus 4?	8		
11.	What is 10 minus 7?		3	
12.	What is 4 minus 4?		0	
13.	What is 6 minus 4?		2	
14.	What is 1 plus 6?	7		

TOTAL CORRECT	TOTAL TIME

Grade 1: Verbal Number Combinations within 10 (Addition & Subtraction)

Date: Burlington Public Schools Math Fluency Assessment Second Grade Addition and Subtraction Time: 1 minute Combinations to 20 8 - 3= 9 + 4= 12 - 6= 4 + 8= 16 - 9= 6 + 3= 7 - 6= 10 + 3= 7 + 5= 6 - 2= 17 11 - 8= 9 - 7= 1 + 8= 6 + 7= 13 - 9= 9 + 8= 11 - 10= 7 + 4= 12 - 5= 10 - 9= 10 + 10 + 10 12 - 8= 5 + 3= 10 - 5= 4+6= 16 - 6= 2 + 3= 12 - 9= 8 + 7= 8 - 2= 4 + 10=

Grade 2: Written Number Combinations within 20 (Addition & Subtraction)

EXAMINER SCORING SHEET - VERBAL ADDITION AND SUBTRACTION (Second Grade)

Student Name:	Date:	Examiner Name:	
(A.848) (A.648) (A.644)	20,000,000		

If the student says the correct answer, **circle the number**. If the student says another number **put** an X through the item, and write in what s/he said.

HESITATION RULE: This is a fluid skill, so the HESITATION RULE is 3 seconds.

ITEM	OUESTION	CORRECT ANSWER		
11 6.91	QUESTION	Addition	Subtraction	
1.	What is 2 plus 6?	8		
2.	What is 5 minus 2?		3	
3.	What is 8 plus 4?	12		
4.	What is 2 plus 4?	6		
5.	What is 7 plus 3?	10		
6.	What is 14 minus 7?		7	
7.	What is 11 minus 3?		8	
8.	What is 8 plus 8?	16		
9.	What is 11 minus 9?		2	
10.	What is 5 plus 8?	13		
11.	What is 9 minus 4?		5	
12.	What is 15 minus 9?		6	
13.	What is 12 minus 3?		9	
14.	What is 8 plus 6?	14		

TOTAL CORRECT _	TOTAL TIME

Grade 2: Verbal Number Combinations within 20 (Addition & Subtraction)

Name:		-	Multiplication	ey Assessment on and Division as within 100
5 × 5=	18 ÷ 3=	10 × 9=	16 ÷ 2=	64 ÷ 8=
8 × 6=	70 ÷ 7=	7 x 9=	9 × 10=	49 ÷ 7=
72 ÷ 8=	9 × 6=	12 ÷ 3=	3 × 6=	12 ÷ 6=
5 x 8=	45 ÷ 5=	8 × 8=	50 ÷ 5=	8 × 5=
21 ÷ 3=	4 × 5=	32 ÷ 8=	10 × 8=	14 ÷ 7=
6 x 6=	30 ÷ 10=	10 x 2=	2 x 5=	10 ÷ 5=
36 ÷ 6=	7 x 7=	4 × 3=	48 ÷ 8=	9 x 4=
4 × 4=	56 ÷ 8=	90 ÷ 10=	7 x 5=	18 ÷ 6=
36 ÷ 6= 4 × 4= 8 × 3=	24 ÷ 4=	8 x 9=	24 ÷ 6=	10 × 7=
72 ÷ 9=	3 × 5=	70 ÷ 10=	2 × 6=	24 ÷ 3=

Grade 3: Written Number Combinations within 100 (Multiplication & Division)

EXAMINER SCORING SHEET - VERBAL MULTIPLICATION AND DIVISION (Third Grade)

Student Name:	Date:	Examiner Name:	

If the student says the correct answer, circle the number. If the student says another number put an X through the item, and write in what s/he said.

HESITATION RULE: This is a fluid skill, so the HESITATION RULE is 3 seconds.

ITEM	QUESTION	CORRECT ANSWER	
HEN		Multiplication	Division
1.	What is 2 times 4?	8	
2.	What is 24 divided by 6?		4
3.	What is 5 times 5?	25	
4.	What is 15 divided by 3?		.5
5.	What is 7 times 9?	63	
6.	What is 8 divided by 2?		4
7.	What is 10 times 7?	70	
8.	What is 64 divided by 8?		8
9.	What is 9 times 3?	27	
10.	What is 6 times 8?	48	
11.	What is 72 divided by 9?		8
12.	What is 4 divided by 2?		2
13.	What is 6 times 7?	42	
14.	What is 40 divided by 10?		4

TOTAL CORRECT	TOTAL TIME	
---------------	------------	--

Grade 3: Verbal Number Combinations within 100 (Multiplication and Division)

	Public Schools e, Progress Monitoring nute	-4	Multipl	Fluency Assessment ication and Division binations within 144
6 × 5=	63 ÷ 9=	8 × 4=	108 ÷ 12=	18 ÷ 9=
7 x 7=	88 ÷ 8=	3 × 12=	10 × 9=	48 ÷ 8=
63 ÷ 7	7 × 11=	9 ÷ 3=	2 x 3=	35 ÷ 7=
11 × 5:	24 ÷ 6=	6 x 7=	121 ÷ 11=	9 × 4=
40 ÷ 5	6 × 11=	36 ÷ 4=	8 × 12=	48 ÷ 12=
7 × 8=	90 ÷ 10=	12 × 7=	6 × 12=	24 ÷ 4=
110 ÷ 1	0= 2 x 9=	9 × 9=	27 ÷ 9=	10 × 4=
110 ÷ 1 10 × 11	10 ÷ 5=	33 ÷ 3=	3 × 3=	108 ÷ 9=
7 x 2=	56 ÷ 7=	7 × 6=	16 ÷ 4=	11 × 2=
55 ÷ 5	= 3 x 12=	66 ÷ 11=	3 × 5=	32 ÷ 8=

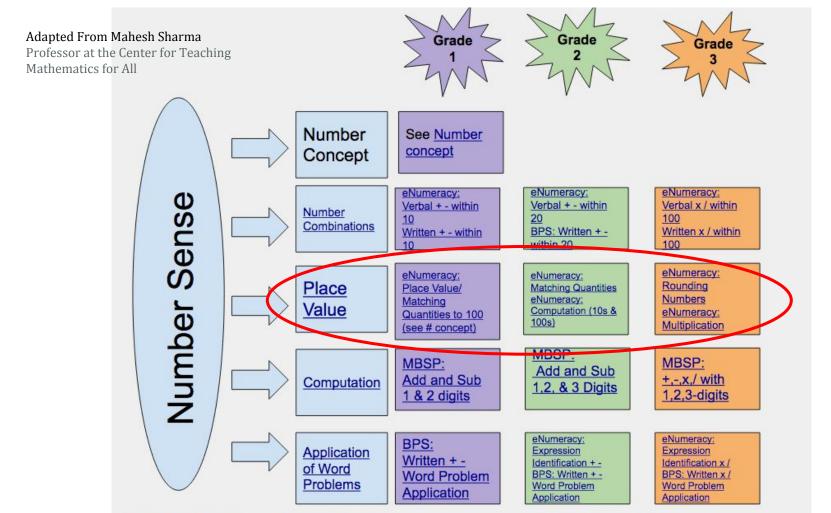
Grade 4: Written Number Combinations within 144 (Multiplication and Division)

Burlington Public Schools Math Fluency Assessment Fifth Grade Addition, Subtraction, Time: 1 minute Multiplication and Division 4 - 3= 9 x 10= 30 ÷ 6= 8 - 5= 6 + 3= 12 x 11= 4 + 6= 72 ÷ 8= 7 + 4= 16 - 7= 24 ÷ 3= 7 x 9= 15 - 10= 5 + 7= 56 ÷ 8= 9 x 4= 13 - 9= 9 + 8= 33 ÷ 3= 4 x 5= 17 - 8= 8 + 7= 55 ÷ 5= 12 - 9= 8 x 10= 9 + 3= 9 x 12= 60 ÷ 6= 9 x 7= 27 ÷ 9= 10 - 8= 7 + 7= 5 x 12= 72 ÷ 6= 10 + 2= 11 x 3= 9 - 5= 88 ÷ 11= 10 - 4= 6 + 5= 7 x 4= 110 ÷ 11= 2 + 8= 9 - 8= 7 x 11= 6 ÷ 3= 2 + 4= 6 x 8= 9 + 9= 9 - 4=

Progress Monitoring - 1

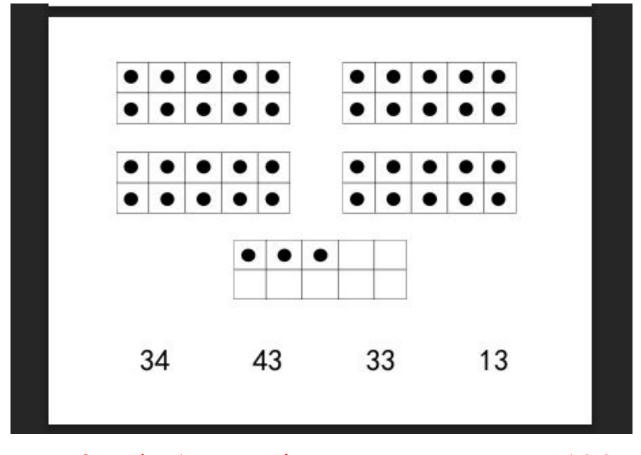
Property of Burlington, MA Public Schools

Grade 5: Written Number Combinations (All Operations)

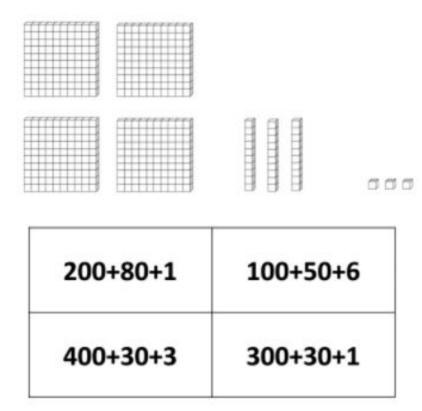


MBSP: Monitoring Basic Skills and Progress

BPS: Burlington Public Schools created



Grade 1: Matching Quantities to 100 Place Value



Grade 2: Matching Quantities (standard/expanded) (Place Value)

652 805 33 900 796

Grade 2: Computation 10s and 100s (more/less) (Place Value)

736 440 971 249 89

Grade 3: Rounding Numbers to 10s and 100s (Place Value)

$$5 \times 4 = 20$$

5 x 40 =

Grade 3: Multiplication (Place Value)

Adapted From Mahesh Sharma Grade Grade Grade Professor at the Center for Teaching Mathematics for All Number See Number concept Concept eNumeracy: eNumeracy: eNumeracy: Sense Verbal + - within Verbal + - within Verbal x / within Number 100 Combinations BPS: Written + -Written x / within Written + - within within 20 100 eNumeracy: eNumeracy: eNumeracy: Place Rounding Matching Quantities Place Value/ eNumeracy: Numbers Matching Number Value Computation (10s & eNumeracy: Quantities to 100 100s) Multiplication (see # concept) MBSP: MBSP: MBSP: Add and Sub Add and Sub +,-,x,/ with Computation 1,2, & 3 Digits 1 & 2 digits 1,2,3-digits eNumeracy: enumeracy: BPS: Expression Application Expression Written + -Identification + -Identification x / of Word

Word Problem

Application

MBSP: Monitoring Basic Skills and Progress

Problems

BPS: Burlington Public Schools created

BPS: Written x /

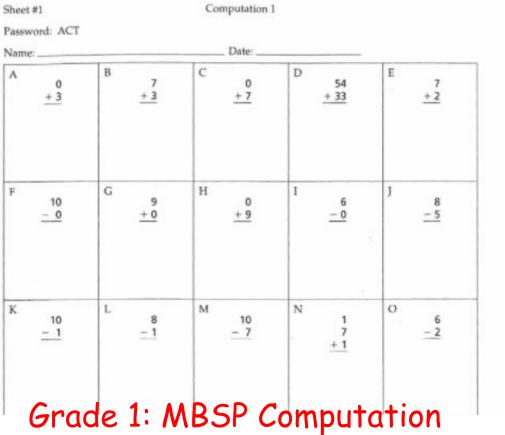
Word Problem

Application

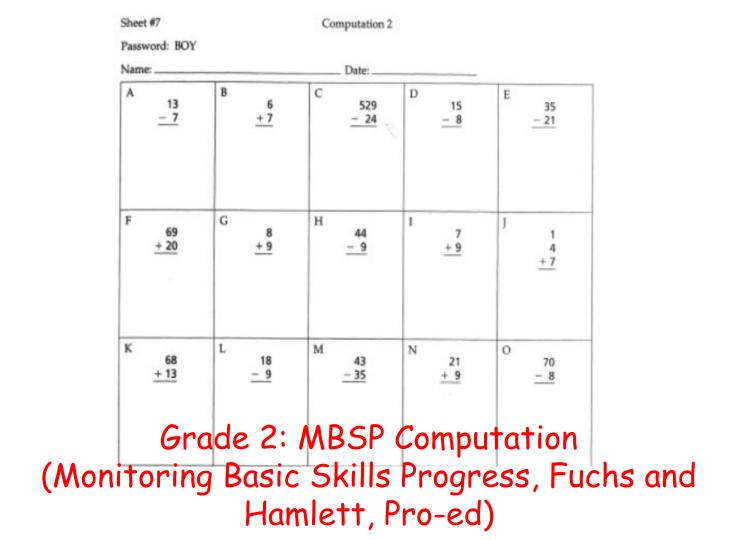
BPS: Written + -

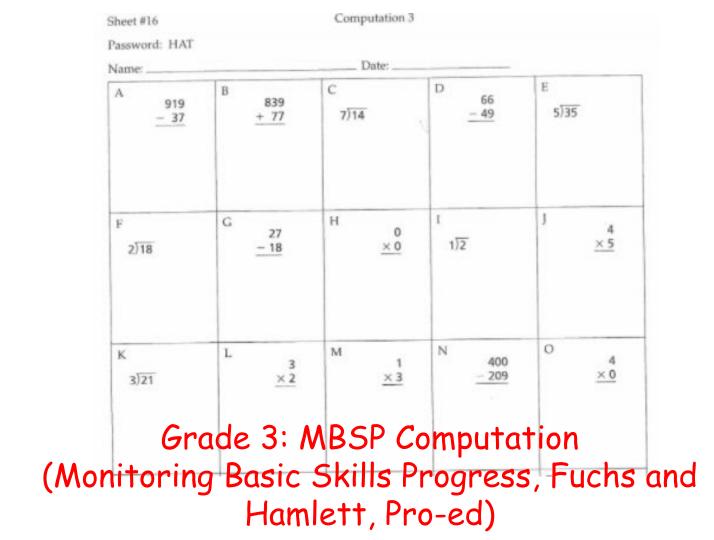
Word Problem

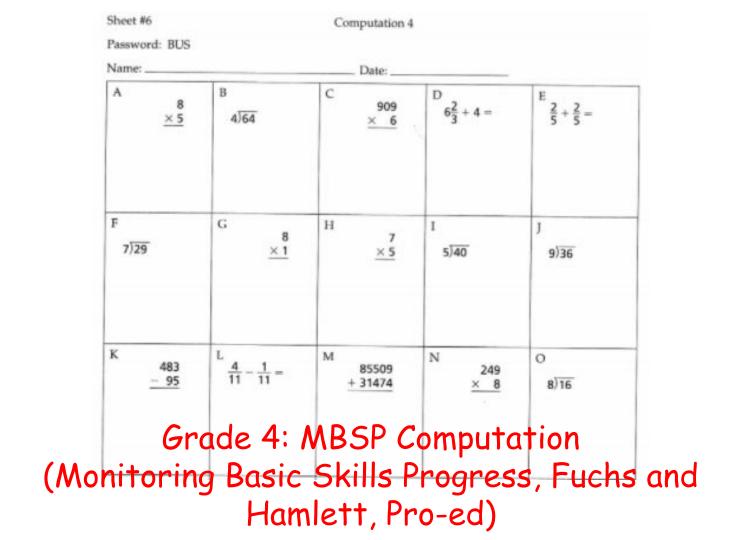
Application

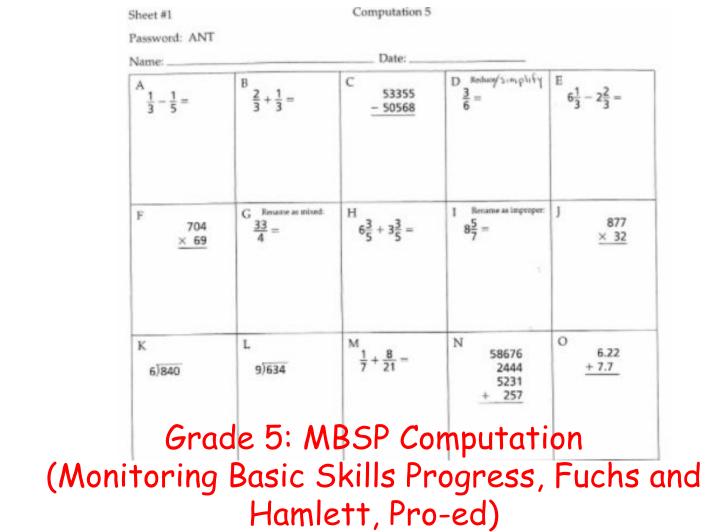


(Monitoring Basic Skills Progress, Fuchs and Hamlett, Pro-ed)



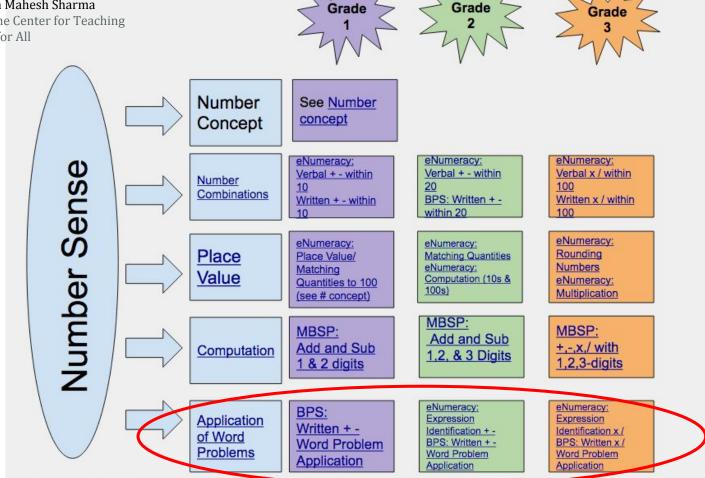






Adapted From Mahesh Sharma

Professor at the Center for Teaching Mathematics for All



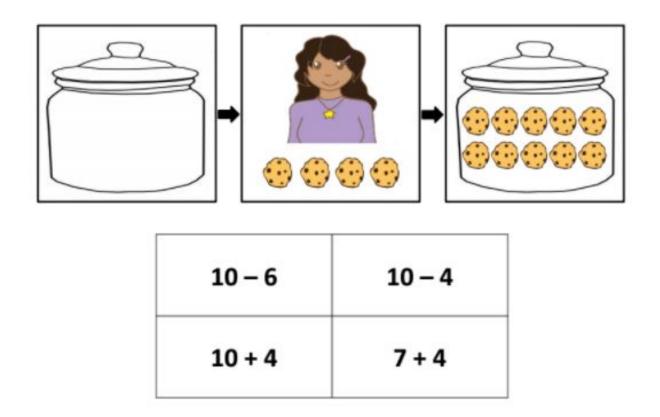
MBSP: Monitoring Basic Skills and Progress

BPS: Burlington Public Schools created

2.)	Some students took the bus to go home.
	At the first stop, 5 students got off.
	Now there are 3 students on the bus.
	How many students were on the bus in the beginning?
Num	ber Sentence:
	ver:

(Addition and Subtraction)

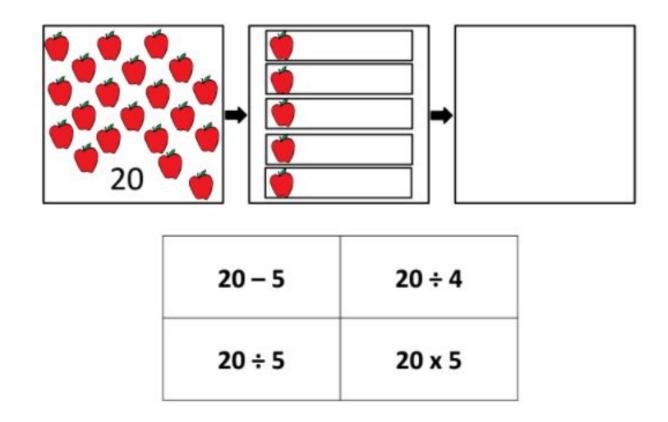
3.)	Juanita is 12 years old.
	Juanita has 15 more pencils than markers.
	She has 49 pencils.
	How many markers does she have?
Nun	ber Sentence:
Ans	ver:
C	
Grac	le 2: Written Word Problem Application
	(Addition and Subtraction)



Grade 2: Expression ID Word Problem Application (Addition and Subtraction)

An elastic is 8 inches long.	
It is stretched to be 3 times as long.	
How long is the elastic now?	
ber Sentence:	_
ver:	
	It is stretched to be 3 times as long. How long is the elastic now? ber Sentence:

Grade 3: Written Word Problem Application (Multiplication and Division)



Grade 3: Expression ID Word Problem Application (Multiplication and Division)

1.)	The 4th graders are going on a field trip.
	There are 25 students in each class.
	9 students can fit into a van.
	How many vans are needed for 75 students?
	ition:

Grade 4: Written Word Problem Application (Multiplication and Division)

7.)	Three jars are being used to collect rainwater.
	The jars have 17 fluid ounces, 21 fluid ounces, and 25 fluid ounces.
	If the total amount of water was redistributed equally between the 3 jars,
	how many fluid ounces would be in each jar?
-	
Equ	ations:
Ans	wer:

Grade 5: Written Word Problem Application (Multiplication and Division)



Decomposing Numerals : Scoring Sheet

EXAMINER SCORING SHEET - DECOMPOSING NUMERALS (Kindergarten)

	ATION RULE: This is a fluid skill, so the HESITATION F	RULE is 3 seconds.
ПЕМ	HESITATION PROMPT	CORRECT ANSWER
1.	Point to the box and say, How many dots go here? (4)	(2)
2.	Point to the box and say, How many dots go here? (5)	*
3.	Point to the box and say, How many dots go here? (2)	(I)
4.	Point to the box and say, How many dots go here? (4)	(3)
5.	Point to the box and say, How many dots go here? (3)	(2)
6.	Point to the box and say, How many dots go here? (3)	(1)
7.	Point to the box and say, How many dots go here? (5)	(0)
8.	Point to the box and say, How many dots go here? (5)	(4)



ITEM	HESITATION PROMPT	CORRECT ANSWER
1.	Point to the box and say, How many dots go here? (4)	@
2.	Point to the box and say, How many dots go here? (5)	×HH
3.	Point to the box and say, How many dots go here? (2)	0
4.	Point to the box and say, How many dots go here? (4)	×4
5.	Point to the box and say, How many dots go here? (5)	XHV
6.	Point to the box and say, How many dots go here? (3)	(1)
7.	Point to the box and say. How many dots go here? (5)	* 5
8.	Point to the box and say, How many dots go here? (5)	X U.

CORRECT NUMERALS DECOMPOSED 3 TOTAL TIME 49 Sec

To Calculate Accuracy:

Total Correct ÷ Total Items X 100= % Correct (Accuracy)

$$3 \div 8 \times 100 = 37.5 \%$$

38% Accuracy

To Calculate Fluency:

RPM= Rate per minute

Total Correct ÷ Total time in seconds X 60 = RPM (Fluency)

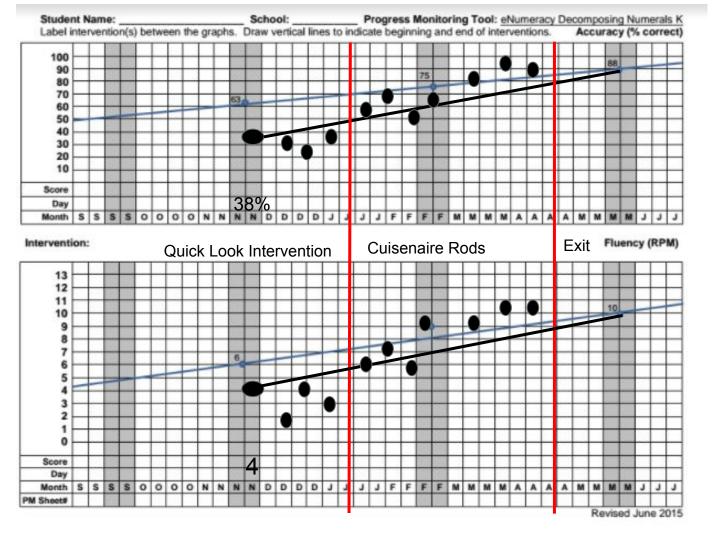
$$3 \div 49 \times 60 = 3.67$$

4 RPM

ITEM	HESITATION PROMPT	CORRECT ANSWER
1.	Point to the box and say, How many dots go here? (4)	@
2.	Point to the box and say, How many dots go here? (5)	×нч
3.	Point to the box and say, How many dots go here? (2)	0
4.	Point to the box and say, How many dots go here? (4)	×4
5.	Point to the box and say, How many dots go here? (5)	XHV
6.	Point to the box and say, How many dots go here? (3)	(1)
7.	Point to the box and say. How many dots go here? (5)	× 5
8.	Point to the box and say, How many dots go here? (5)	XHV

CORRECT NUMERALS DECOMPOSED 3

TOTAL TIME 49 Sec



www.bpsenumeracy.wordpress.com

Burlington Public Schools

Massachusetts

2017



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