# **NCTM Annual Meeting and Exposition 2017**

April 5 - 8, 2017

San Antonio, Texas

# Session 474 Using the Desmos Calculator to Analyze Student Photographs and Pictures

Friday, April 7, 2017

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# http://www.corestandards.org/Math/Practice/

### MP1 Make sense of problems and persevere in solving them:

\*how you could express the problem with equations, diagrams, or graphs.

### MP4 Model with mathematics:

\*express data and relationships in the problem with tables, graphs, diagrams, or equations, and check your result to see if it makes sense.

# MP5 Use appropriate tools strategically:

\*decide which tools are most helpful for solving the problem and why.

### MP6 Attend to precision:

\*think carefully about the required accuracy of results; is a number estimate or geometric sketch good enough, or is a precise value or drawing needed?

# **Skills Available for Common Core**

### **Sixth-Grade Math Standards**

https://www.ixl.com/standards/common-core/math

### 6.RP Ratios and Proportional Relationships

6.RP.A.3 Use ratio and rate reasoning to solve real-world and mathematical problems, e.g., by reasoning about tables of equivalent ratios, tape diagrams, double number line diagrams, or equations.

6.RP.A.3a Make tables of equivalent ratios relating quantities with whole-number measurements, find missing values in the tables, and plot the pairs of values on the coordinate plane. Use tables to compare ratios.

### 6.NS The Number System

6.NS.C.6b Understand signs of numbers in ordered pairs as indicating locations in quadrants of the coordinate plane; recognize that when two ordered pairs differ only by signs, the locations of the points are related by reflections across one or both axes.

6.NS.C.6c Find and position integers and other rational numbers on a horizontal or vertical number line diagram; find and position pairs of integers and other rational numbers on a coordinate plane.

### 6.EE Expressions and Equations

6.EE.C Represent and analyze quantitative relationships between dependent and independent variables.

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6.EE.C.9 Use variables to represent two quantities in a real-world problem that change in relationship to one another; write an equation to express one quantity, thought of as the dependent variable, in terms of the other quantity, thought of as the independent variable. Analyze the relationship between the dependent and independent variables using graphs and tables, and relate these to the equation.

### **Seventh-Grade Math Standards**

### 7.RP Ratios and Proportional Relationships

7.RP.A.2 Recognize and represent proportional relationships between quantities.

7.RP.A.2a Decide whether two quantities are in a proportional relationship, e.g., by testing for equivalent ratios in a table or graphing on a coordinate plane and observing whether the graph is a straight line through the origin.

7.RP.A.2b Identify the constant of proportionality (unit rate) in tables, graphs, equations, diagrams, and verbal descriptions of proportional relationships.

7.RP.A.2c Represent proportional relationships by equations.

7.RP.A.2d Explain what a point (x, y) on the graph of a proportional relationship means in terms of the situation, with special attention to the points (0, 0) and (1, r) where r is the unit rate.

### **Eighth-Grade Math Standards**

### 8.EE Expressions and Equations

8.EE.B Understand the connections between proportional relationships, lines, and linear equations.

8.EE.B.5 Graph proportional relationships, interpreting the unit rate as the slope of the graph. Compare two different proportional relationships represented in different ways.

8.EE.B.6 Use similar triangles to explain why the slope m is the same between any two distinct points on a non-vertical line in the coordinate plane; derive the equation y = mx for a line through the origin and the equation y = mx + b for a line intercepting the vertical axis at b.

### 8.F Functions

8.F.A Define, evaluate, and compare functions.

8.F.A.1 Understand that a function is a rule that assigns to each input exactly one output. The graph of a function is the set of ordered pairs consisting of an input and the corresponding output.

8.F.A.2 Compare properties of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions).

8.F.A.3 Interpret the equation y = mx + b as defining a linear function, whose graph is a straight line; give examples of functions that are not linear.

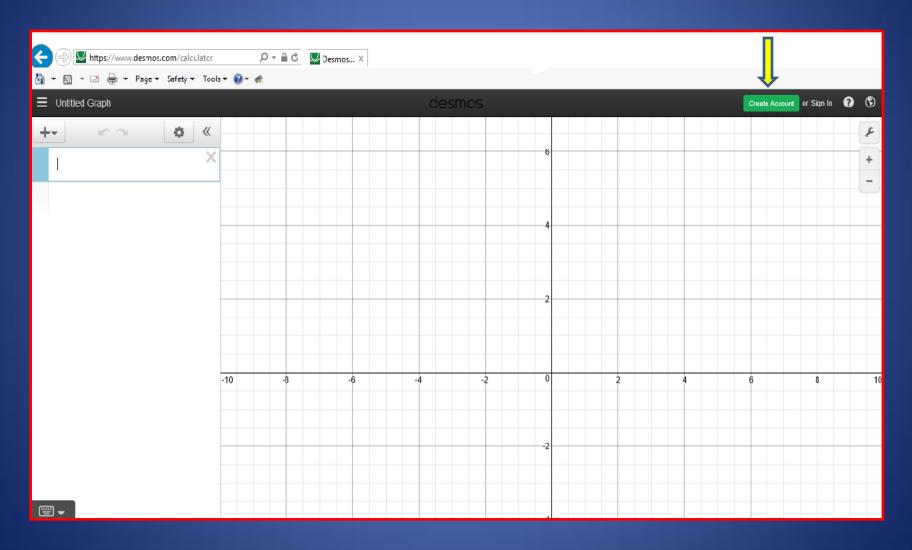
8.F.B Use functions to model relationships between quantities.

8.F.B.4 Construct a function to model a linear relationship between two quantities. Determine the rate of change and initial value of the function from a description of a relationship or from two (x, y) values, including reading these from a table or from a graph. Interpret the rate of change and initial value of a linear function in terms of the situation it models, and in terms of its graph or a table of values.

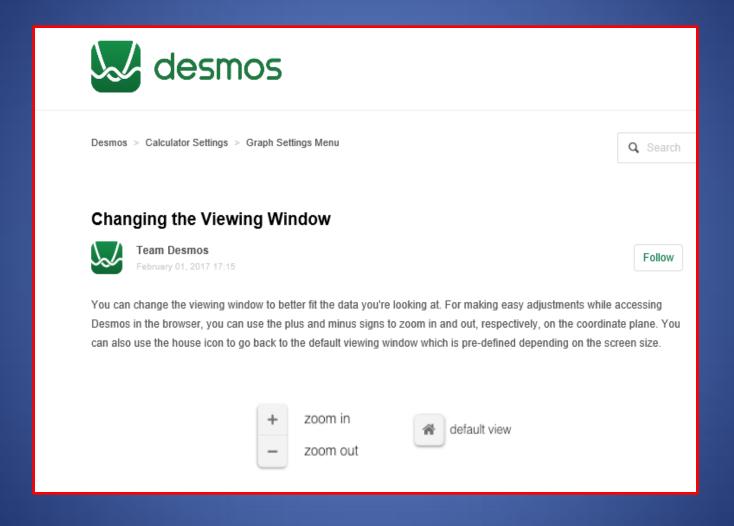
8.F.B.5 Describe qualitatively the functional relationship between two quantities by analyzing a graph (e.g., where the function is increasing or decreasing, linear or nonlinear). Sketch a graph that exhibits the qualitative features of a function that has been described verbally.

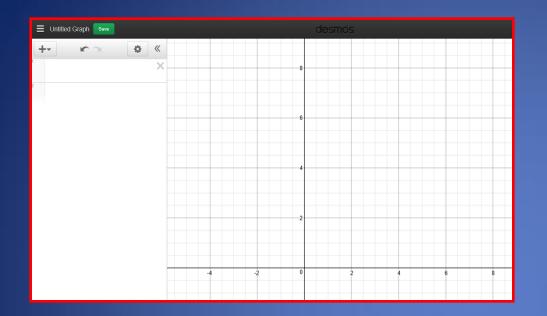
# https://www.desmos.com/calculator

Be sure to create an account as soon as you access the calculator!



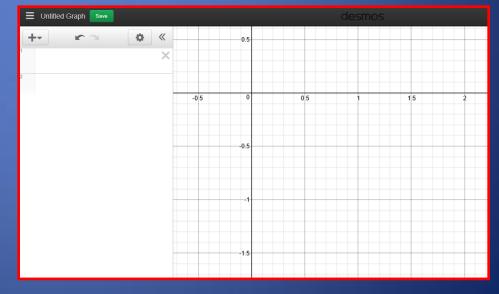
# http://support.desmos.com/hc/en-us/articles/209686513-Changing-the-Viewing-Window





You can drag the coordinate axes to other locations.

You can also change the increments on the axes by zooming in or out.





Press the "ABC" key and another keyboard will pop up. This one has the braces (restricted domains/ranges) and the symbol for "is approximately" (line of best fit.) Students will need both of these for writing equations.



Date_		_Period
he Desmos Graphin	Calculator – A	ctivity 1
os://www.desmos.com	/calculator	
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ccount at this time.)		
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umber as the stope	what is the chang	ge in the y values as x
box, type in $y = 2x$ ; as oh and then compare i		ld appear. Describe the
		ut of the denominator!)
cs of that graph and co	mpare it to the oth	hers.
es of mat graph and co		are it to die ou

	For your fourth equation, type in $y = -x$ ; what has happened? Describe the characteristics:
(5)	Now type in $y = -3x$ ; what are the characteristics of this graph?
	The last equation is $y = -1/2x$ (don't forget to "click out" of the denominator); describe the characteristics of this graph:
	: y = mx + b (Be sure to delete the previous graphs in Part 1 first!)  Graph y = 2x + 3; describe the graph:
(2)	Graph $y = 2x - 1$ ; describe this graph and compare it to the one in ex. (1).

What wer	e the y interce	pts?			
Graph y =	-2x + 3; descri	ibe the graph ar	d compare it to	ex. (1).	
	partner(s), wri		nations in the fo	rm y = mx + b a	nd describe
grapiis (co.	npare/contrast				
d: y = b (De	lete all the eq	uations from P	art 2)		
	_	uations from P y = -6, and y =		e characteristic	s of these
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(1) Graph	_			e characteristic	s of these
(1) Graph	_			e characteristic	s of these
(1) Graph; graphs:	y = 5, y = 2.5,	y = -6, and y =	-1/2; describe th	e characteristic	
(1) Graph graphs:	y = 5, y = 2.5,	y = -6, and y =	1/2; describe the		
(1) Graph graphs:	y = 5, y = 2.5, y wo more equate. List them and	y = -6, and y =	1/2; describe the		a positive

Part 4: Optional Graphs: you may graph the following equations and observe what the graphs look like. Describe their characteristics on the lines below. (Delete all the equations from Part 3)

(1)	y =	$\mathbf{x}^2$
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(2) 
$$y = x^2 + 2$$

(3) 
$$y = x^2 - 5$$

(4) 
$$y = -x^2$$

(5) 
$$y = -x^2 + 2$$

(6) 
$$y = -x^2 - 5$$

(7) 
$$y = 2x^2$$

(8)	<b>Y</b> :	= .	2	$\mathbf{x}^2$
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### Working With The Desmos Graphing Calculator - Activity 2

### https://www.desmos.com/calculator

Today, you will be working with "sliders". These allow you to change the parameters of an equation so you can see the animations as the values increase and decrease.

(You should create an Account at this time if you haven't already done so. When you make interesting and creative graphs, be sure to SAVE them with a title. Then you can do a screenshot and send it to Mrs. Cooperman via email!)

- (1) In the rectangular box on the left, type in y = mx; you should see a graph that is a straight line passing through (0,0).
- (2)A "slider" graphic will suddenly appear and you will be asked if you would like to add one for "m". (Yes!) The "slider" is the constant multiplier (the coefficient of x) and is represented by the "m".
- (3) You can move the slider back and forth, changing the multiplier from negative to positive values. Each time you move the slider, the graph changes on the coordinate plane.

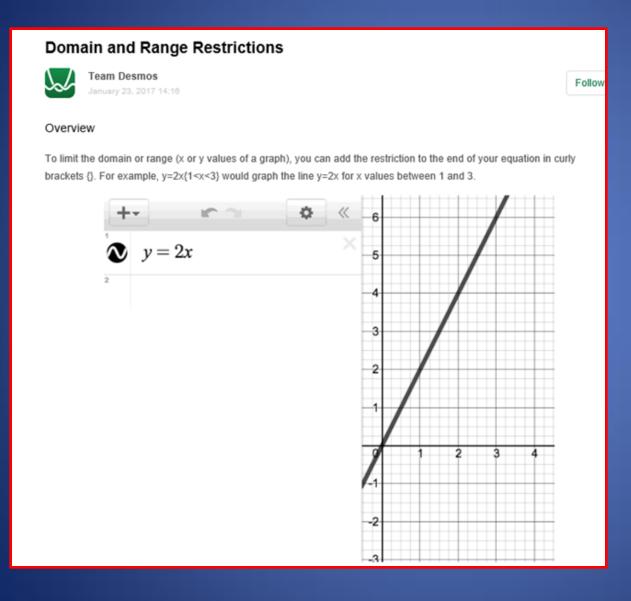
(4)Describe w negative m	The state of the s	h the graphs; be v	very specific about	the positive, zero, and
-				

(5) Type in this equation, type in y = 5; another slider graphic will appear. What kind of lines

are you working with now?

	For your next equation, type in $y = 2x + b$ ; what has happened? Now describe the characteristics of these graphs:
	What do you think will happen if you change the 2 to -2? (You will have to eliminate 2x +b first otherwise the slider won't appear.)
)	The next equation is $y = mx + 4$ ; describe the characteristics of this graph:
1 1	Suppose you changed the equation to $y = mx - 2$ ; (be sure to eliminate all the other
•	equations first otherwise the slider won't appear!) What happens?

# http://support.desmos.com/hc/en-us/articles/202528949-Domain-and-Range-Restrictions



Remember when we were looking at the second keyboard on the **Desmos graph? Students will** need the braces in order to restrict the domains and ranges of the lines outlining the objects in their photos.

### **Domain and Range Restrictions**



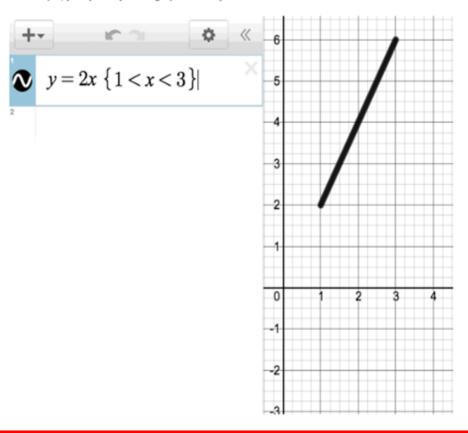
### Team Desmos

January 23, 2017 14:16

Follow

### Overview

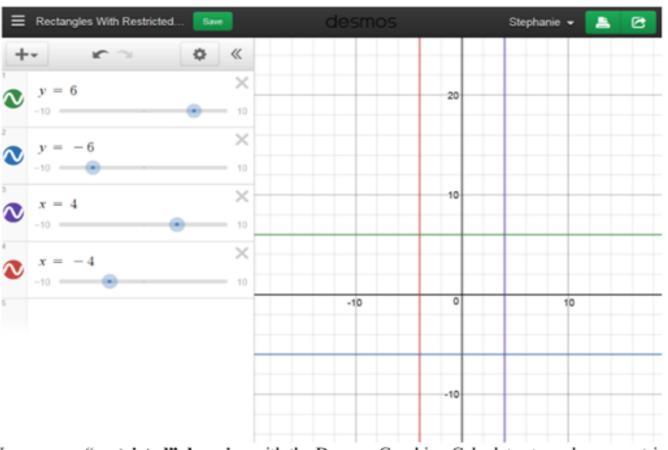
To limit the domain or range (x or y values of a graph), you can add the restriction to the end of your equation in curly brackets {}. For example, y=2x{1<x<3} would graph the line y=2x for x values between 1 and 3.



**Students will** need to adjust their lines so that segments outline the various shapes in their photographs. This can be done by restricting the domain and range of the equation.

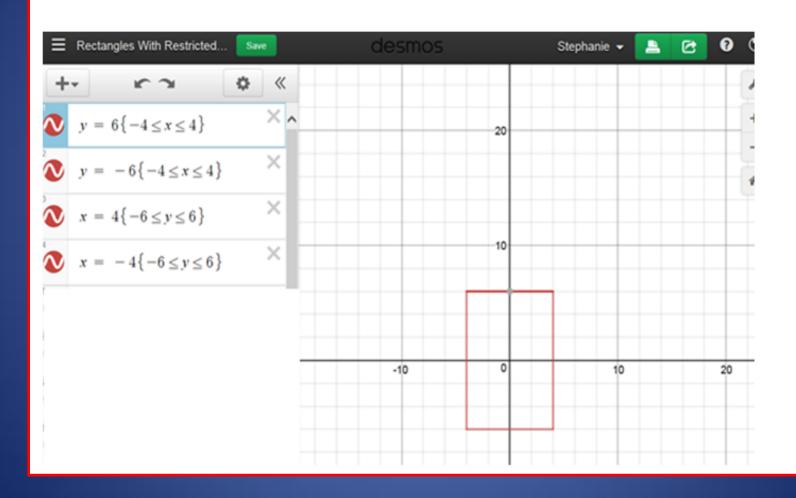
# **Desmos Graphing Calculator Activity 3**

### Making a Rectangle Using Restricted Domains

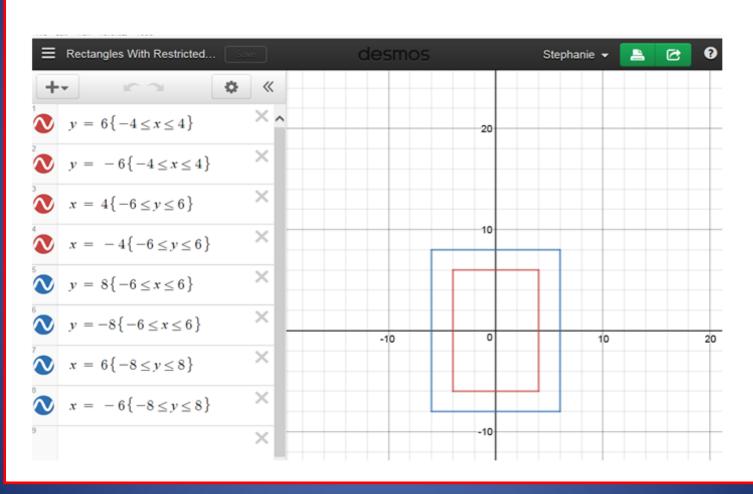


You can use "restricted" domains with the Desmos Graphing Calculator to make geometric shapes from linear graphs. We will also be using vertical and horizontal lines to make the sides.

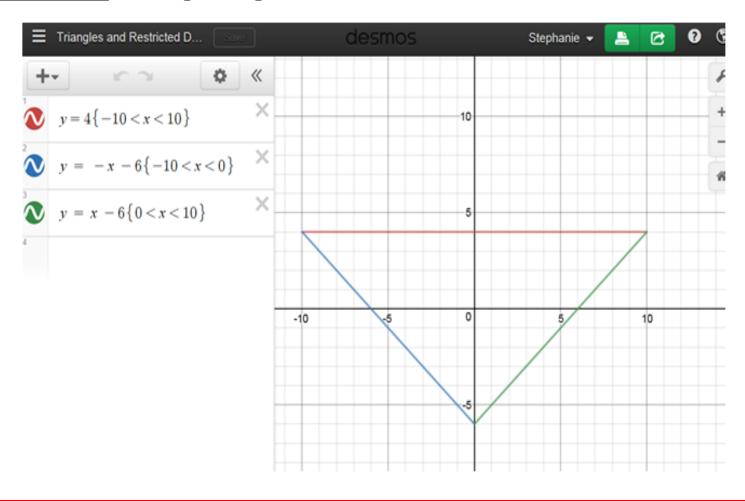
We're going to add the braces with the restrictions for x and y <u>next</u> to the original equations: **Be** sure to include the braces <u>before</u> and <u>after</u> the values for x and y. (You can make all the sides red.)



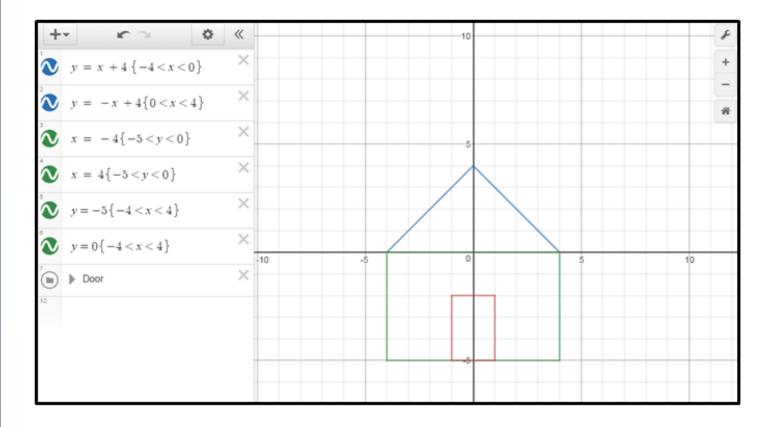
Let's put another rectangle around the first one. Look at the four new equations that determine the blue rectangle. (Each side of the larger rectangle was originally in four different colors. Change all of those sides to the color blue.)



# Extra Practice: Making a triangle with restricted domains on x.



### Using the <u>Desmos</u> Graphing Calculator to Make a House



When I open the folder called "Door"; all the equations that form the door are listed inside that folder! Using folders helps to save space on the equation column.

# http://support.desmos.com/hc/en-us/articles/208156426-Adding-to-the-Graph-Add-Item-Menu-

Follow

### Adding to the Graph (Add Item Menu)

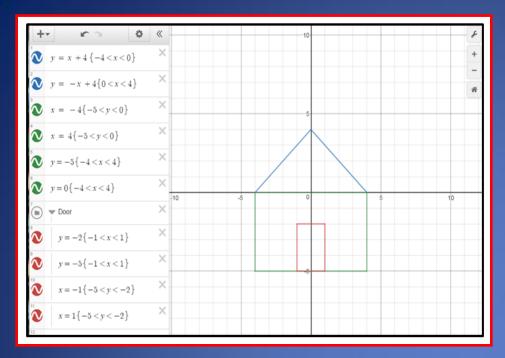


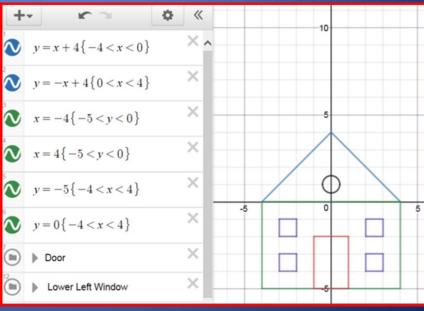
You can use the **Add Item** menu to add an expression, note, table, folder, or image to your graph. To start, click on the "plus sign" and then choose the type of item you'd like to add to your graph. An example of each is below:

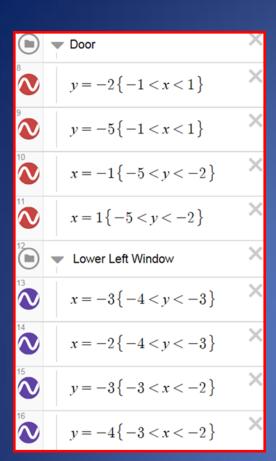


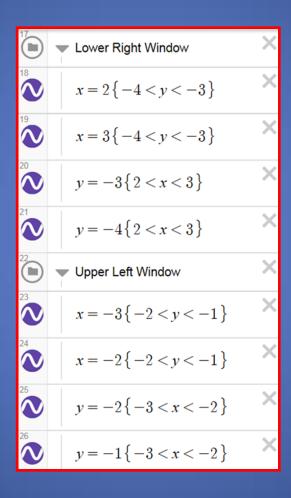


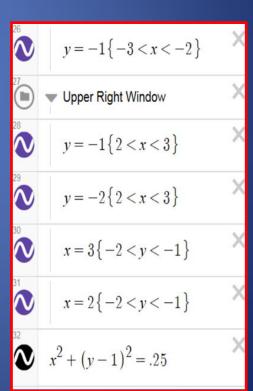
The "+" icon at the upper left of your graph add a note, an expression, a table, a folder, or an image. (We're getting closer and closer to the **Photography** Project!)











Note: Use the +key to add a folder which you'll need to title. After you write your equations, you can click on the white area around the colored icons of each equation and drag them on top of the folder. If it went into the folder properly, you'll see a light gray line on the left of the equation. Click on the folder to close it and all your equations will disappear from the column. Click on the folder to open it and all your equations will be listed again underneath!

You can make a folder for each window: two above the door and two more next to the door on each side.

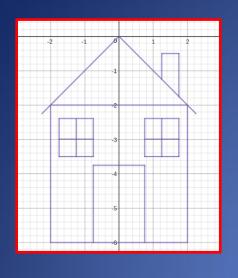
How about a chimney? Is the fireplace going?

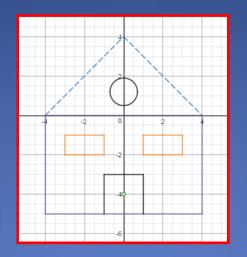
A nice green lawn? Or is it snow-covered?

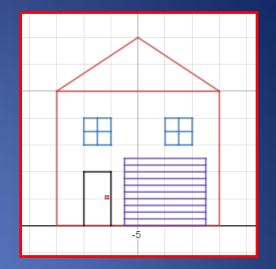
How about a picket fence?

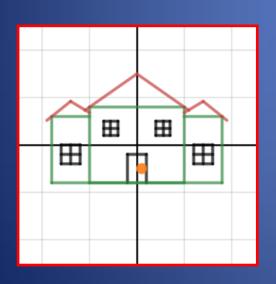
# **Saving Screen Shots On Your Chrome Book**

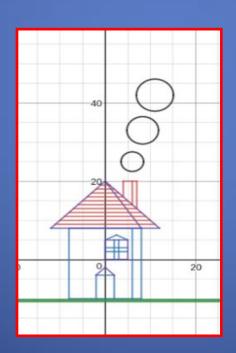
- 1. Press Ctrl + Switch Window; the screenshot will be taken.
- 2. When the popup says "screenshot taken", click on it;
- 3. Then, drag to "My Drive" on the left.
- 4. Go to Google Drive:
- 5. Click "Make a Folder"; name it "Desmos".
- 6. Go to "Recent" and then click on the screenshot(s).
- 7. Click the three dots and click "Move to":
- 8. Move it to the folder, "Desmos".

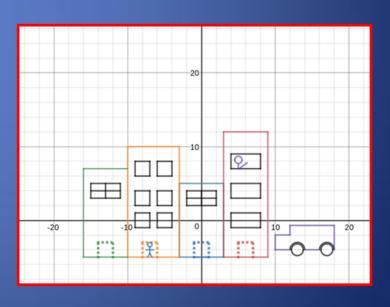


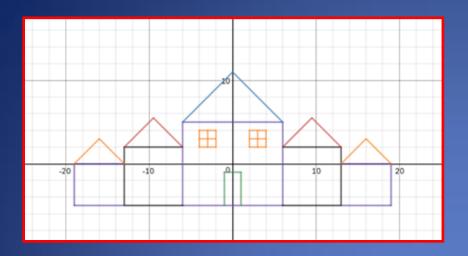


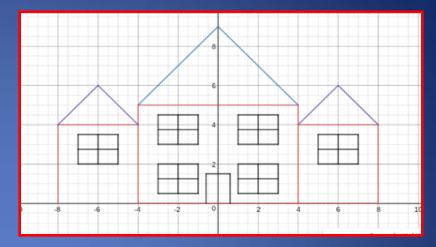


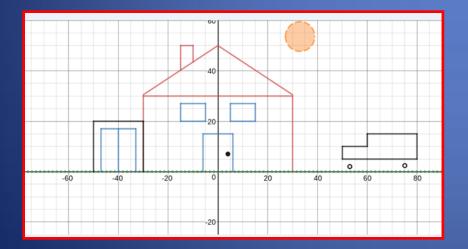


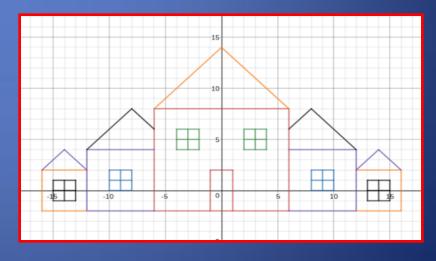


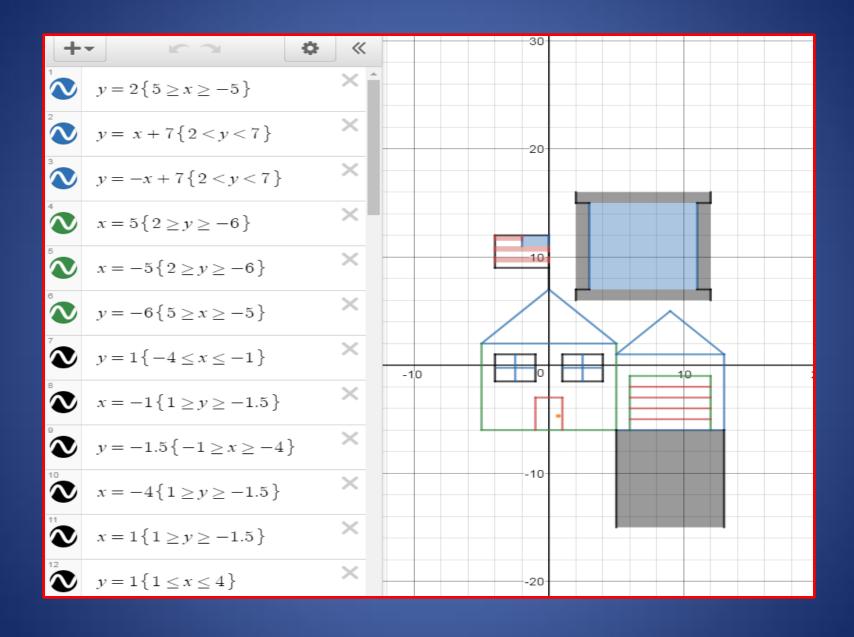


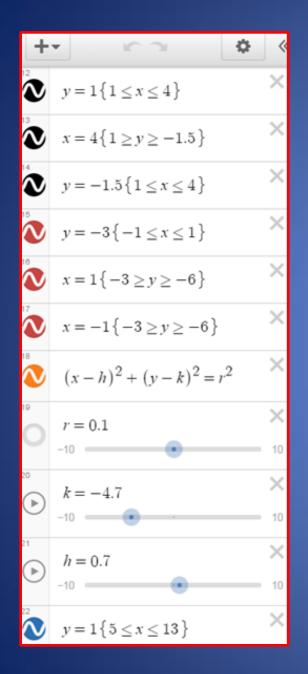






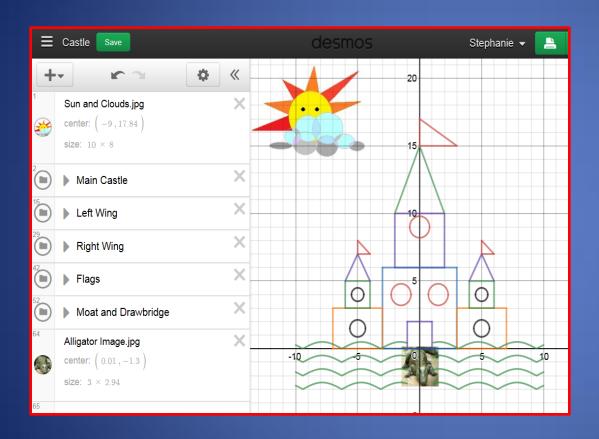


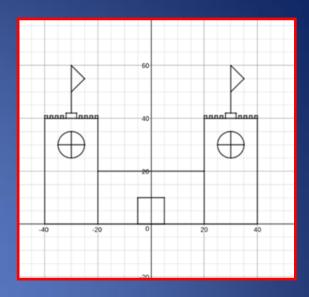


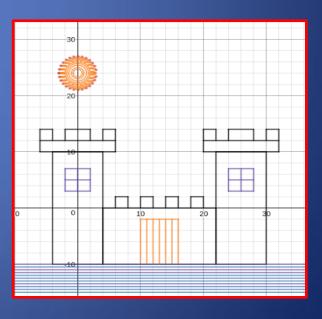












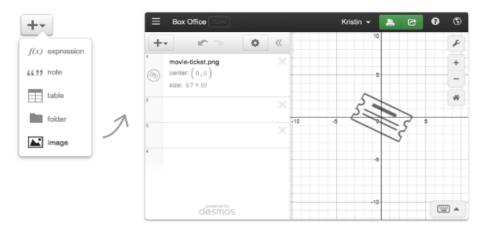
### http://support.desmos.com/hc/en-us/articles/203291245-Add-Image-to-Graph

#### Add Image to Graph

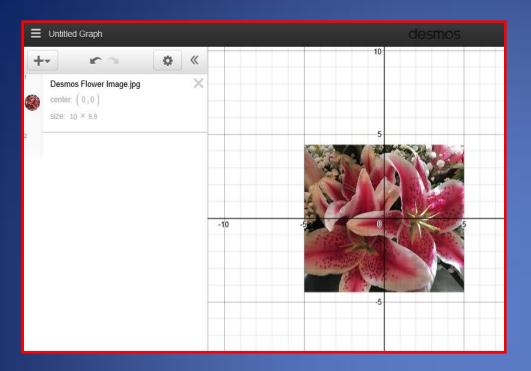


Follow

Add images to your graph to use as a template for your graph, add text labels, or for a little pop of extra color! To add an image to your graph, start by opening the Add Item menu and choose Image. Clicking and dragging the image into the expression list is also supported in many browsers.

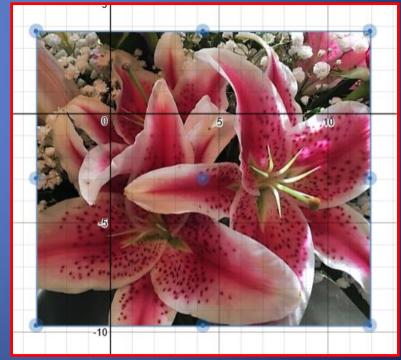


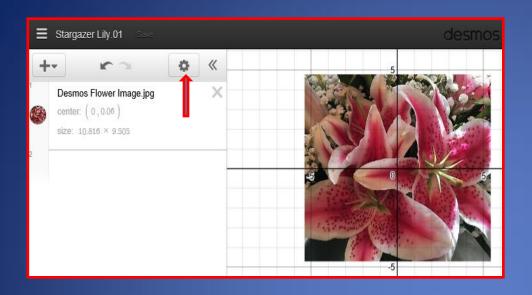
To **Move** the image, click on the center point and drag the image to where you'd like to place it. Or, you can manually change the coordinate of the center point in the expression list. This will automatically move the image so that its center is at that new coordinate point. To **Resize** the image, click and drag any one of the outer points surrounding the image and drag outwards to make larger and inwards to make smaller.

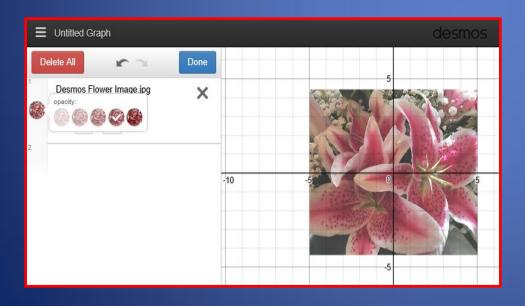


Now is a good time to Save your file. You must be signed in to do that. We use our Google sign-in and a unique password.

The flower image is centered at the origin. It can be resized and moved to another location.

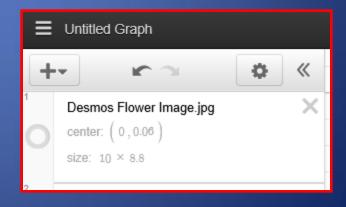


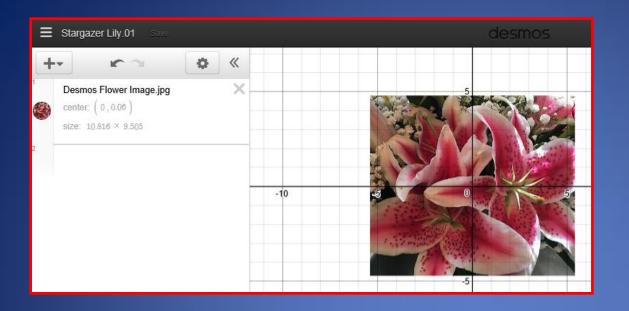




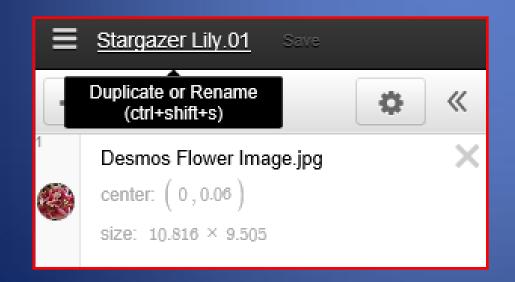
Click and hold the little gear icon above the image block. Now you can control the opacity of the picture.

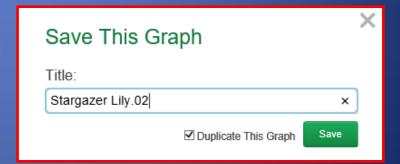
You can also click on the little flower icon and make the image invisible!





You may want to duplicate your file so you can add something later.
Keep the original but save a copy with a new name.

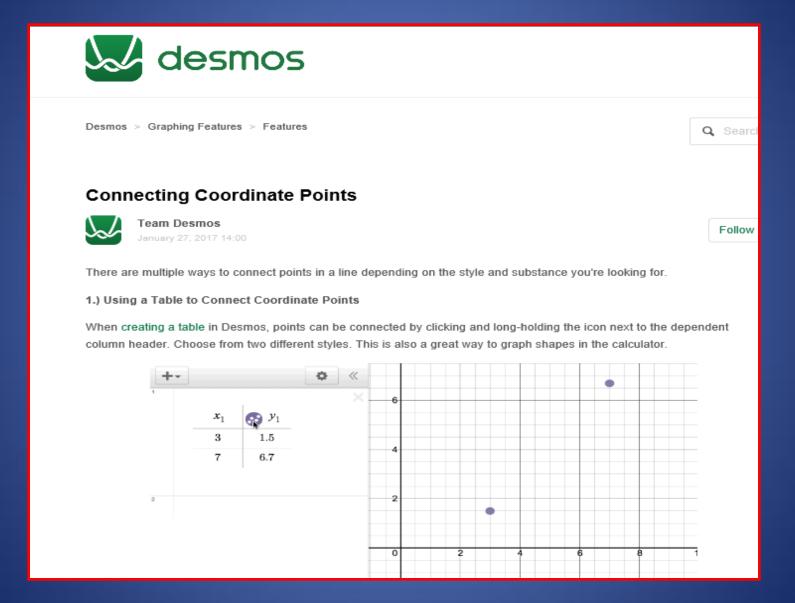




## Steps to Save A Photo:

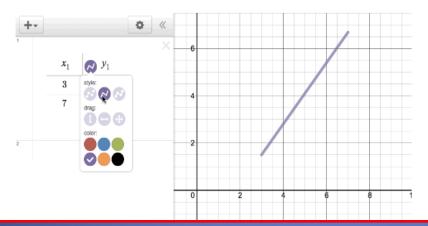
- 1. Take photo with phone, tablet, or Chrome book.
- 2. Next, email the picture from your phone to your school email
- 3. Then, save it to your Google Drive by downloading it.
- 4. Import from your Google Drive into Desmos.

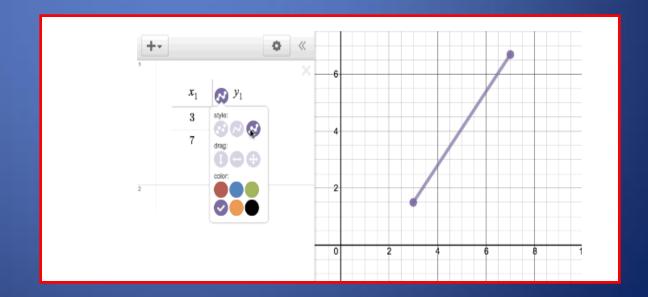
### http://support.desmos.com/hc/en-us/articles/205841709-Connecting-Coordinate-Points



#### 1.) Using a Table to Connect Coordinate Points

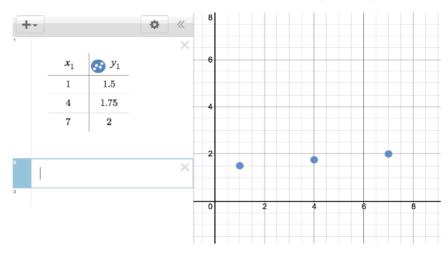
When creating a table in Desmos, points can be connected by clicking and long-holding the icon next to the dependent column header. Choose from two different styles. This is also a great way to graph shapes in the calculator.





#### 2.) Using Linear Regression to Connect Points

Points that display a linear pattern can be connected with an extended line by running a linear regression on the table data.

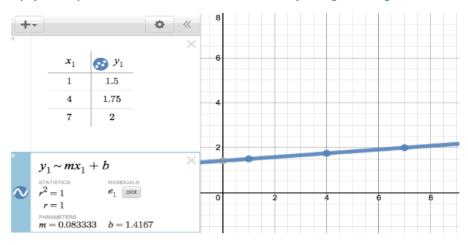


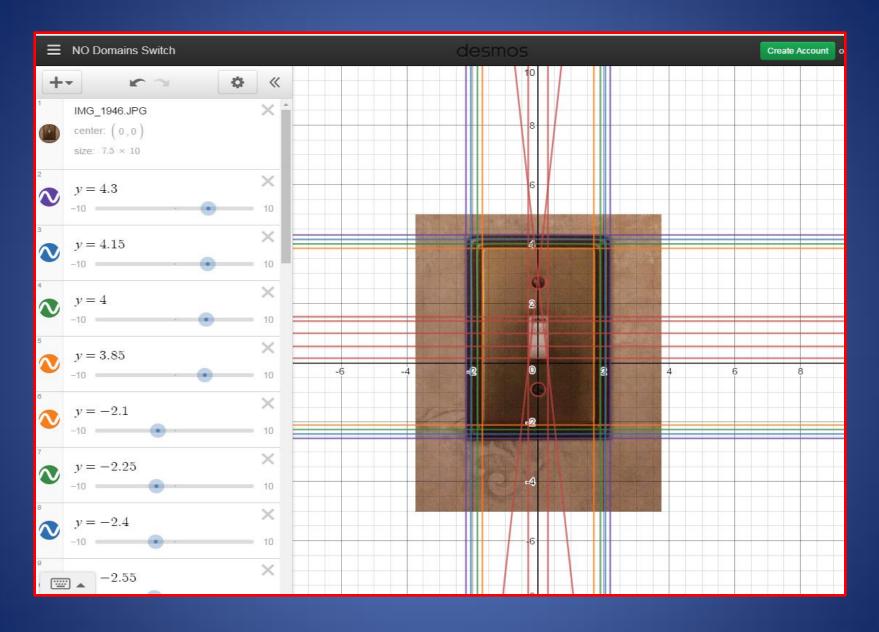
# $y_{\#} \sim mx_{\#} + b$

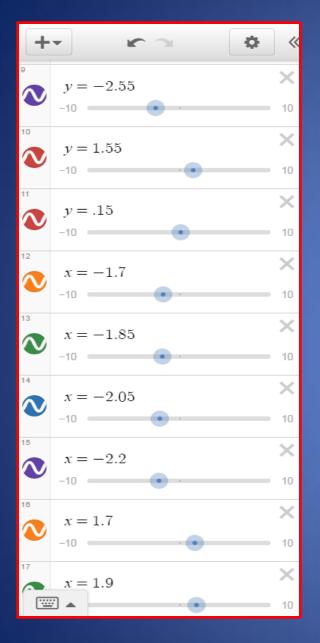
$$y_1 \sim mx_1 + b$$

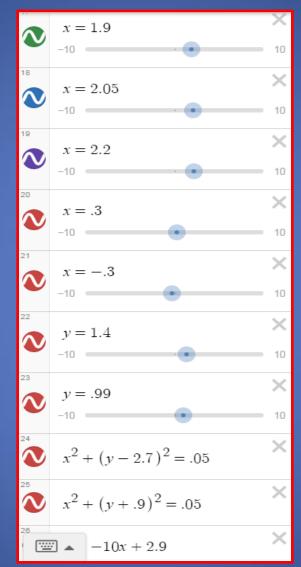
#### 2.) Using Linear Regression to Connect Points

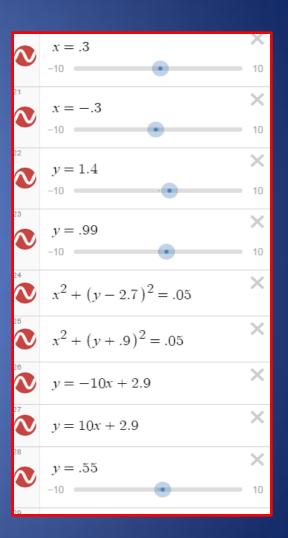
Points that display a linear pattern can be connected with an extended line by running a linear regression on the table data.

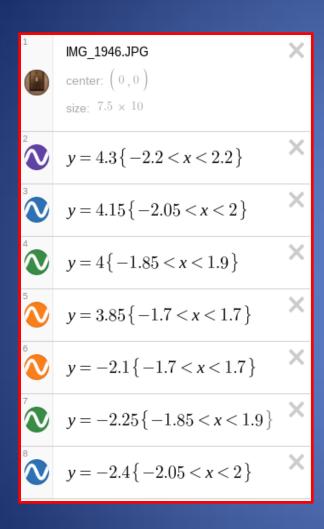


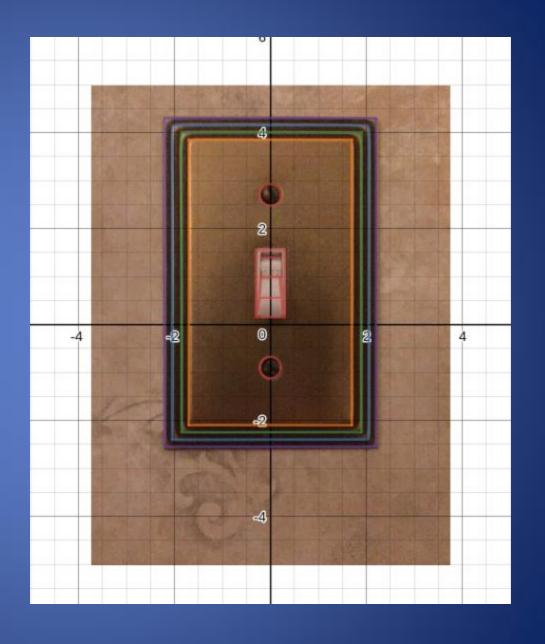












$$y = -2.55\{2.2 > x > -2.2\}$$

$$y = 1.55\{.3 > x > -.3\}$$

$$y = .15\{.3 > x > -.3\}$$

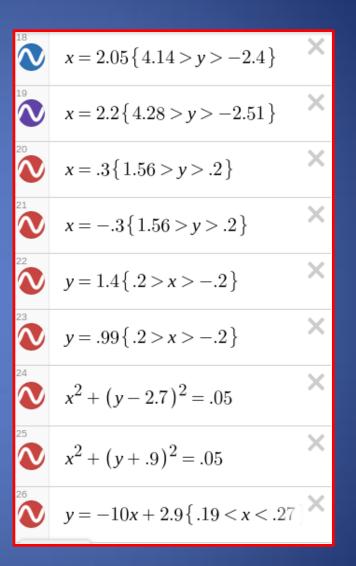
$$x = -1.7\{3.85 > y > -2.1\}$$

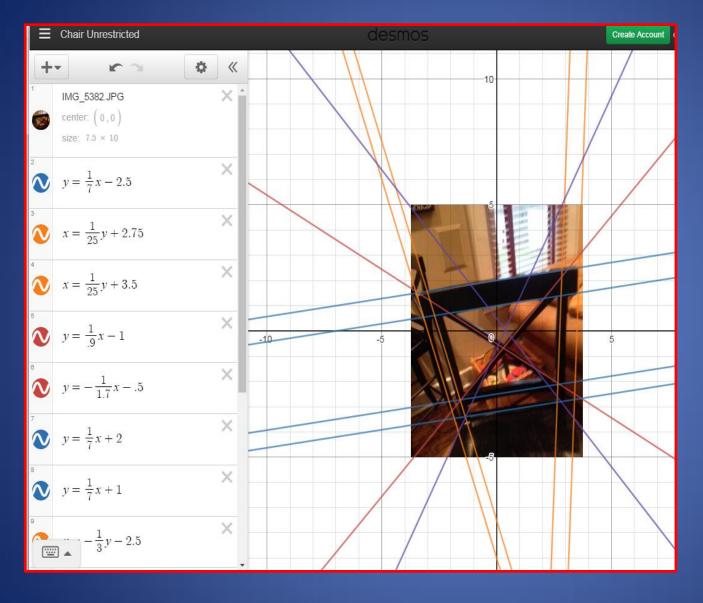
$$x = -1.85\{-2.24 < y < 4\}$$

$$x = -2.05\{4.1 > y > -2.4\}$$

$$x = -2.2\{4.28 > y > -2.51\}$$

$$x = 1.7\{3.85 > y > -2.1\}$$





$$y = -\frac{1}{1.7}x - .5$$

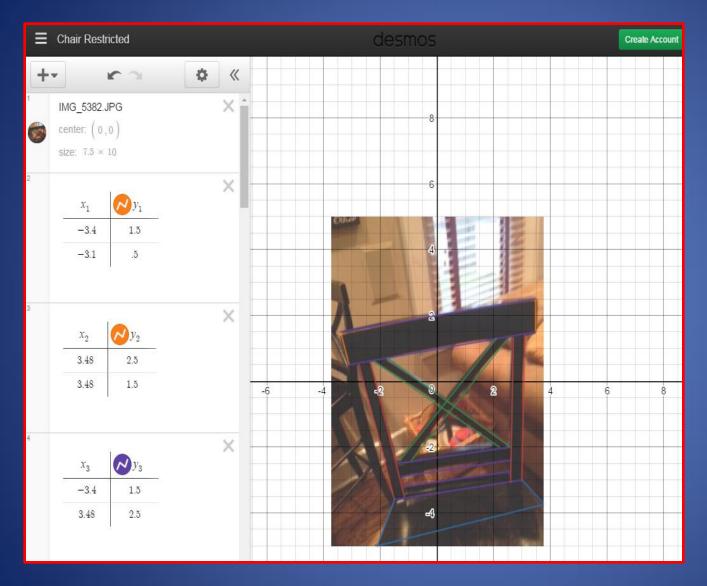
$$y = \frac{1}{7}x + 2$$

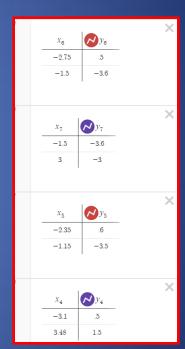
$$y = \frac{1}{7}x + 1$$

$$x = -\frac{1}{3}y - 2.5$$

$$x = -\frac{1}{3}y - 3$$

$$y = \frac{1}{7}x - 3.2$$

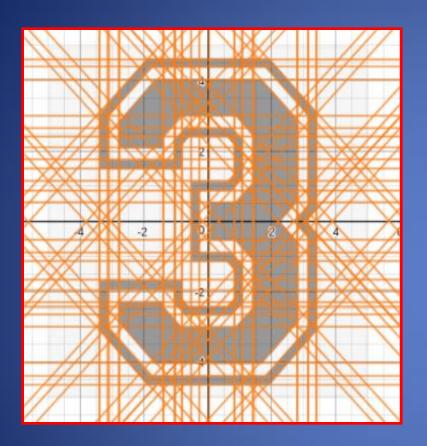


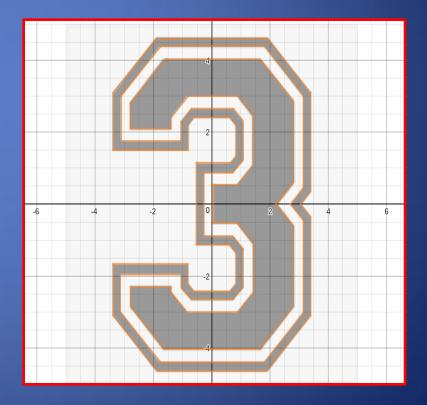


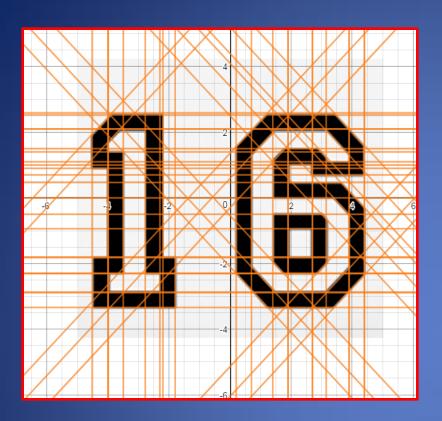
_			
	$x_8$	$\sim y_8$	^
	3.1	1.4	
	3	-3	
10			×
	<i>x</i> <sub>9</sub>	$\sim y_9$	
	2.7	1.32	
	2.6	-3.05	
		'	
11			×
	$x_{11}$	$\bigvee y_{11}$	
	-1.4	-2.5	_
	2.6	-2	_
		1	
12			×
	<i>x</i> <sub>10</sub>	$\bigvee y_{10}$	
	-1.2	-3.2	
	2.55	-2.75	_

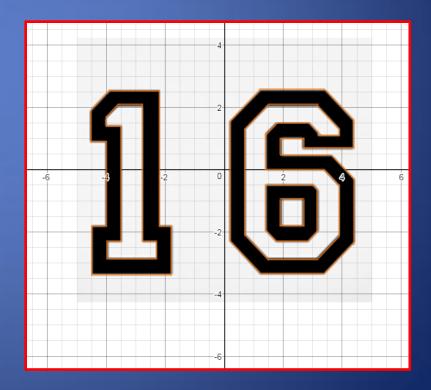
	$x_{14}$	$V_{14}$	
	-1.75	.7	
	2.6	-2	
14			
	.	<b>1</b> 11	×
	x <sub>13</sub>	<b>∨</b> y <sub>13</sub>	
	-2.2	.6	
	2.2	-2	
	,		
15			$\times$
	$x_{15}$	$\bigvee y_{15}$	
	2.1	1.3	
	-1.3	-2.4	
	'		
16		. –	×
	$x_{12}$	$V_{12}$	
	-1.25	-2.9	
	2.6	-2.4	
		I	

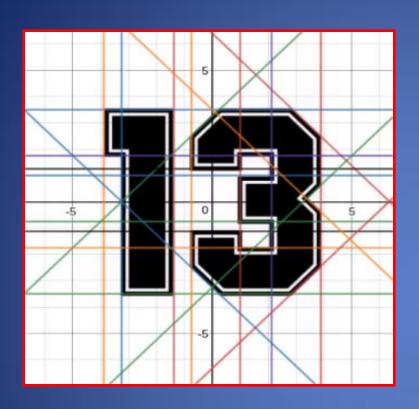


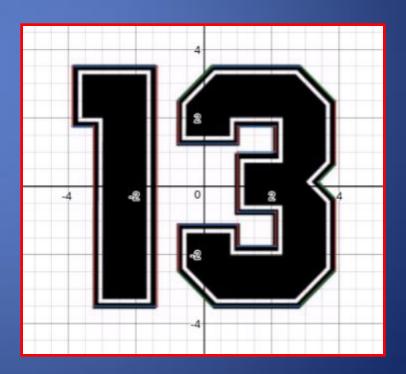


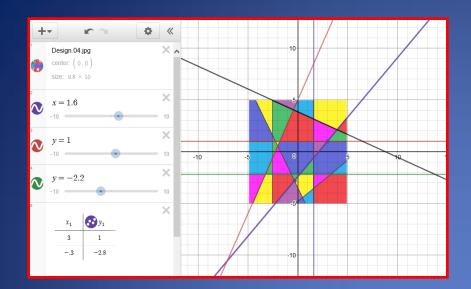


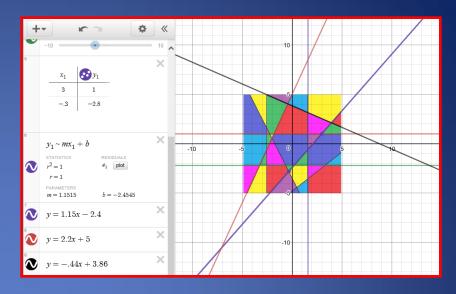


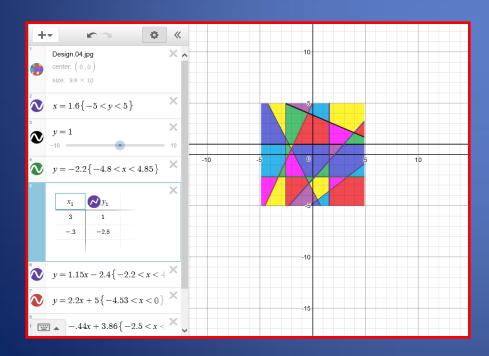




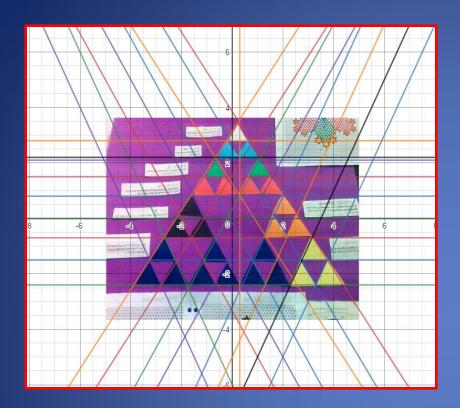


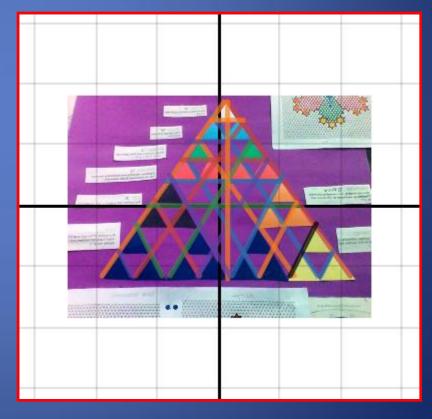


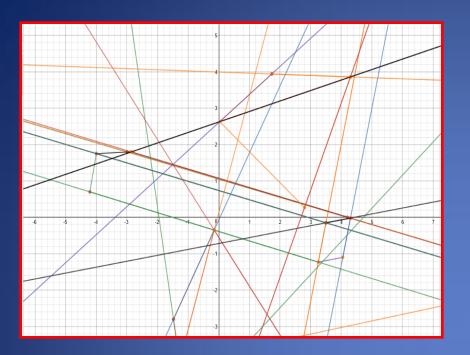


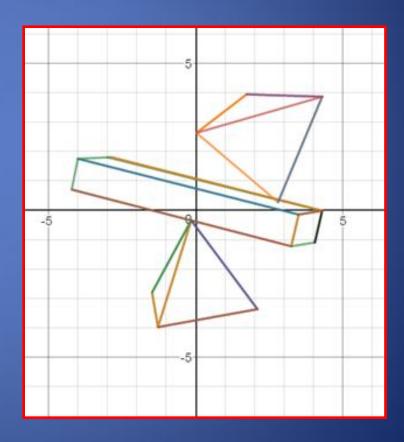


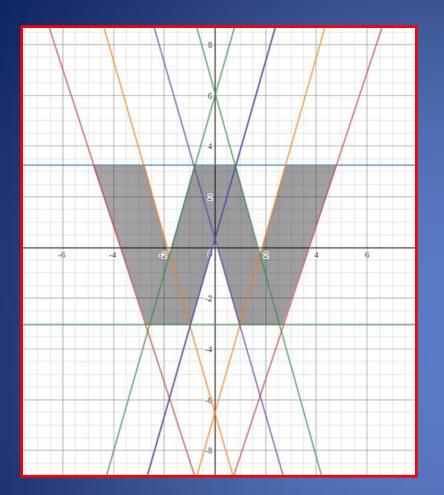
This graphic design was done in a Paint document and saved as a jpeg so it could be inserted onto a new set of coordinate axes. The picture on the left shows the beginning of the restrictions on the equations.

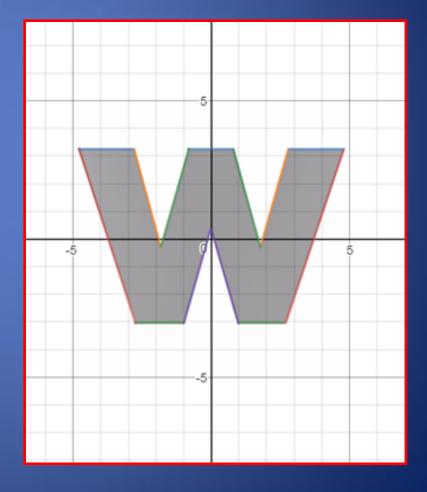


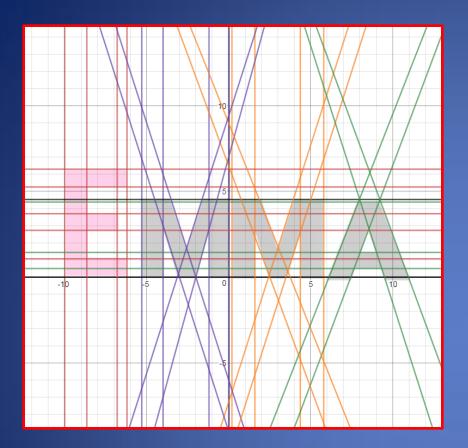


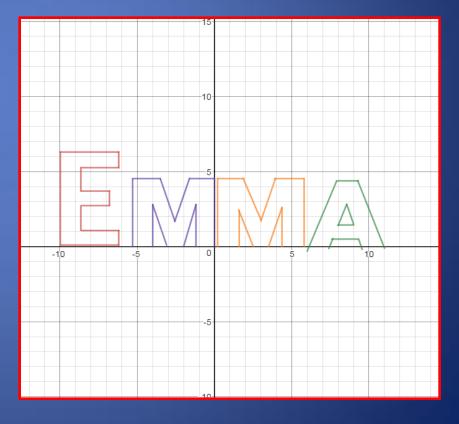


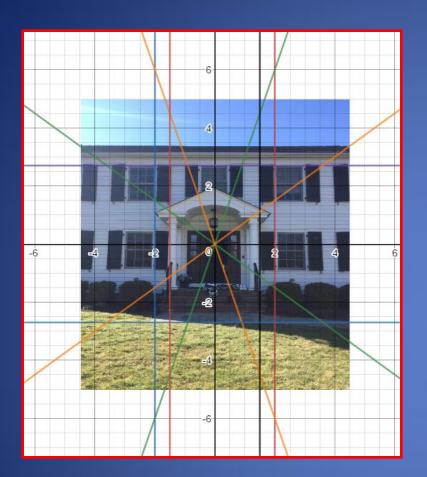


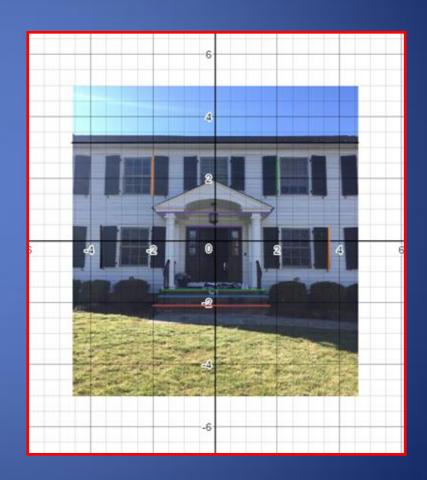


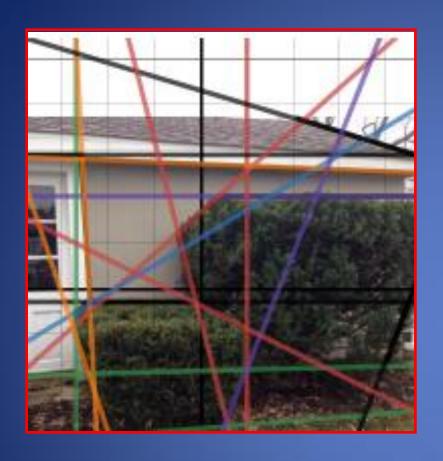


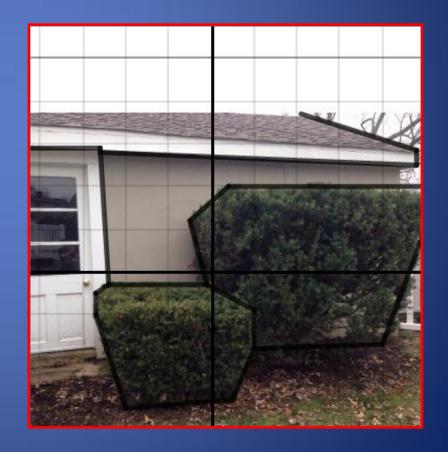


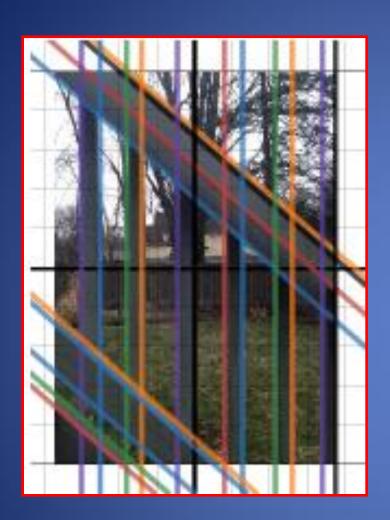


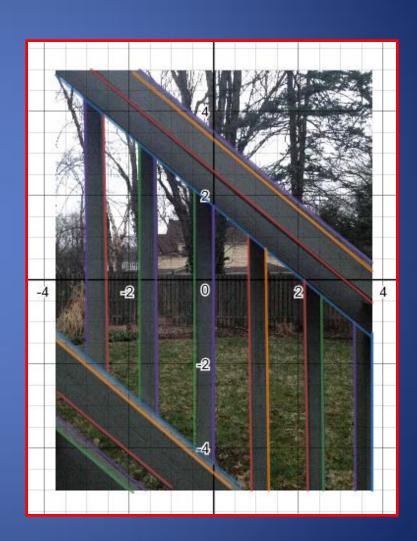




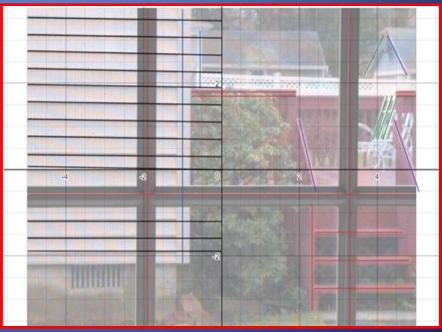


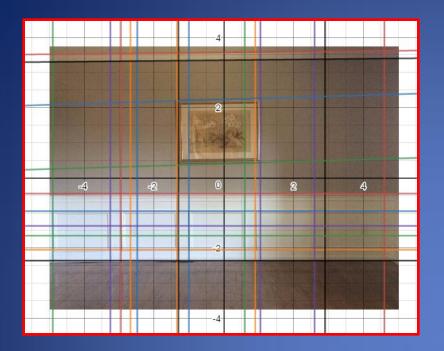


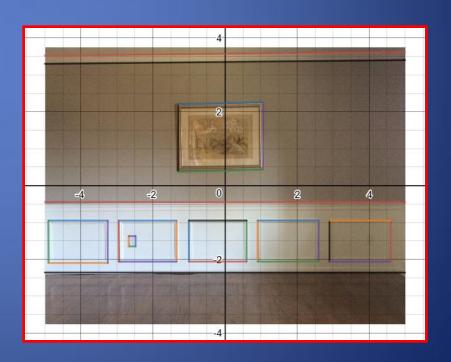


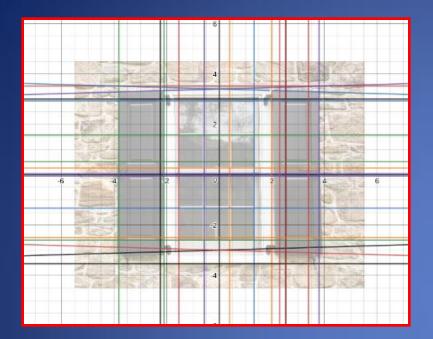


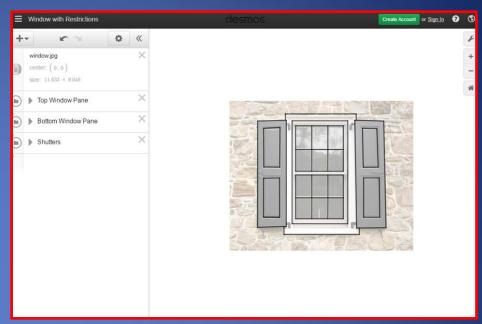


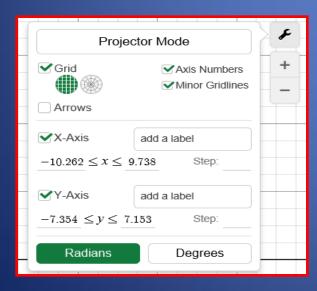






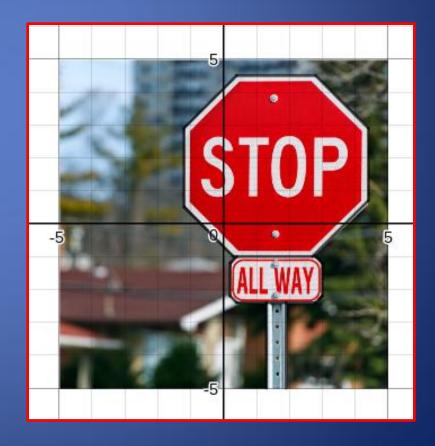


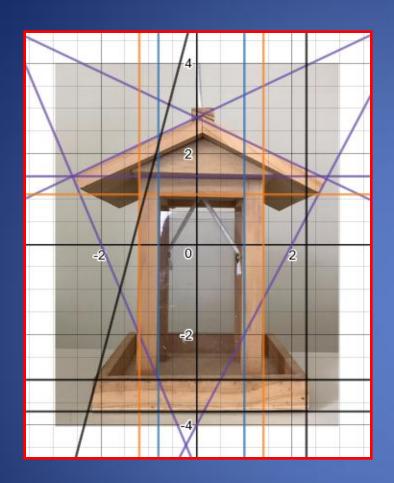


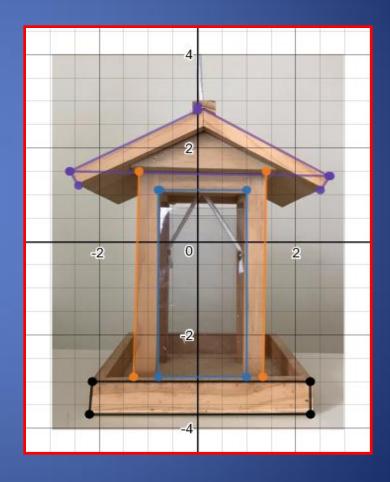


The icon with the wrench allows you to adjust the view of the final picture. This student eliminated the grid and axes so that only the window and shutters were visible.









## Grading Rubric: consider the following attributes:

- \*Original photograph or drawing
- \*The photograph has vertical and horizontal lines, and lines with positive and negative slopes
- \*There are at least 10 12 lines set up with the equation y = mx + b and/or using a table and line of best fit
- \*Student does the unrestricted and the restricted views of the photograph
- \*Level of difficulty for the equations
- \*Use of folders



# Thank you for coming to this presentation!

If you would like a copy of the slide show, please send an email to:

Stephanie Cooperman: Shc283@att.net

or

Neil Cooperman: Ncoop@att.net